

A Self-Coherence Based Anti-Jamming GPS Receiver

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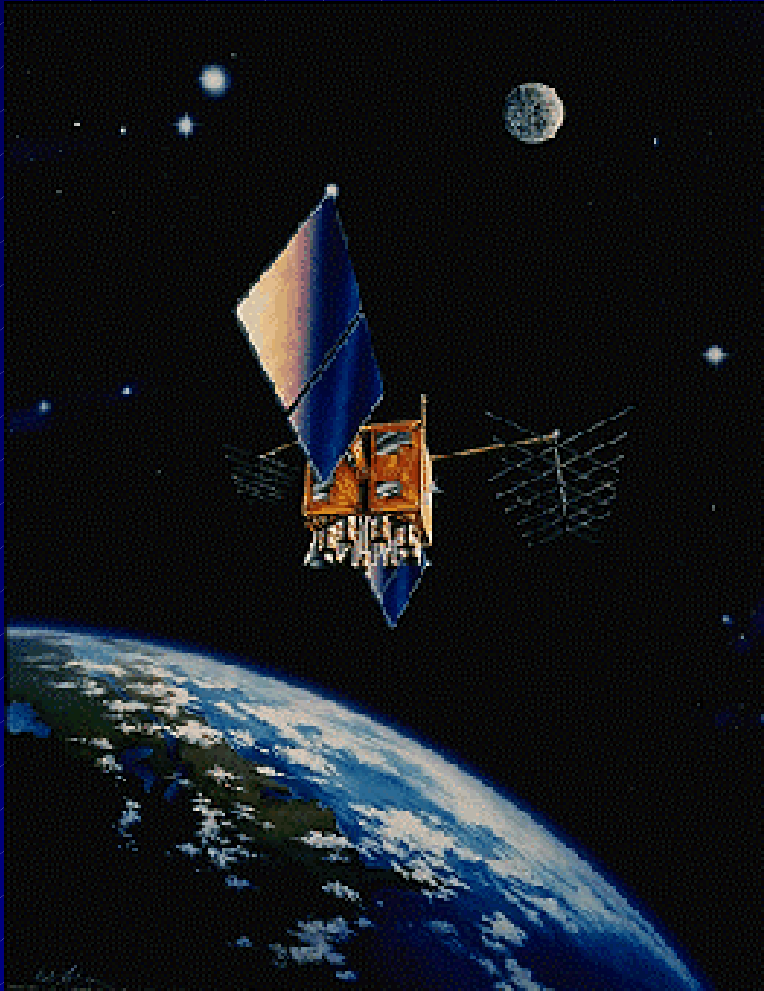
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OUTLINE

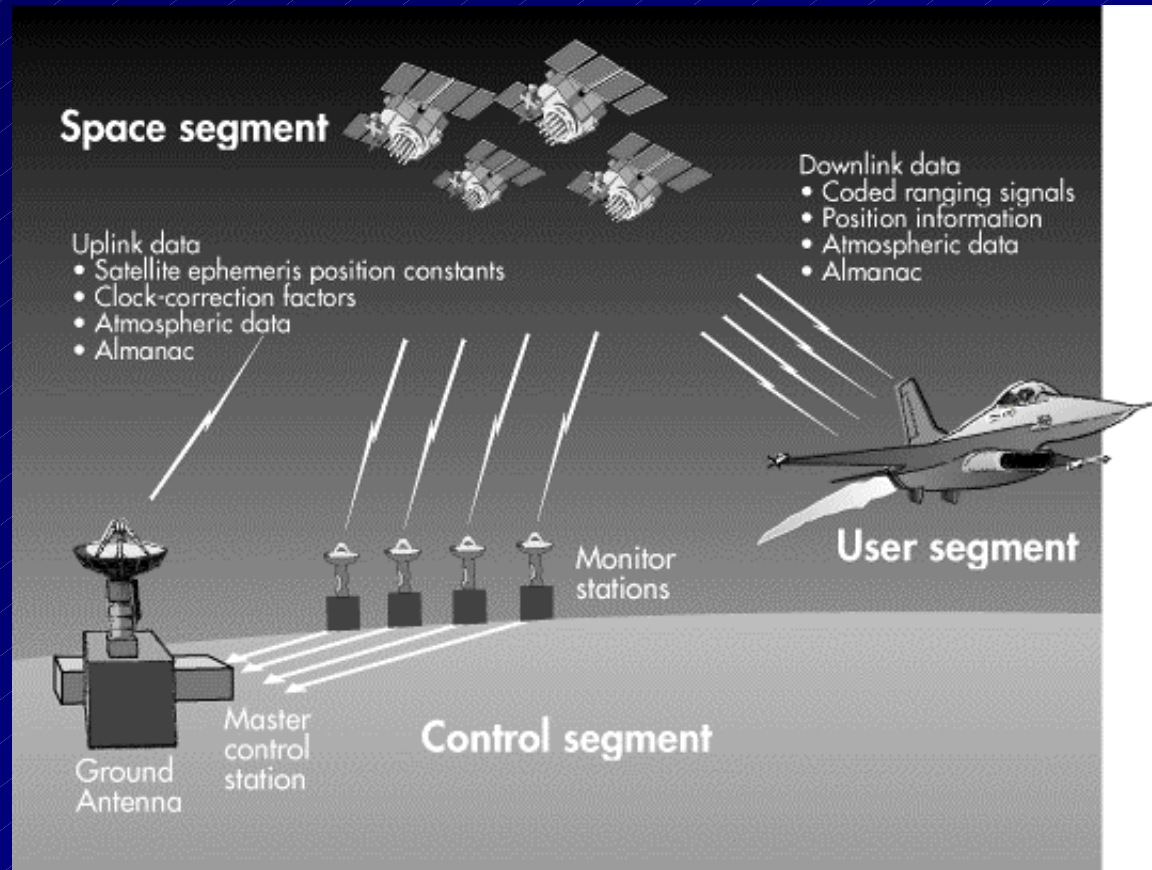
- GPS overview
- Existing techniques in GPS interference suppression
- Self-coherence based anti-jamming GPS receiver
- Simulation results
- Conclusions

WHAT IS GPS?



- GPS is a satellite-based all-weather navigation system providing precise position, velocity, and timing information.
- Global navigation systems
 - GPS: US
 - GLONASS: Russia
 - Galileo: Europe

GPS COMPONENTS



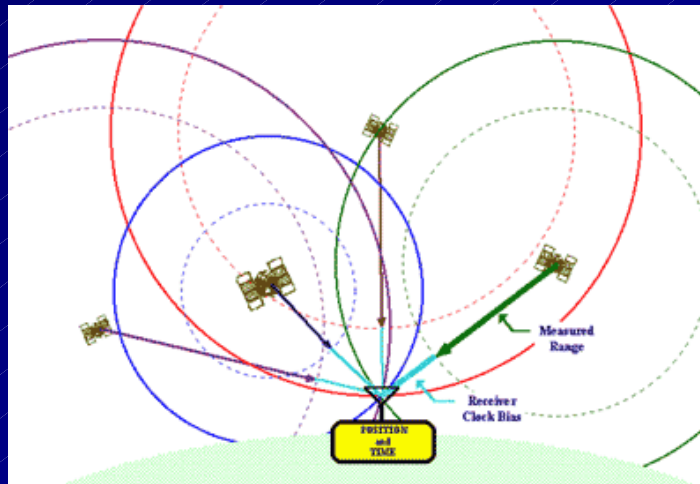
- Space segment: satellite constellation
- Control segment: ground stations
- User segment: receivers

HOW GPS WORKS?

- GPS uses one-way time-of-arrival ranging to determine user position - measure the direct path signal travel time from a satellite to a user's receiving device.



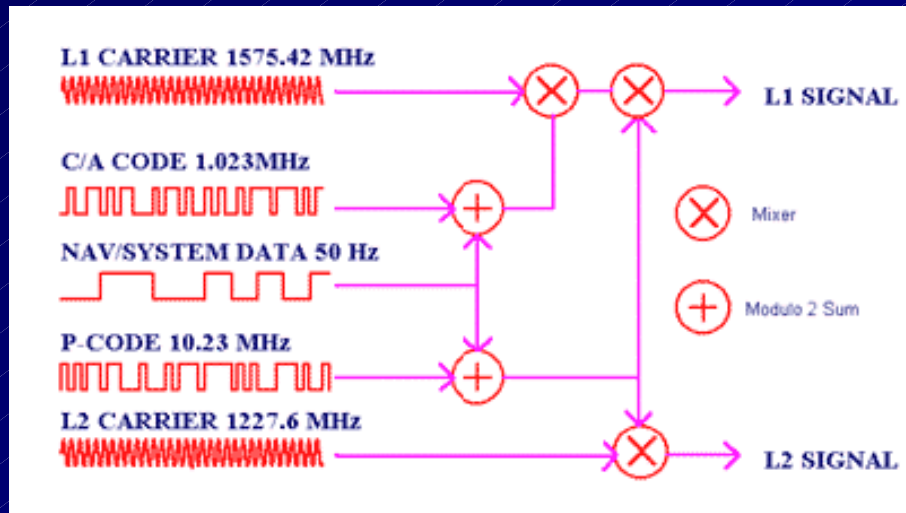
- **Pseudorange**: the range from the satellite plus clock offset



- Geolocation of the receiver: the intersection of pseudoranges from a set of satellites (minimum 4).

