Appendix 1 RMS Values of Commonly Observed Converter Waveforms

A.1 Results for some common waveforms See text for results

A.2 General piecewise waveform

How to compute the rms value of a waveform that can be broken into smaller piecewise segments

Example: transistor current waveform, including effects of short turn-on current spike

A.2 General piecewise waveform

Basic expression for rms value of waveform v(t) having period *T*:

Suppose the waveform can be represented as a series of segments, with the k^{th} segment having length $D_k T_s$ and with T_s equal to the switching period:

(rms value) =
$$\sqrt{\frac{1}{T} \int_0^T v^2(t) dt}$$



Then the rms value can be expressed as:

$$rms = \sqrt{\sum_{k=1}^{n} D_k u_k}$$

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where u_k is the contribution of the k^{th} segment — see following slides

Some basic segment shapes



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Appendix A: RMS Values

Example

Transistor current waveform, including turn-on current spike induced by diode reverse recovery

- The turn-on current spike is short but of high magnitude. Does it significantly increase the rms current?
- The observed current waveform is approximated by piecewise linear segments as shown below



Six segments:

1-3 are from diode reverse recovery

4 is transistor on time

5 is transistor turn-off transition

6 is transistor off time

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Appendix A: RMS Values

Calculation

1. Triangular segment:

 $D_1 = (0.2 \ \mu s) / (10 \ \mu s) = 0.02$

 $u_1 = I_1^2 / 3 = (20 \text{ A})^2 / 3 = 133 \text{ A}^2$

2. Constant segment:

 $D_2 = (0.2 \ \mu s)/(10 \ \mu s) = 0.02$ $u_2 = I_1^2 = (20 \ A)^2 = 400 \ A^2$

3. Trapezoidal segment:

$$D_3 = (0.1 \ \mu \text{s})/(10 \ \mu \text{s}) = 0.01$$
$$u_3 = (I_1^2 + I_2^2 + I_3^2)/3 = 148 \text{ A}^2$$

4. Constant segment:

$$D_4 = (5 \ \mu s)/(10 \ \mu s) = 0.5$$

 $u_4 = I_2^2 = (2 \ A)^2 = 4 \ A^2$

5. Triangular segment:

$$D_5 = (0.2 \ \mu s) / (10 \ \mu s) = 0.02$$

 $u_5 = I_2^2 / 3 = (2 \ A)^2 / 3 = 1.3 \ A^2$

6. Zero segment:



5

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$$i(t)$$
 $I_1 = 20 \text{ A}$
 1 2 3 4 5 6
 $I_2 = 2 \text{ A}$ 0 A
 $0.2 \ \mu \text{s}$ $0.2 \ \mu \text{s}$ $0.1 \ \mu \text{s}$ $5 \ \mu \text{s}$ $0.2 \ \mu \text{s}$ $T_s \ t$
 $10 \ \mu \text{s}$

Result:

$$rms = \sqrt{\sum_{k=1}^{6} D_k u_k} = 3.76 \text{ A}$$

Without the current spike, the rms value is approximately 1.4 A. So in this example, the diode reverse recovery significantly increases the transistor rms current.

Appendix A: RMS Values