

Appendix 1

RMS Values of Commonly Observed Converter Waveforms

A.1 Results for some common waveforms

See text for results

A.2 General piecewise waveform

How to compute the rms value of a waveform that can be broken into smaller piecewise segments

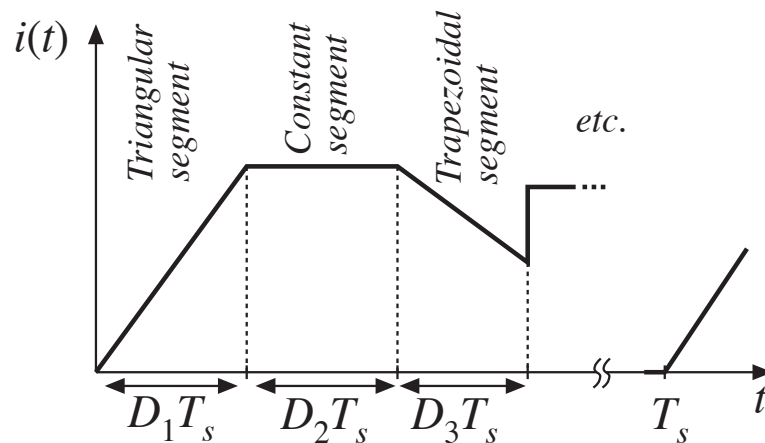
Example: transistor current waveform, including effects of short turn-on current spike

A.2 General piecewise waveform

Basic expression for rms value of waveform $v(t)$ having period T :

$$(\text{rms value}) = \sqrt{\frac{1}{T} \int_0^T v^2(t) dt}$$

Suppose the waveform can be represented as a series of segments, with the k^{th} segment having length $D_k T_s$ and with T_s equal to the switching period:

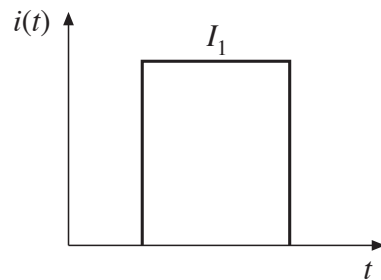


Then the rms value can be expressed as:

$$rms = \sqrt{\sum_{k=1}^n D_k u_k}$$

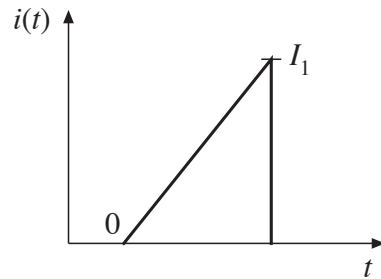
where u_k is the contribution of the k^{th} segment — see following slides

Some basic segment shapes



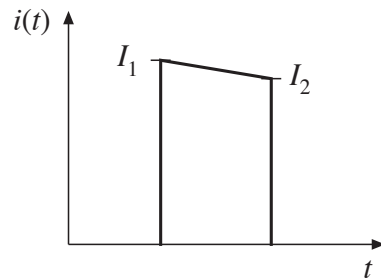
Constant segment

$$u_k = I_1^2$$



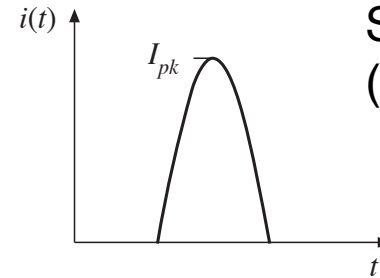
Triangular segment

$$u_k = \frac{1}{3} I_1^2$$



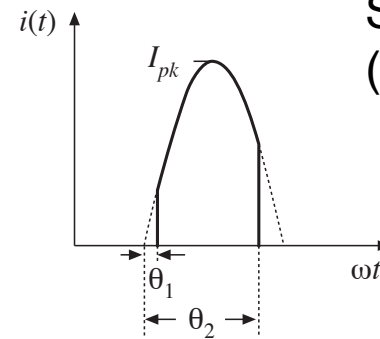
Trapezoidal segment

$$u_k = \frac{1}{3} (I_1^2 + I_1 I_2 + I_2^2)$$



Sinusoidal segment
(half or full period)

$$u_k = \frac{1}{2} I_{pk}^2$$



Sinusoidal segment
(partial period)