GPS SIGNAL

GPS employs **direct-sequence spread-spectrum (DS-SS)** signaling



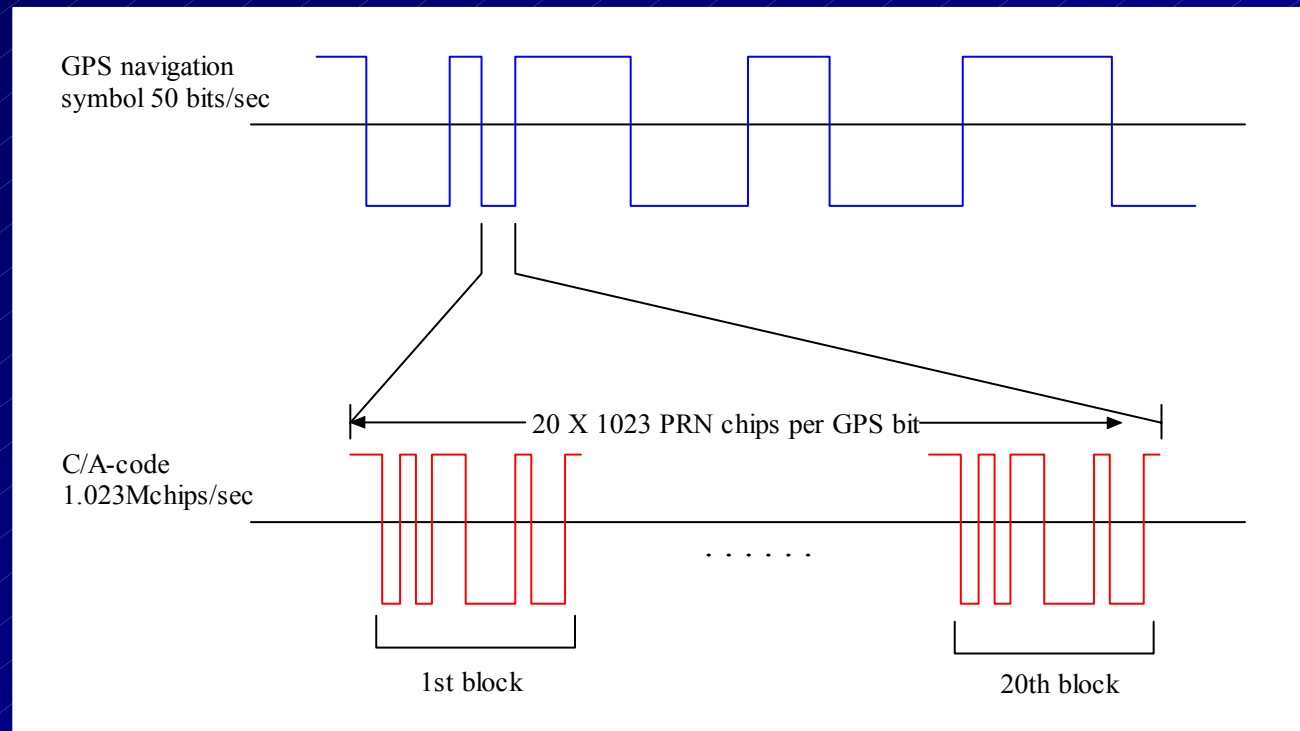
- Two *L*-band frequencies:
 - $L1=1.57542$ GHz
 - $L2=1.2276$ GHz

- Two pseudorandom codes

- **Coarse/acquisition (C/A) code**: chip rate 1.023 Mchips/sec, BW 2 MHz, repeats every millisecond.
- **Precision (P) code**: chip rate 10.23 Mchips/sec, BW 20 MHz, repeats about every week (military use).

GPS SIGNAL (Cont'd)

■ GPS C/A signal waveform:



CHALLENGES IN GPS

- Two dominant sources of errors in precision GPS:
 - **Interference**: reduces the SNR of the GPS signal such that the receiver is unable to obtain measurements from the GPS satellite.
 - **Multipath**: broadens and biases the cross-correlation function.

GPS AND DSSS SYSTEMS

■ Common

- Both use PN
- Both require synchronization
 - ◆ DSSS: desreading
 - ◆ GPS: desreading and pseudorange measurement

■ Difference

- Multipath
 - ◆ DSSS: improves system performance due to diversity – **constructive** 😊
 - ◆ GPS: results in erroneous pseudorange measurements – **destructive** ☹️
- Near-far phenomena
 - ◆ DSSS: a **severe problem** ☹️
 - ◆ GPS: **not a problem** 😊

INTERFERENCE IN GPS

Types of Interference in GPS:

- Additive white Gaussian noise (AWGN)
 - Broadband interference can sometimes be modeled as AWGN
- Continuous wave (CW)
 - A pure tone or narrowband modulated signal.
 - Chirp signal
- Pulsed interference (e.g., radars)
 - Effectively “shoots holes” in the received signal

EXISTING TECHNIQUES

■ Maximum Likelihood Approach

(Time-delay and carrier-phase estimation)

- ◆ Single-antenna approach
- ◆ Multiple-antenna approach

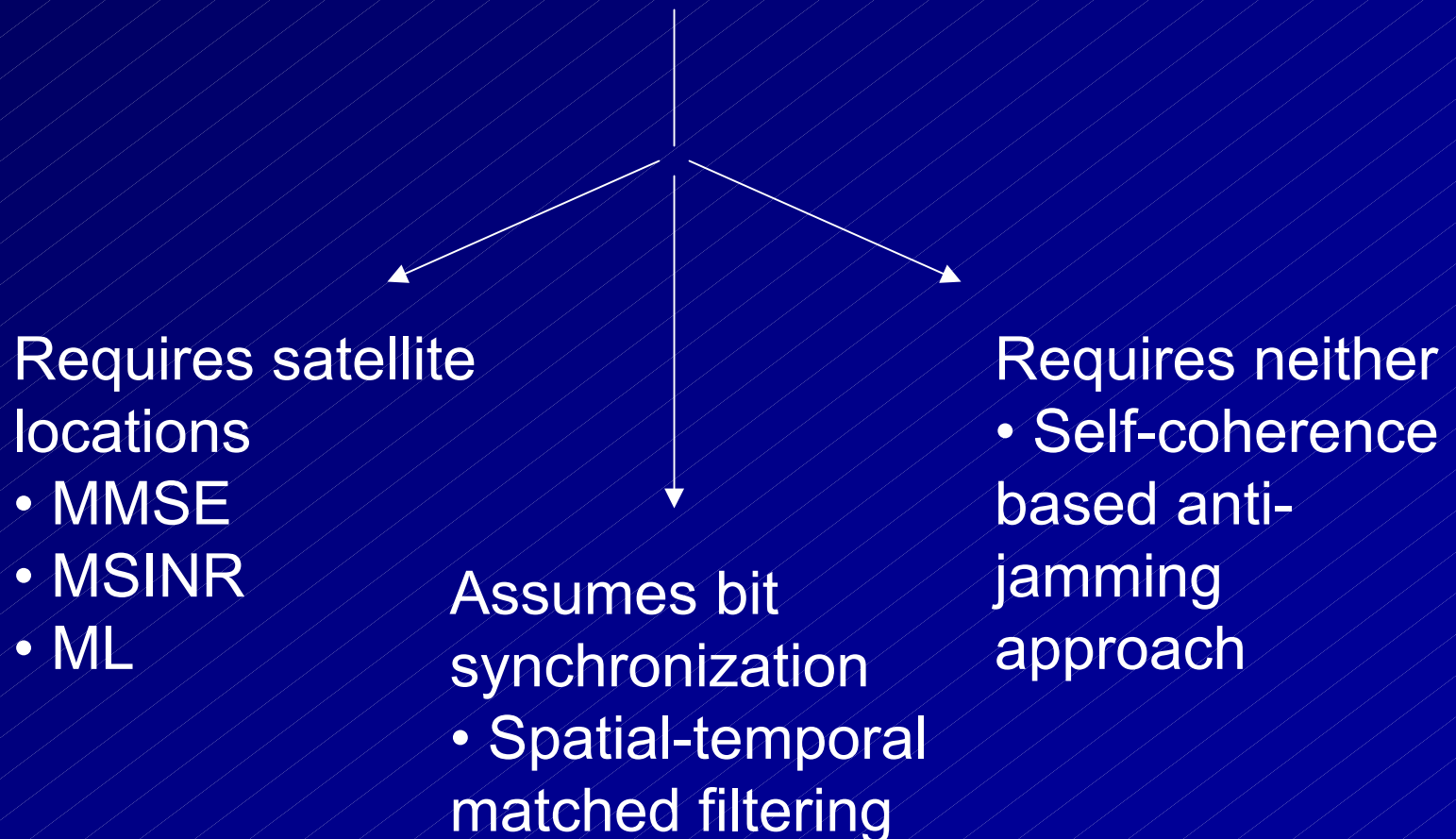
■ Suboptimum Methods

(Interference Suppression)

- Space-time adaptive method
- Time-frequency method
- Navigation data demodulation

