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**Avoid Design Problems Using Worst Case
Analysis Calculations**

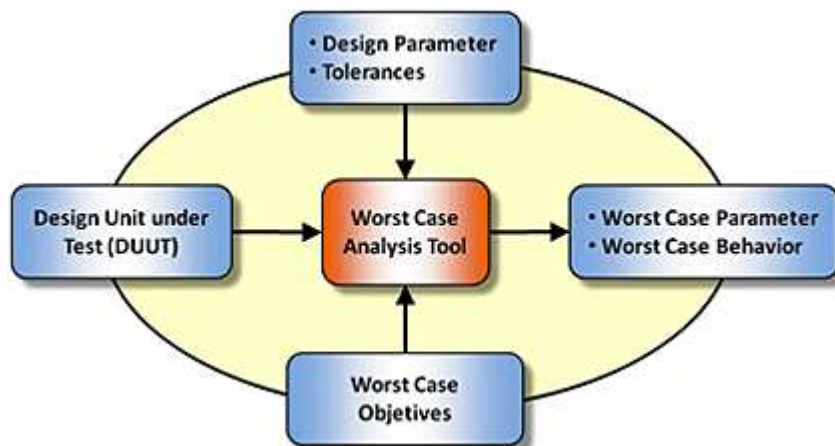
2nd Edition

Agenda

- Discussion on what is worst case analysis
- Different types of worst case analysis – i.e.: Extreme value, RSS
- Discussion on electronic component tolerances – resistors, capacitors, and Inductors, with an inductor saturation example.
- Example 1: Output voltage regulation. Reference and IC tolerance included.
- Example 2: Feedback loop stability WCA.
- Example 3: MOSFET Power dissipation. FET and Diode tolerances included.

Worst Case Analysis Definition

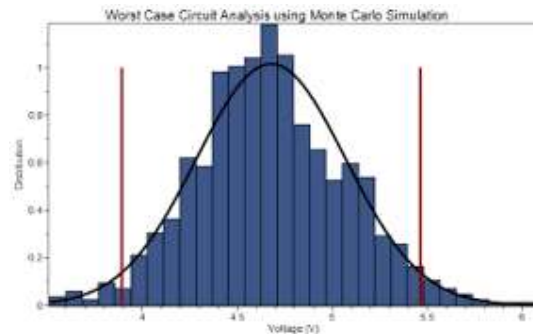
- A worst-case analysis is an assessment of a circuit's functional performance, accounting for tolerances, such as **Beginning of life (BOL)**, environmental (**Temperature**), aging **End of Life (EOL)**, and, in the case of Space applications, radiation tolerances.



Worst Case Analysis Method Types

- **Extreme Value Analysis (EVA)** This is an estimate of the most extreme limits of the circuit's components and function.
- **Root Sum Square (RSS)** method works on a statistical approach. It assumes that most of the components fall to the mid of the tolerance zone rather than at the extreme ends.
- **Monte Carlo analysis**, in which parameters are randomly selected from a distribution, and the circuit simulated, anywhere from 1000 to 100000 times.

$$\Delta Y = \sqrt{\sum_{i=1}^n \delta_i^2}$$



Worst Case Analysis component Tolerances

Resistor Tolerances

EOL obtained from component manufacturer,
or engineering APL

$\text{delT} := 75$

$\text{tol_rd1_bol} := 0.1\%$	$\text{tol_rd1_eol} := 0.5\%$	$\text{tol_rd1_temp} := 25 \cdot 10^{-6} \cdot \text{delT}$	ppm /C
$\text{tol_rd2_bol} := 1\%$	$\text{tol_rd2_eol} := 0.5\%$	$\text{tol_rd2_temp} := 100 \cdot 10^{-6} \cdot \text{delT}$	ppm /C
$\text{tol_rd3_bol} := 1\%$	$\text{tol_rd3_eol} := 0.5\%$	$\text{tol_rd3_temp} := 250 \cdot 10^{-6} \cdot \text{delT}$	ppm /C
$\text{tol_rd4_bol} := 10\%$	$\text{tol_rd4_eol} := 0.5\%$	$\text{tol_rd4_temp} := 2000 \cdot 10^{-6} \cdot \text{delT}$	ppm /C

Variations

$$k1 := (\text{tol_rd1_bol} + \text{tol_rd1_eol} + \text{tol_rd1_temp}) \quad k1 = 7.875 \cdot 10^{-3}$$

$$k2 := (\text{tol_rd2_bol} + \text{tol_rd2_eol} + \text{tol_rd2_temp}) \quad k2 = 0.023$$

$$\text{xr23} := 53.6 \cdot k$$

$$\text{xr23min} := \text{xr23} \cdot (1 - k1)$$

$$\text{xr23max} := \text{xr23} \cdot (1 + k1)$$

$$\text{xr23min} = 5.318 \cdot 10^4$$

$$\text{xr23max} = 5.402 \cdot 10^4$$

Worst Case Analysis component Tolerances

Capacitor Tolerances

EOL obtained from component manufacturer,
or engineering APL

$$\text{delT} := 75$$

$$\text{tol_npo_bol} := 5\%$$

$$\text{tol_npo_eol} := 0.5\%$$

$$\text{tol_npo_temp} := 30 \cdot 10^{-6} \cdot \text{delT}$$

$$\text{tol_bx_bol} := 10\%$$

$$\text{tol_bx_eol} := 21\%$$

$$\text{tol_bx_temp} := 15\%$$

$$\text{tol_x7r_bol} := 10\%$$

$$\text{tol_x7r_eol} := 21\%$$

$$\text{tol_x7r_temp} := 15\%$$

BX characteristics are identical to X7R dielectric, with the added restriction that the Temperature-Voltage Coefficient (TVC) is not to exceed -25% ΔC at rated voltage, over the operating temperature range (-55°C to 125°C).