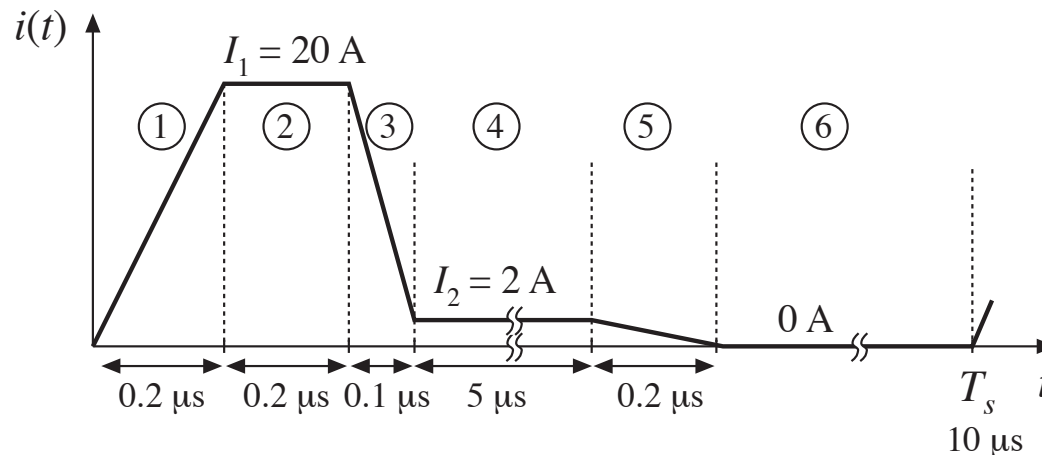
$$u_k = \frac{1}{2} I_{pk}^2 \left(1 - \frac{\sin(\theta_2 - \theta_1) \cos(\theta_2 + \theta_1)}{(\theta_2 - \theta_1)} \right)$$

Example

Transistor current waveform, including turn-on current spike induced by diode reverse recovery

The turn-on current spike is short but of high magnitude. Does it significantly increase the rms current?

The observed current waveform is approximated by piecewise linear segments as shown below



Six segments:

1-3 are from diode reverse recovery

4 is transistor on time

5 is transistor turn-off transition

6 is transistor off time

Calculation

1. Triangular segment:

$$D_1 = (0.2 \mu\text{s}) / (10 \mu\text{s}) = 0.02$$

$$u_1 = I_1^2 / 3 = (20 \text{ A})^2 / 3 = 133 \text{ A}^2$$

2. Constant segment:

$$D_2 = (0.2 \mu\text{s}) / (10 \mu\text{s}) = 0.02$$

$$u_2 = I_1^2 = (20 \text{ A})^2 = 400 \text{ A}^2$$

3. Trapezoidal segment:

$$D_3 = (0.1 \mu\text{s}) / (10 \mu\text{s}) = 0.01$$

$$u_3 = (I_1^2 + I_2^2 + I_3^2) / 3 = 148 \text{ A}^2$$

4. Constant segment:

$$D_4 = (5 \mu\text{s}) / (10 \mu\text{s}) = 0.5$$

$$u_4 = I_2^2 = (2 \text{ A})^2 = 4 \text{ A}^2$$

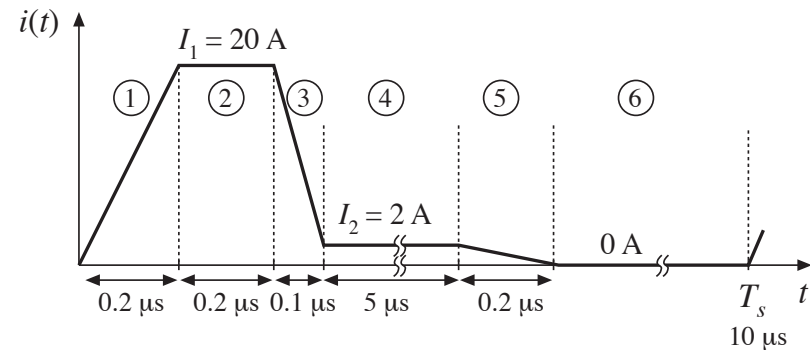
5. Triangular segment:

$$D_5 = (0.2 \mu\text{s}) / (10 \mu\text{s}) = 0.02$$

$$u_5 = I_2^2 / 3 = (2 \text{ A})^2 / 3 = 1.3 \text{ A}^2$$

6. Zero segment:

$$u_6 = 0$$



Result:

$$rms = \sqrt{\sum_{k=1}^6 D_k u_k} = 3.76 \text{ A}$$

Without the current spike, the rms value is approximately 1.4 A. So in this example, the diode reverse recovery significantly increases the transistor rms current.