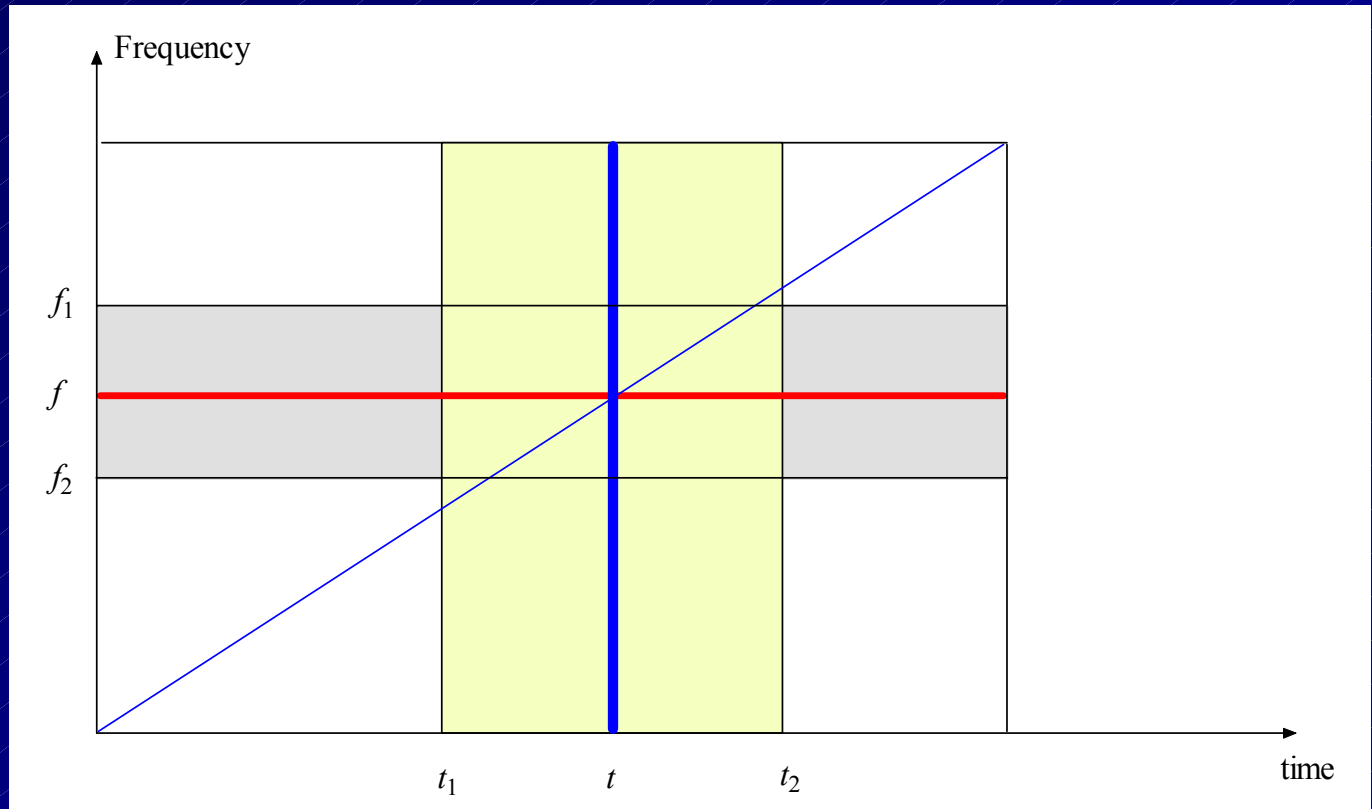
EXISTING TECHNIQUES

GPS interference suppression



Interference Representation

■ Time-frequency domain

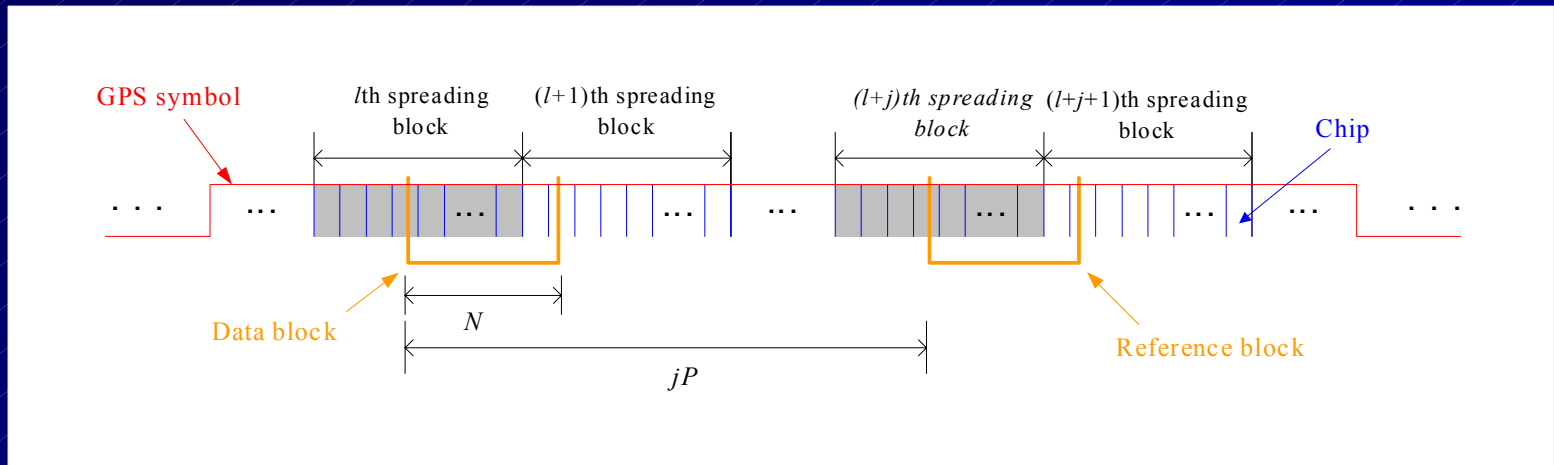


INTERFERENCE SUPPRESSION IN GPS (Cont'd)

- Spread-spectrum (SS) provides certain protections against interference
 - Receiver fails when the interference to signal ratio exceeds the 30 dB.
- Interference suppression
 - Separate domain: time, space, or frequency
 - Joint domain: time-frequency or space-time
- **None** of these methods fully utilizes the **repetitive** feature of the GPS C/A-code.

GPS SIGNAL STRUCTURE

Noise-free GPS data structure



- Two blocks of data (N consecutive samples each)
 - Data block
 - Reference block: jP samples apart from data block

The NOTION OF SELF-COHERENCE

■ Self-coherent signal

The **correlation** between the signal and its frequency-shifted version is **nonzero** for some time lag.

■ Significance of self-coherence

- **Blindly** extract the desired signals in the presence of **unknown** noise and interference.
- SCORE algorithm

SELF-COHERENCE (Cont'd)

- Example:

$$x(t) = as(t) + v(t)$$

- $s(t)$: self-coherent signal [not $v(t)$]

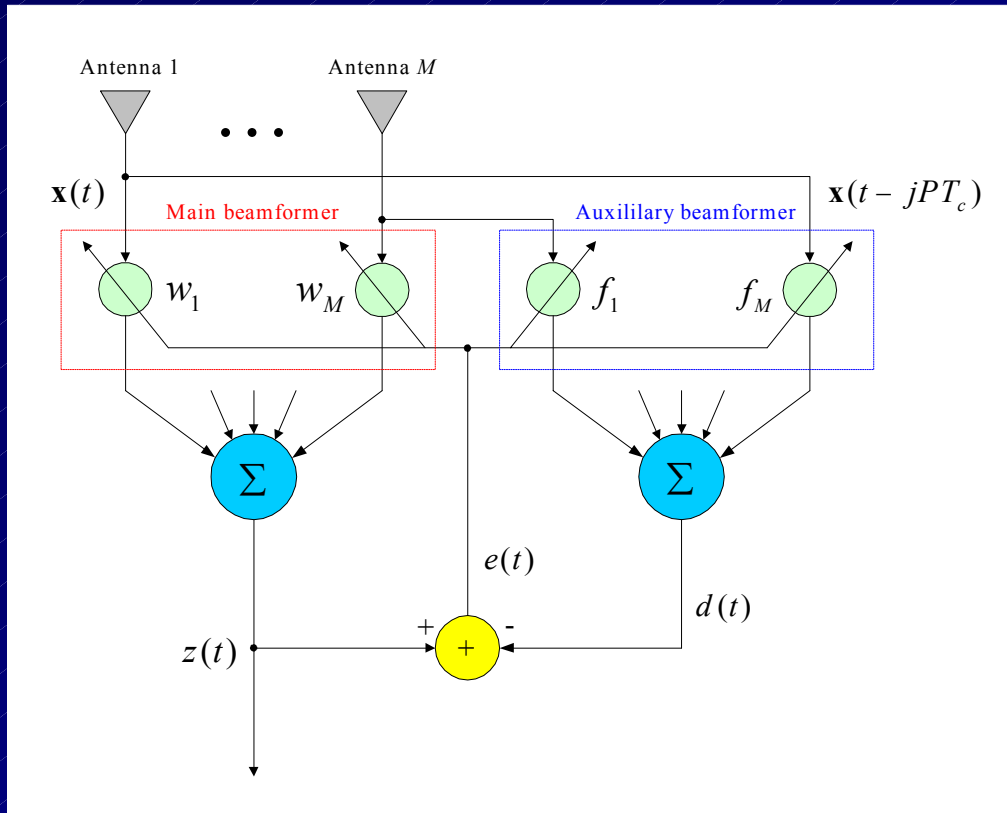
Cyclic autocorrelation of $x(t)$

$$R_{xx}^{(\beta)}(\tau) = |a|^2 R_{ss}^{(\beta)}(\tau) + R_{vv}^{(\beta)}(\tau) = |a|^2 R_{ss}^{(\beta)}(\tau)$$

- Frequency shift completely **decorrelates** the interference component in $x(t)$.

SELF-COHERENCE GPS RECEIVER

Receiver structure



- M -antenna array
- Two beamformers
 - w : generates **output** signal
 - f : generates **reference** signal

SELF-COHERENCE GPS RECEIVER (Cont'd)

- Assumptions:
 - Data block and reference blocks are within the same navigation symbol.
 - Interference does not have the same periodic structure as that of the GPS C/A signals.
- The proposed receiver acts like a pre-processor to suppress interference of all satellites.
 - Conventional multipath mitigation techniques, such as delay lock loop (DLL), can then operate on significantly higher SINR than that encountered at the receiver input.

