Chapter 17 Line-Commutated Rectifiers

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17.1 The single-phase full-wave rectifier



Full-wave rectifier with dc-side *L*-*C* filter

Two common reasons for including the dc-side *L*-*C* filter:

- Obtain good dc output voltage (large *C*) and acceptable ac line current waveform (large *L*)
- Filter conducted EMI generated by dc load (small *L* and *C*)

17.1.1 Continuous conduction mode



THD =
$$\sqrt{\left(\frac{1}{\text{distortion factor}}\right)^2 - 1} = 48.3\%$$

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17.1.2 Discontinuous conduction mode



Typical distortion factor of a full-wave rectifier with no inductor is in the range 55% to 65%, and is governed by ac system inductance.

17.1.3 Behavior when *C* is large



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Sometimes the L-C filter is present only to remove high-frequency conducted EMI generated by the dc load, and is not intended to modify the ac line current waveform. If L and C are both zero, then the load resistor is connected directly to the output of the diode bridge, and the ac line current waveform is purely sinusoidal.

An approximate argument: the *L*-*C* filter has negligible effect on the ac line current waveform provided that the filter input impedance Z_i has zero phase shift at the second harmonic of the ac line frequency, $2f_L$.



Approximate THD



Example



Typical ac line current and voltage waveforms, near the boundary between continuous and discontinuous modes and with small dc filter capacitor. $f_0/f_L = 10$, Q = 1

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17.2 The Three-Phase Bridge Rectifier



17.2.1 Continuous conduction mode

Fourier series:

$$i_a(t) = \sum_{n=1,5,7,11,\dots}^{\infty} \frac{4}{n\pi} I_L \sin\left(\frac{n\pi}{2}\right) \sin\left(\frac{n\pi}{3}\right) \sin\left(n\omega t\right)$$

- Similar to square wave, but missing triplen harmonics
- THD = 31%
- Distortion factor = $3/\pi = 95.5\%$
- In comparison with single phase case:

the missing 60° of current improves the distortion factor from 90% to 95%, because the triplen harmonics are removed



A typical CCM waveform



Inductor current contains sixth harmonic ripple (360 Hz for a 60 Hz ac system). This ripple is superimposed on the ac line current waveform, and influences the fifth and seventh harmonic content of $i_a(t)$.

17.2.2 Discontinuous conduction mode



Phase *a* current contains pulses at the positive and negative peaks of the line-to-line voltages $v_{ab}(t)$ and $v_{ac}(t)$. Distortion factor and THD are increased. Distortion factor of the typical waveform illustrated above is 71%.

17.3 Phase control

Replace diodes with SCRs:

Phase control waveforms:



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Dc output voltage vs. delay angle α



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17.3.1 Inverter mode



If the load is capable of supplying power, then the direction of power flow can be reversed by reversal of the dc output voltage *V*. The delay angle α must be greater than 90°. The current direction is unchanged.

17.3.2 Harmonics and power factor

Fourier series of ac line current waveform, for large dc-side inductance:

$$i_a(t) = \sum_{n=1,5,7,11,\dots}^{\infty} \frac{4}{n\pi} I_L \sin\left(\frac{n\pi}{2}\right) \sin\left(\frac{n\pi}{3}\right) \sin\left(n\omega t - n\alpha\right)$$

Same as uncontrolled rectifier case, except that waveform is delayed by the angle α . This causes the current to lag, and decreases the displacement factor. The power factor becomes:

power factor = $0.955 |\cos(\alpha)|$

When the dc output voltage is small, then the delay angle α is close to 90° and the power factor becomes quite small. The rectifier apparently consumes reactive power, as follows:

$$Q = \sqrt{3} I_{a, rms} V_{L-L, rms} \sin \alpha = I_L \frac{3\sqrt{2}}{\pi} V_{L-L, rms} \sin \alpha$$

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Real and reactive power in controlled rectifier at fundamental frequency



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17.4 Harmonic trap filters

A passive filter, having resonant zeroes tuned to the harmonic frequencies



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Harmonic trap



Filter transfer function



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Simple example



Simple example: transfer function



- Series resonance: fifth harmonic trap
- Parallel resonance: C_1 and L_s
- Parallel resonance tends to increase amplitude of third harmonic
- Q of parallel resonance is larger than Q of series resonance

Example 2



Approximate impedance asymptotes



Transfer function asymptotes



Bypass resistor



Harmonic trap filter with high-frequency roll-off



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17.5 Transformer connections

Three-phase transformer connections can be used to shift the phase of the voltages and currents
This shifted phase can be used to cancel out the low-order harmonics
Three-phase delta-wye transformer connection shifts phase by 30°:



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Twelve-pulse rectifier



Waveforms of 12 pulse rectifier



- Ac line current contains 1st, 11th, 13th, 23rd, 25th, etc. These harmonic amplitudes vary as 1/n
- 5th, 7th, 17th, 19th, etc. harmonics are eliminated

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Rectifiers with high pulse number

Eighteen-pulse rectifier:

- Use three six-pulse rectifiers
- Transformer connections shift phase by 0°, +20°, and -20°
- No 5th, 7th, 11th, 13th harmonics

Twenty-four-pulse rectifier

- Use four six-pulse rectifiers
- Transformer connections shift phase by 0°, 15°, -15°, and 30°
- No 5th, 7th, 11th, 13th, 17th, or 19th harmonics

If *p* is pulse number, then rectifier produces line current harmonics of number $n = pk \pm 1$, with k = 0, 1, 2, ...