RECEIVED SIGNAL

- Received signal at the chip-rate in the **data** block

$$\mathbf{x}(n) = \sum_{q=0}^Q s_q(n - \tau_q) \mathbf{a}_q e^{j\phi_q} + u(n)\mathbf{d} + \mathbf{v}(n)$$

– $S_0(n)$ is direct-path signal

- If the GPS signal, interference, and noise are **independent**

$$\mathbf{R}_{xx} = E \left\{ \mathbf{x}(n) \mathbf{x}^H(n) \right\} = \mathbf{R}_s + \mathbf{R}_u + \mathbf{R}_v$$

RECEIVED SIGNAL (Cont'd)

- The samples of GPS signal in the reference block have the **same** values as the corresponding samples in the data block within the **same** symbol

$$\mathbf{x}(n) = \mathbf{x}(n - jP), \quad 1 \leq j < 20$$

- If the GPS signals are the only data components that are correlated when delayed jP samples

$$\mathbf{R}_{xx}^{(P)} = E \left\{ \mathbf{x}(n) \mathbf{x}^H(n - jP) \right\} = \mathbf{R}_s$$

PROPOSED RECEIVER

- Cost function – SCORE algorithm

$$C(\mathbf{w}, \mathbf{f}) = \frac{|R_{zd}|^2}{R_{zz}R_{dd}} = \frac{|\mathbf{w}^H \mathbf{R}_{xx}^{(P)} \mathbf{f}|}{\left[\mathbf{w}^H \mathbf{R}_{xx} \mathbf{w} \right] \left[\mathbf{f}^H \mathbf{R}_{xx} \mathbf{f} \right]}$$

\mathbf{w} is obtained by **maximizing** $C(\mathbf{w}, \mathbf{f})$

- Beamformer output: $z(n) = \mathbf{w}^H \mathbf{x}(n)$
- Reference signal: $d(n) = \mathbf{f}^H \mathbf{x}(n - jP)$
- Cross-correlation between $z(n)$ and $d(n)$:

$$R_{zd} = E \left\{ z(n) d^H(n) \right\}$$

PROPOSED RECEIVER (Cont'd)

- Error signal

$$e(n) = z(n) - d(n)$$

Least-squares solution of \mathbf{f}

$$\mathbf{f}_{LS} = \mathbf{R}_{xx}^{-1} \mathbf{R}_{xx}^{(P)H} \mathbf{w}$$

- The weight vector \mathbf{w} that maximizes the cost function is the eigenvector corresponding to the **largest** eigenvalue of the generalized eigenvalue problem

$$\mathbf{R}_{xx} \mathbf{w} = \lambda_{\max} \mathbf{R}_{xx}^{(P)} \mathbf{R}_{xx}^{-1} \mathbf{R}_{xx}^{(P)} \mathbf{w}$$

Exact Expression

■ Define events

$A_1 : x(n) \text{ \& } x(n - jP) \text{ are within the same symbol,}$

$A_{21} : x(n) \text{ \& } x(n - jP) \text{ are in two symbols}$

with the same sign,

$A_{22} : x(n) \text{ \& } x(n - jP) \text{ are in two symbols}$

with different signs

■ The corresponding probabilities are

$$\Pr \{A_1\} = 1 - \frac{jP}{20P}$$

$$\Pr \{A_{21}\} = \Pr \{A_{22}\} = \frac{jP}{40P}$$

Continue

$$\begin{aligned}\mathbf{R}_{xx}^{(P)} &= E \left\{ \mathbf{x}(n) \mathbf{x}^H(n - jP) \middle| A_1 \right\} \Pr \{ A_1 \} \\ &\quad + E \left\{ \mathbf{x}(n) \mathbf{x}^H(n - jP) \middle| A_{21} \right\} \Pr \{ A_{21} \} \\ &\quad + E \left\{ \mathbf{x}(n) \mathbf{x}^H(n - jP) \middle| A_{21} \right\} \Pr \{ A_{21} \} \\ &= \left(1 - \frac{jP}{20P} \right) \mathbf{R}_s\end{aligned}$$

MODIFIED CROSS-SCORE RECEIVER (Cont'd)

- The cross-SCORE based receiver does not have the ability to mitigate multipath.
- Since multipath often comes from near the horizon while the GPS satellites are located above the horizon, adding constraints to the previous receiver can **mitigate multipath** entering the receiver from **near the horizon**.

MODIFIED CROSS-SCORE RECEIVER (Cont'd)

- Define the matrix containing steering vectors associated equally spaced directions covering **solid angle** Ω near the horizon

$$\mathbf{B} = [\mathbf{b}(\gamma_1) \quad \cdots \quad \mathbf{b}(\gamma_D)]$$

- The modified cost function on \mathbf{f}

$$\mathbf{f}_{\text{opt}} = \arg \max_{\mathbf{f}} \frac{\mathbf{f}^H \tilde{\mathbf{R}}_{xx} \mathbf{f}}{\mathbf{f}^H \mathbf{R}_{xx} \mathbf{f}}, \text{ subject to } \mathbf{B}^H \mathbf{f} = \mathbf{0}$$

$$\tilde{\mathbf{R}}_{xx} = \mathbf{R}_{xx}^{(P)} \mathbf{R}_{xx}^{-1} \mathbf{R}_{xx}^{(P)H}$$

MODIFIED CROSS-SCORE RECEIVER (Cont'd)

- Let \mathbf{A} be the matrix that **spans the null space** of \mathbf{B} such that $\mathbf{B}^H \mathbf{A} = \mathbf{0}$.
- Let α be a vector such that $\mathbf{f} = \mathbf{A}\alpha$.
- Using the vector α , the constrained maximization problem can be transformed into the unconstrained maximization problem as

$$\alpha = \arg \max_{\alpha} \frac{\alpha^H \mathbf{A}^H \tilde{\mathbf{R}}_{xx} \mathbf{A} \alpha}{\alpha^H \mathbf{A}^H \mathbf{R}_{xx} \mathbf{A} \alpha}$$

MODIFIED CROSS-SCORE RECEIVER (Cont'd)

- Solving the above **unconstrained** generalized eigenvalue problem lead to α which is given by the eigenvector associated with the largest eigenvalue. The beamformer \mathbf{f}_{opt} be obtained correspondingly.
- The beamformer \mathbf{w}_{opt} is then given by

$$\mathbf{w}_{\text{opt}} = \mathbf{R}_{xx}^{-1} \mathbf{R}_{xx}^{(P)} \mathbf{f}_{\text{opt}} = \mathbf{R}_{xx}^{-1} \mathbf{R}_{xx}^{(P)} \mathbf{A} \alpha$$

IMPLEMENTATION ISSUES

- **Sample estimates** have to be used instead of the exact ones

$$\hat{\mathbf{R}}_{xx} = \frac{1}{N} \mathbf{X}_N \mathbf{X}_N^H, \quad \hat{\mathbf{R}}_{xx}^{(P)} = \frac{1}{N} \mathbf{X}_N \mathbf{X}_{N\text{ref}}^H$$

- Data sample matrix

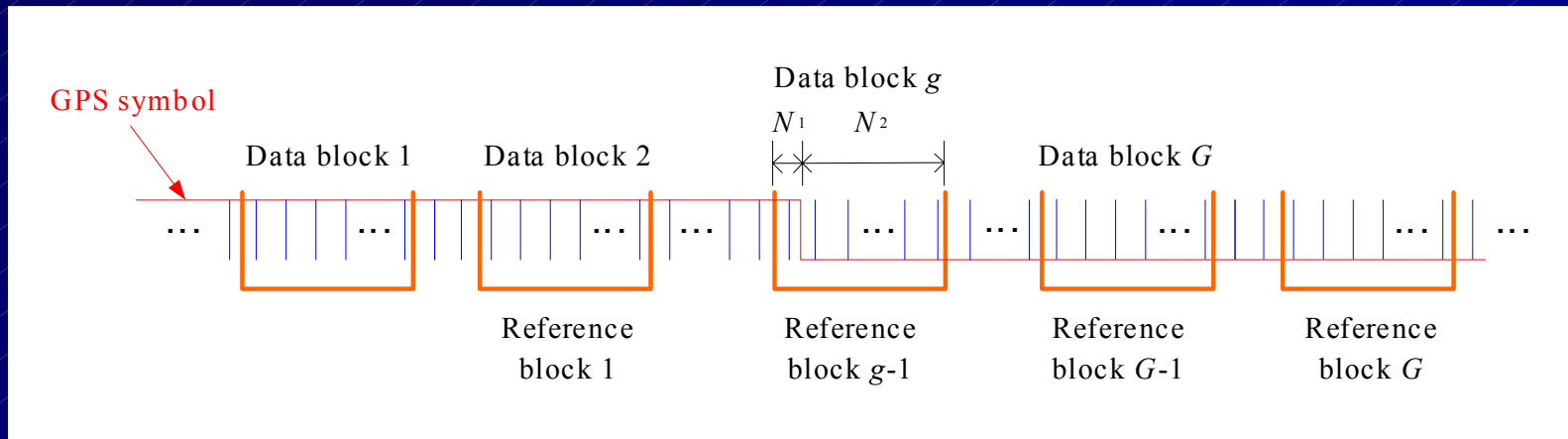
$$\mathbf{X}_N = [\mathbf{x}(n), \quad \dots, \quad \mathbf{x}(n - (N - 1))]$$

- Reference sample matrix

$$\mathbf{X}_{N\text{ref}} = [\mathbf{x}(n - jP), \quad \dots, \quad \mathbf{x}(n - (N - 1) - jP)]$$

IMPLEMENTATION ISSUES (Cont'd)

- **Multiple** data and reference blocks can be used to improve the time-averaging:



$$\hat{\mathbf{R}}_{xx} = \frac{1}{G} \sum_{g=1}^G \mathbf{X}_N(g) \mathbf{X}_N^H(g) / N$$

$$\hat{\mathbf{R}}_{xx}^{(P)} = \frac{1}{G} \sum_{g=1}^G \mathbf{X}_N(g) \mathbf{X}_{N_{\text{ref}}}^H(g) / N$$

COVARIANCE ESTIMATION (Cont'd)

■ The expected values of estimates

$$\overline{\hat{\mathbf{R}}_{xx}^{(P)}} = \left(1 - \frac{jP}{20P}\right) \mathbf{R}_s, \text{ one block estimation}$$

$$\overline{\hat{\mathbf{R}}_{xxG}^{(P)}} = \left(1 - \frac{jP}{20P}\right) \mathbf{R}_s, G \text{ blocks estimation}$$

■ The corresponding variances of estimates

$$\text{var} \left\{ \hat{\mathbf{R}}_{xx}^{(P)} \right\} = \frac{M(N + \sigma_v^2)}{N} \mathbf{R}_s + \frac{M(1 + \sigma_v^2)}{N} \mathbf{R}_v - \left(\overline{\hat{\mathbf{R}}_{xx}^{(P)}} \right)^2$$

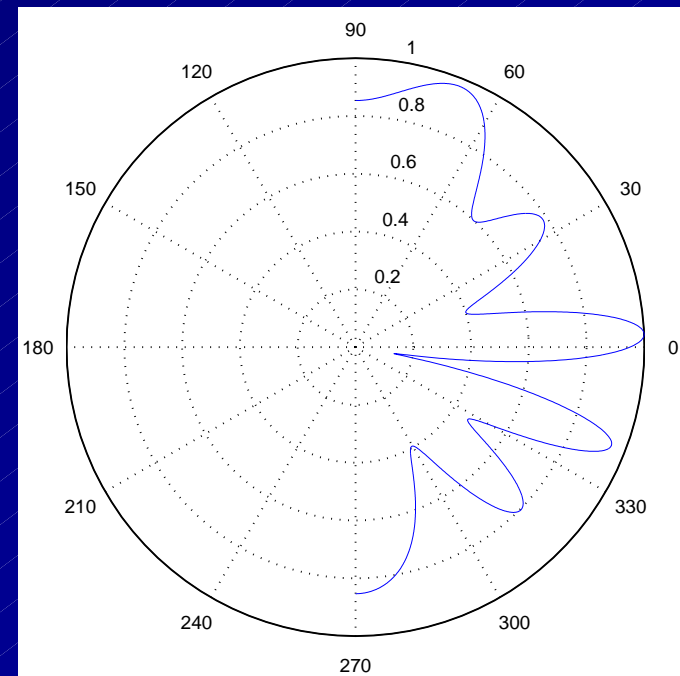
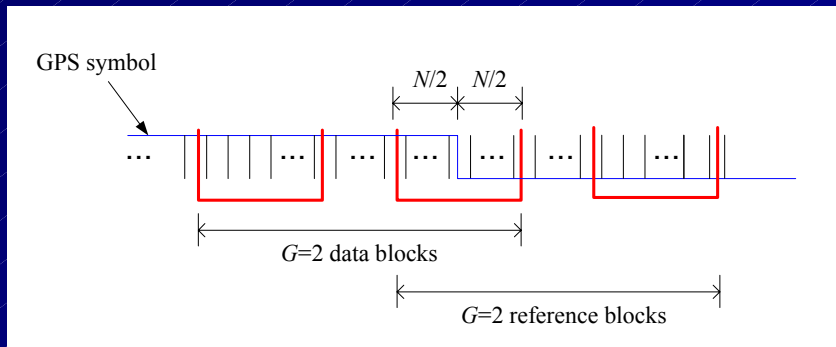
$$\text{var} \left\{ \hat{\mathbf{R}}_{xxG}^{(P)} \right\} = \left(1 - 2 \frac{jP}{20P} + 2 \frac{jP}{20GP}\right) \left[\frac{M(N + \sigma_v^2)}{N} \mathbf{R}_s + \frac{M(1 + \sigma_v^2)}{N} \mathbf{R}_v \right] - \left(\overline{\hat{\mathbf{R}}_{xxG}^{(P)}} \right)^2$$

SIMULATION RESULTS

- Linear uniform array with $M=7$ sensors.
- GPS navigation symbols in **BPSK** format; C/A-code with processing gain of $P=1023$.
- $N=800$ samples in both the data and reference blocks.
- Jammers are generated as broadband binary signals with the same rate as the C/A-code.
- Multipath signal power is one-fifth of the direct-path signal power.

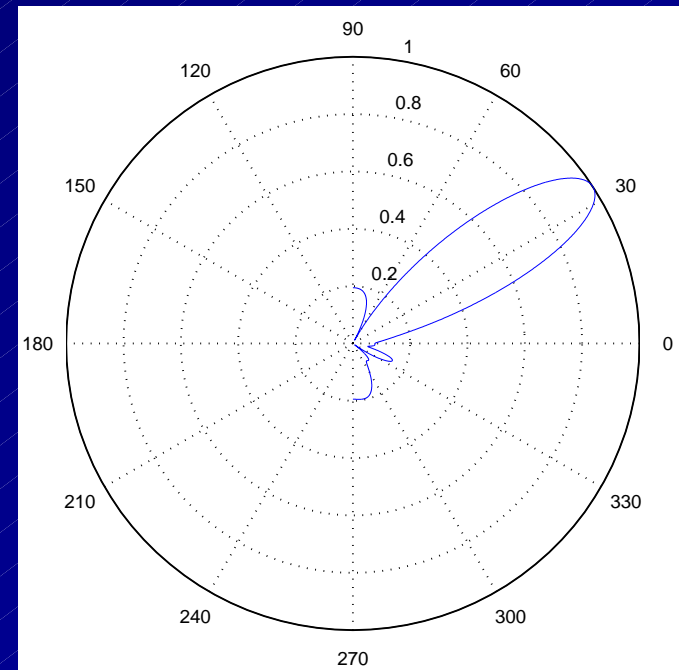
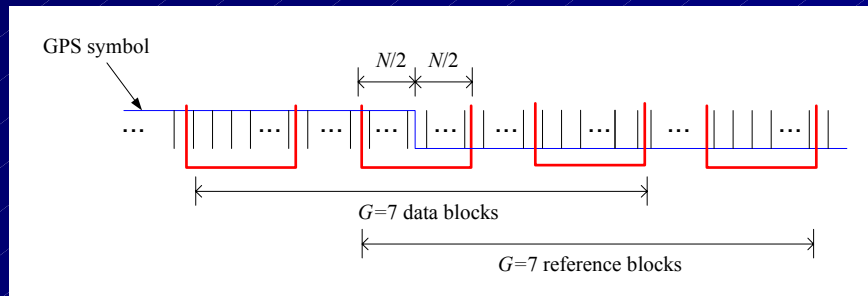
Critical Case

- Beam pattern without interference – **evenly** split data block ($G=2$, $\text{SNR}=-30$ dB)



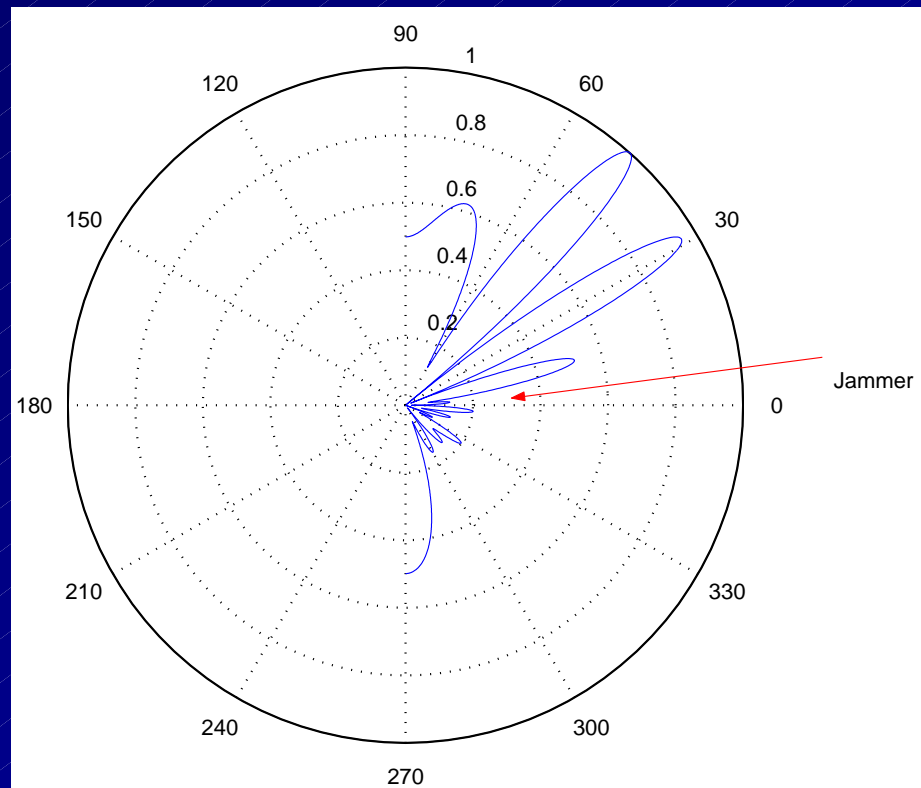
IMPROVED!

- Beam pattern without interference ($G=7$, $\text{SNR}=-30$ dB)



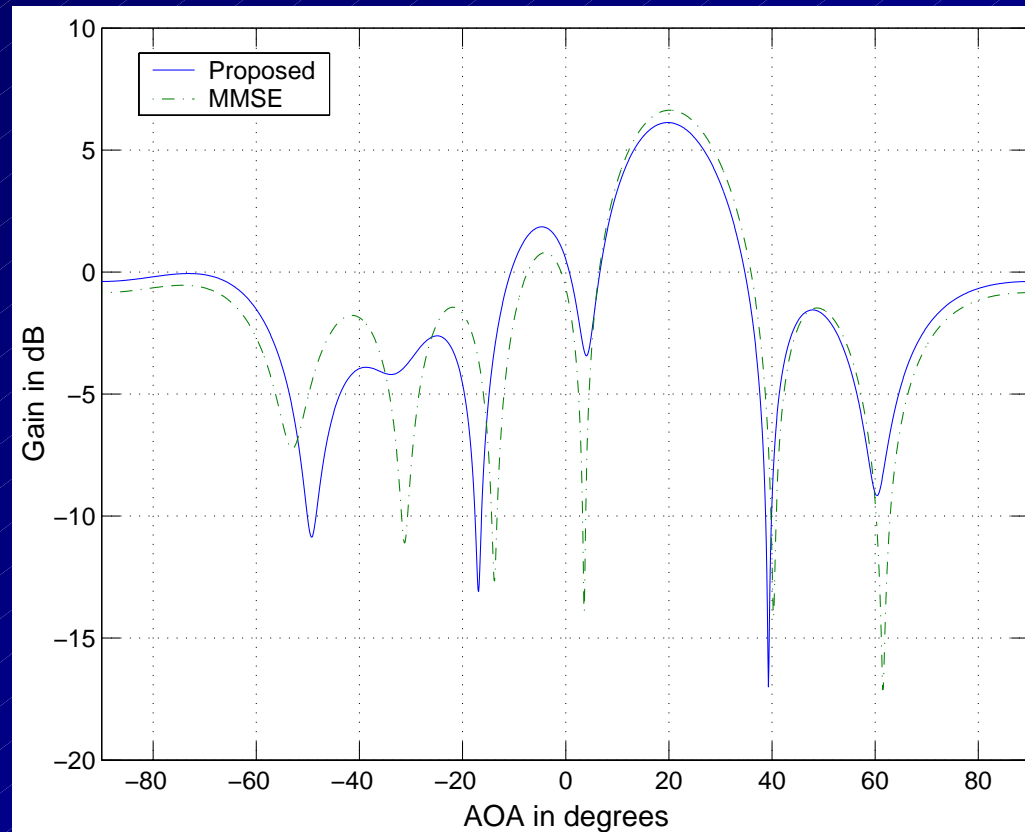
FOR ALL SATELLITES

- With multiple satellites in the field of view ($M=9$, $\text{SNR}=-30$ dB)



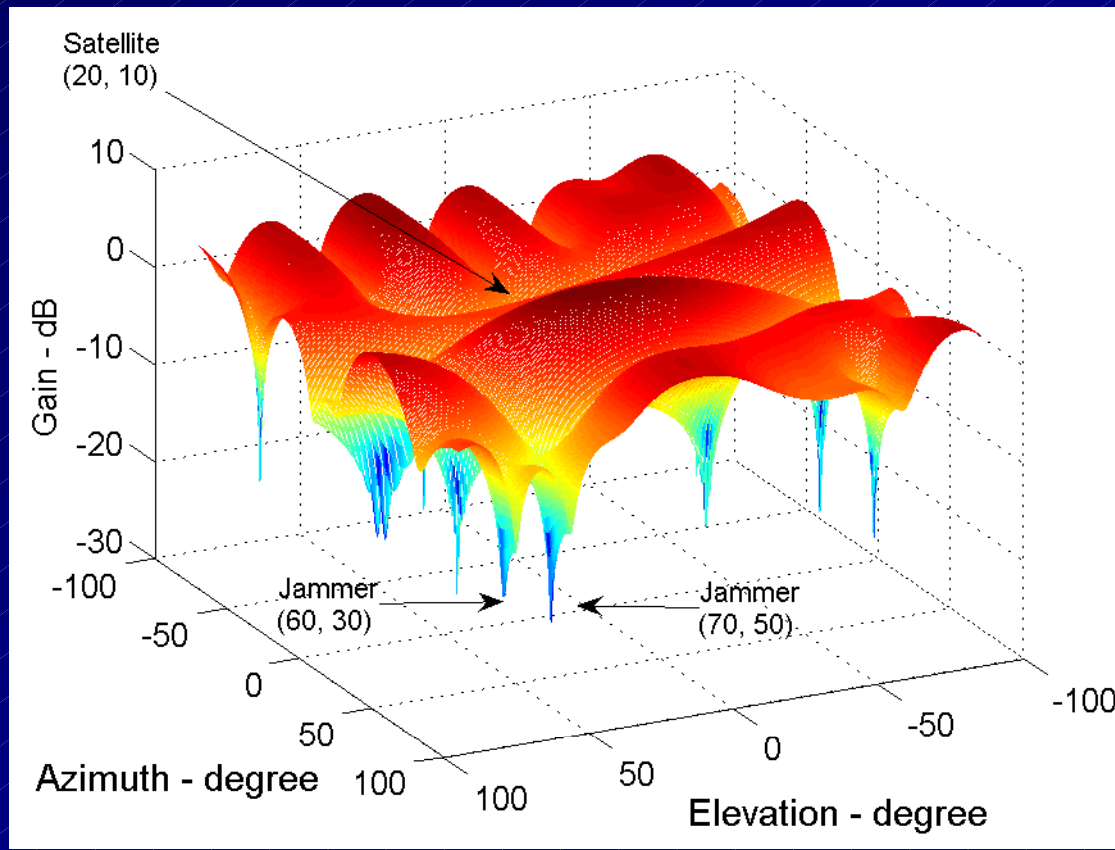
SIMULATION RESULTS (Cont'd)

- Comparison with MMSE method (spatial processing only) (SINR=-33 dB, JSR=30 dB)



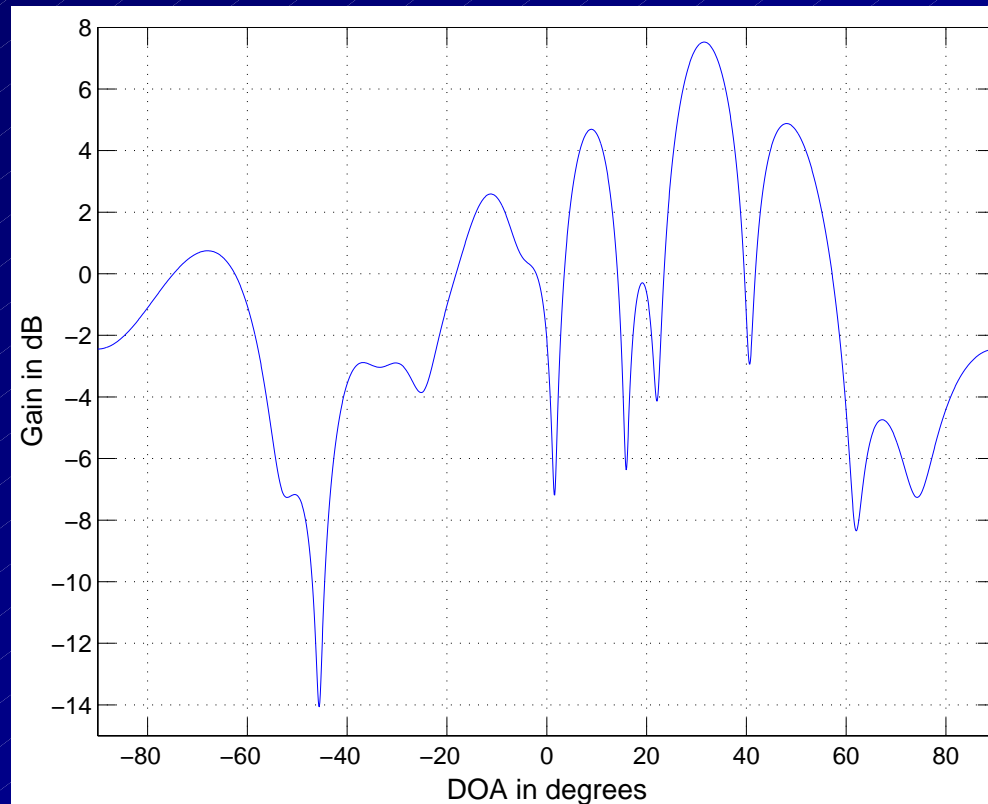
Performance

- Circular array: $M=7$ sensors, SNR=-30 dB and JSR=30 dB.



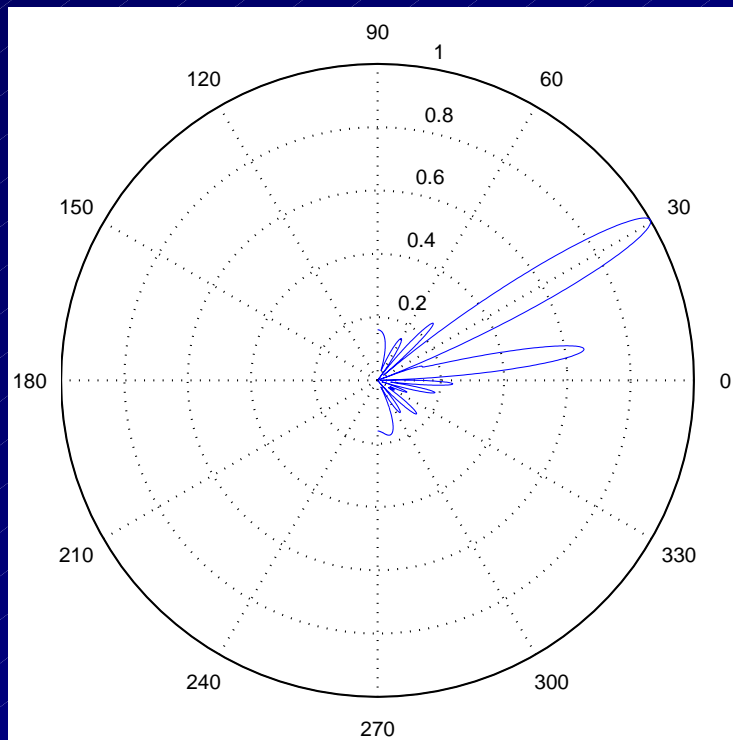
Jammers with Similar Coherence

- Jammers with the same structure as the GPS signals (satellite at 30 degree and two jammers at 10 and 50 degree)

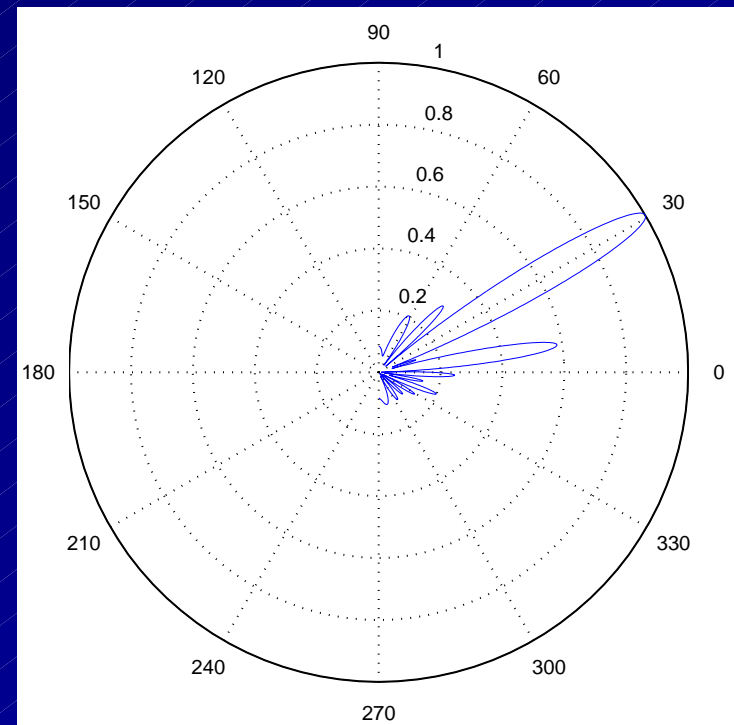


MULTIPATH!

- In the presence of multipath (satellite at 30 degree, one multipath at 8 degrees)



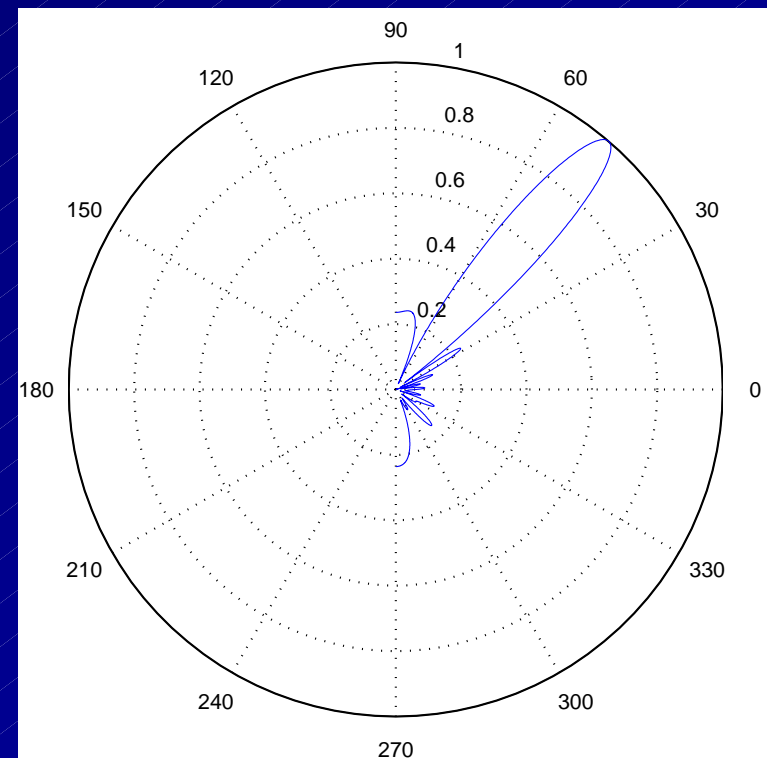
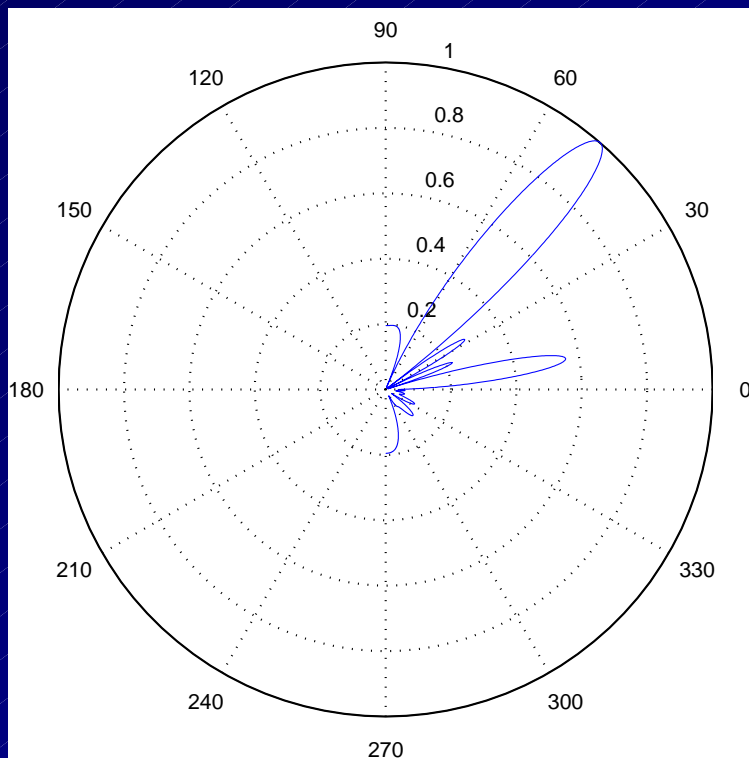
1-chip delay

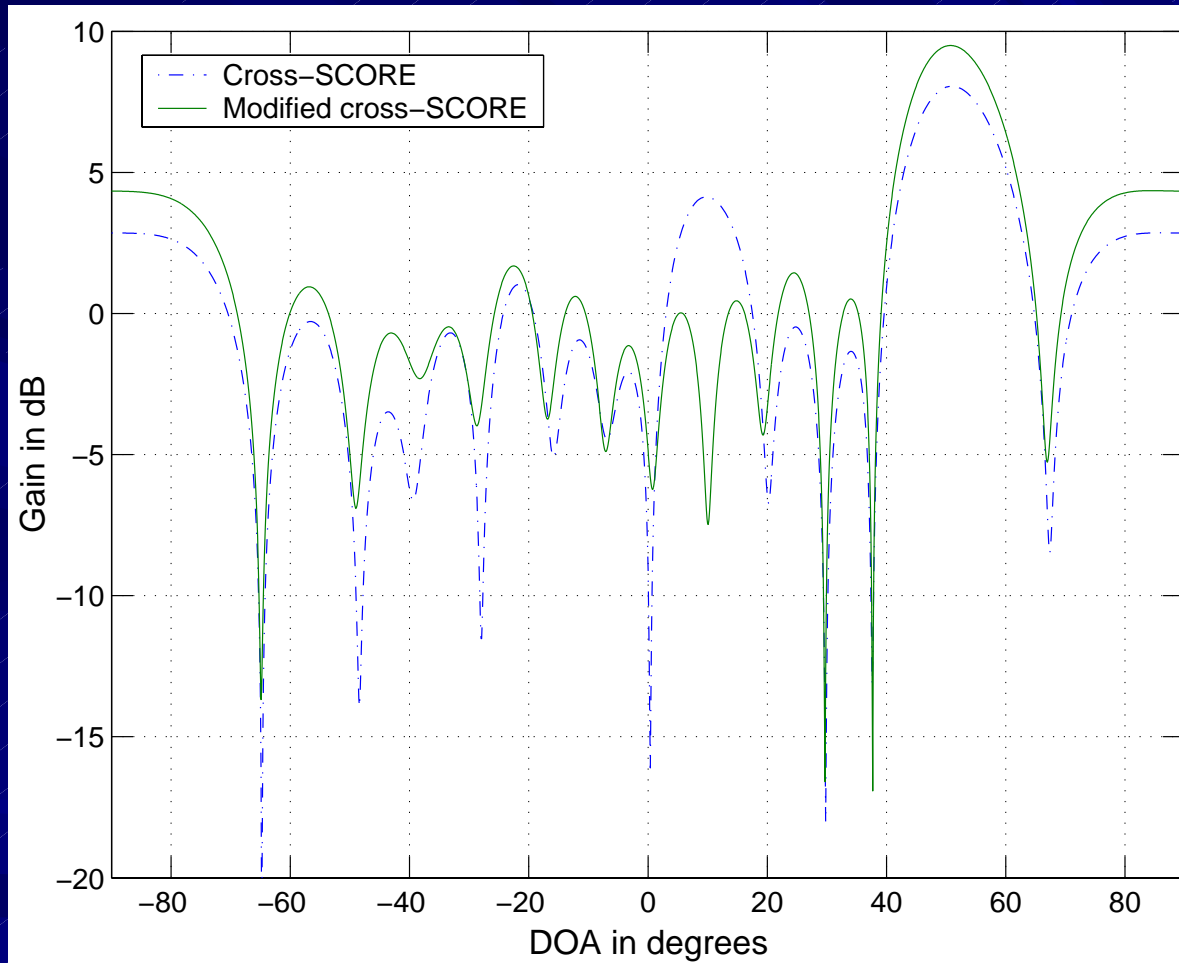


5-chip delay

SIMULATION RESULTS (Cont'd)

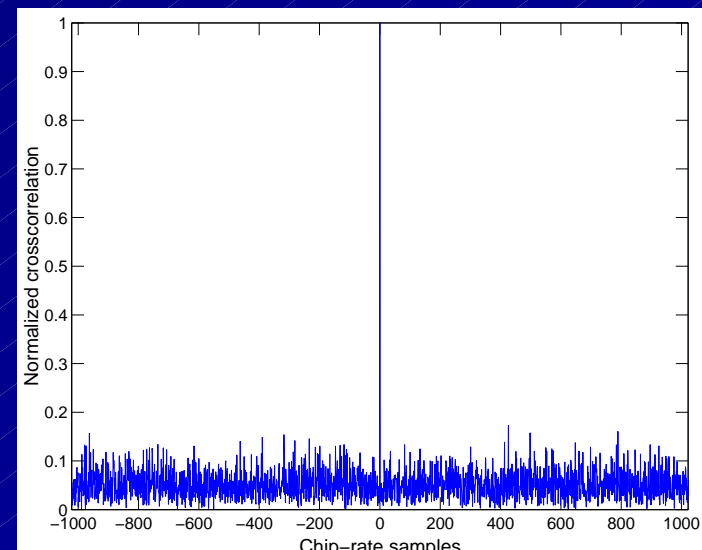
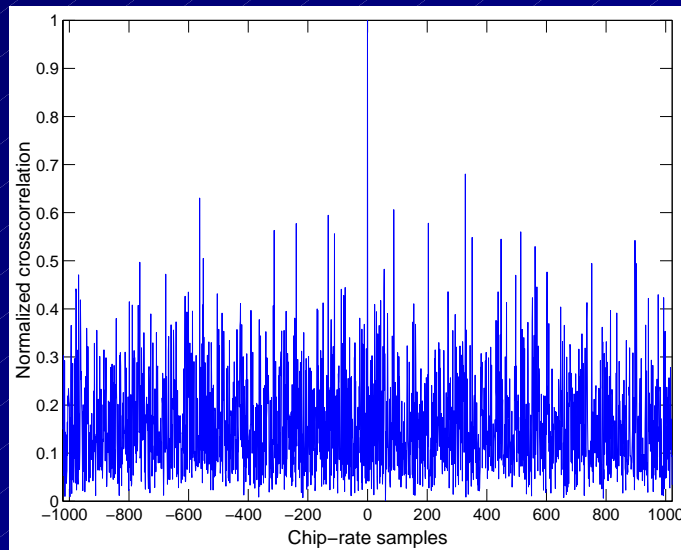
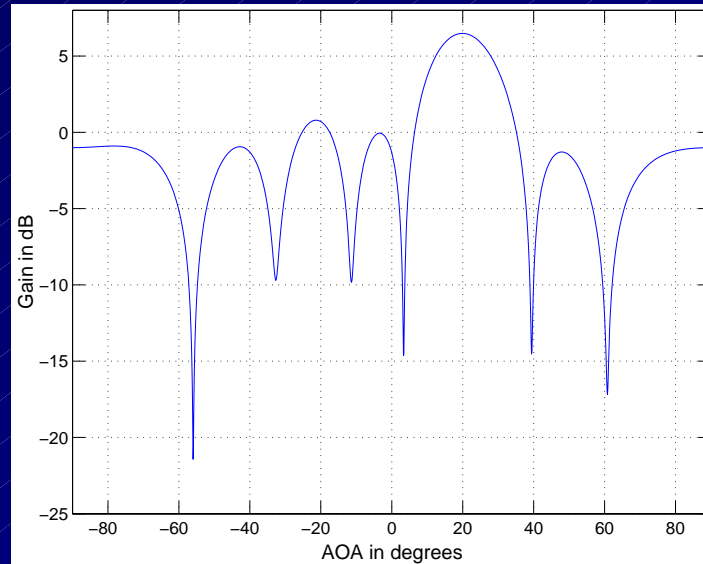
- Comparison between the original and modified approaches in the presence of multipath (10 degree, SNR = -30 dB, 1/5 power)





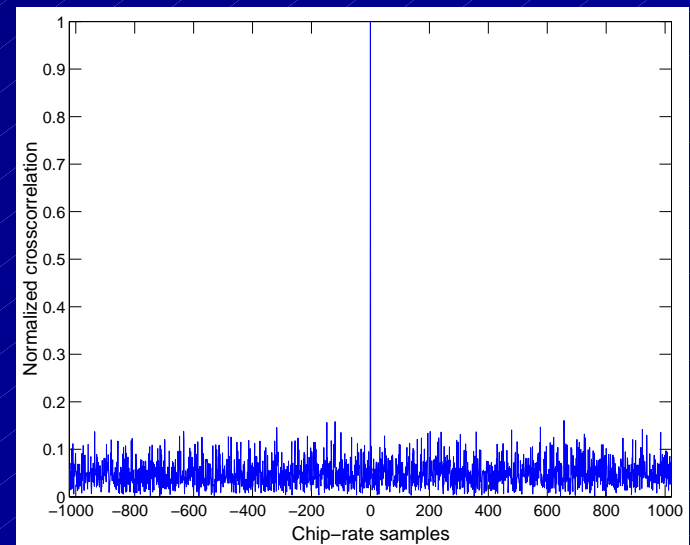
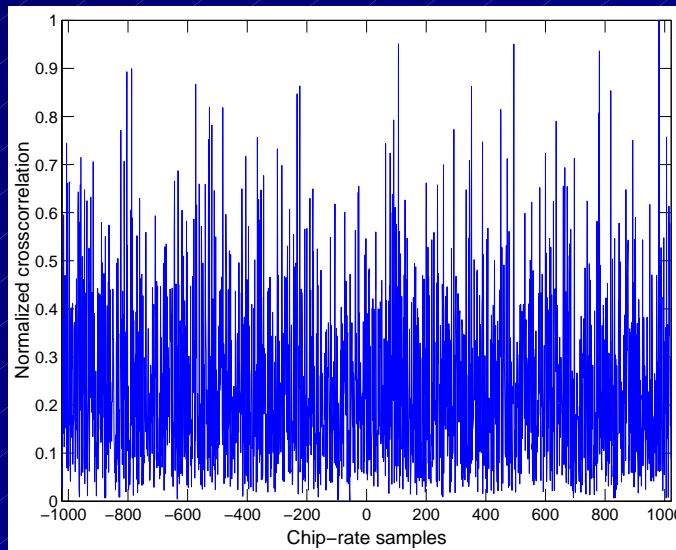
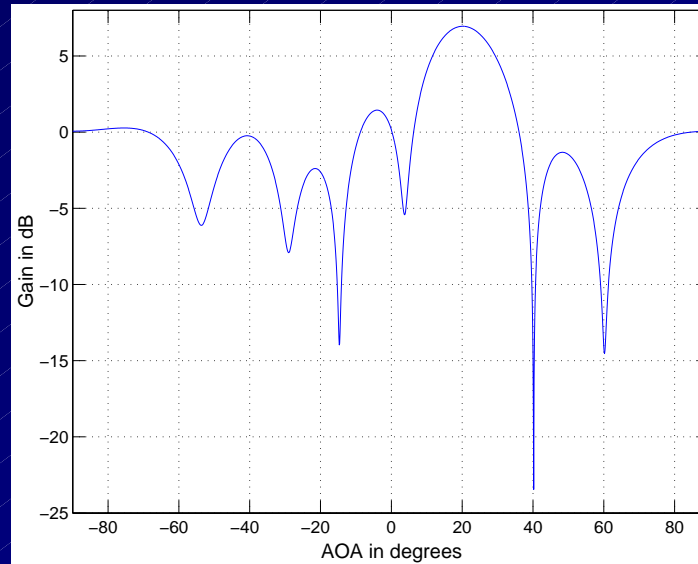
SIMULATION RESULTS (Cont'd)

- Synchronization (SNR=-25 dB, JSR=30 dB)



SIMULATION RESULTS (Cont'd)

- Synchronization (SNR=-25 dB, JSR=50 dB)



CONCLUSIONS

- Presented a novel self-coherence based GPS anti-jam receiver.
- The receiver utilizes the inherent self-coherence feature of the GPS C/A signal.
- The proposed receiver requires neither the knowledge of the transmitted GPS signal nor the location of the satellite.
- The proposed receiver is able to suppress a large class of interference as long as the interferers do not have the same periodic structure as the C/A signal.

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