Variations

$$k3 := (\text{tol_npo_bol} + \text{tol_npo_eol} + \text{tol_npo_temp})$$

$$k3 = 0.057$$

$$k4 := (\text{tol_bx_bol} + \text{tol_bx_eol} + \text{tol_bx_temp})$$

$$k4 = 0.46$$

$$k5 := (\text{tol_x7r_bol} + \text{tol_x7r_eol} + \text{tol_x7r_temp})$$

$$k5 = 0.46$$

$$a1c12 := 39 \cdot p$$

$$a1c12_{\min} := a1c12 \cdot (1 - k3)$$

$$a1c12_{\max} := a1c12 \cdot (1 + k3)$$

$$a1c12_{\min} = 3.833 \cdot 10^{-11}$$
$$a1c12_{\max} = 3.967 \cdot 10^{-11}$$

Worst Case Analysis component Tolerances

Inductor Tolerances

5. DC current at 25°C that causes an inductance drop of 30% (typ) from its value without current.

Part number ¹	Inductance ² ±20% (μH)	DCR (mOhms) ³		SRF typ ⁴ (MHz)	Isat ⁵ (A)	Irms (A) ⁶	
		typ	max			20°C rise	40°C rise
XAL7030-161ME	0.16	1.15	1.26	158	60.0	24.9	32.5
XAL7030-301ME	0.30	1.75	1.92	101	41.0	21.0	27.6
XAL7030-601ME	0.60	3.00	3.30	72	36.0	18.0	23.0
XAL7030-102ME	1.0	4.55	5.00	52	28.0	16.1	21.8
XAL7030-152ME	1.5	7.60	8.36	39	23.5	11.9	15.0
XAL7030-222ME	2.2	13.7	15.07	29	18.0	10.0	12.9
XAL7030-272ME	2.7	15.7	17.30	32	12.8	9.2	11.4
XAL7030-332ME	3.3	19.5	21.45	25	12.3	8.0	10.0
XAL7030-472ME	4.7	26.1	30.00	21	10.1	6.9	9.0
XAL7030-562ME	5.6	28.1	32.32	17	9.8	5.3	7.3
XAL7030-682ME	6.8	45.0	51.75	15	8.7	4.4	6.8
XAL7030-822ME	8.2	53.0	60.94	13	8.4	2.9	5.9
XAL7030-103ME	10	60.4	69.46	12	7.7	2.6	5.3

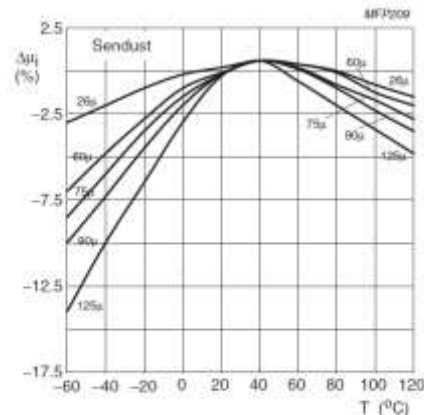
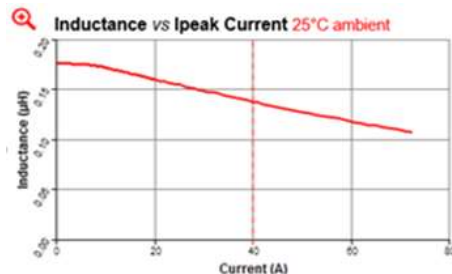
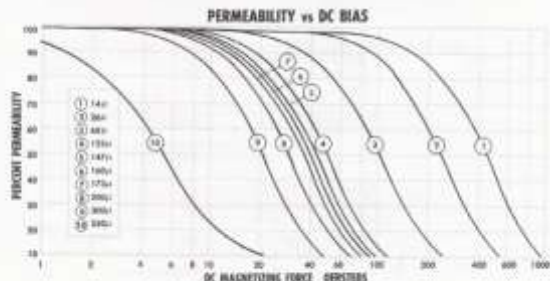


Fig.2 Initial permeability as a function of temperature.



$$L = \frac{4 \cdot 3.14 \cdot \mu \cdot \text{turns}^2 \cdot (A_e)}{l \cdot 10^8}$$

Where:

Linductance = Henry's

μ = core permeability

N = number of turns

Ae = core cross-section (mm²)

le = core magnetic path length (mm)

Worst Case Analysis Inductance rolloff example

Example of saturation current

$V_{in} = 12V$ $V_o = .9V$
 $V_{inmax} = 13.2V$ $I_{omax} = 40A$
 $V_{inmin} = 10.8V$ $I_{omin} = 4A$
 $f = 650kHz$

Now what happens if I push I_{omax} to 60A and reduce the inductance by 30%

$V_{in} = 12V$ $V_o = .9V$
 $V_{inmax} = 13.2V$ $I_{omax} = 60A$
 $V_{inmin} = 10.8V$ $I_{omin} = 4A$
 $f = 650kHz$

$L_{out} = 160nH$

$L_{out} = 112nH$

$I_{peak} = 45.6A$

Peak inductor current

$I_{peak} = 68.7A$

Peak inductor current

Rule of thumb derate I_{sat} by 30 to 40%

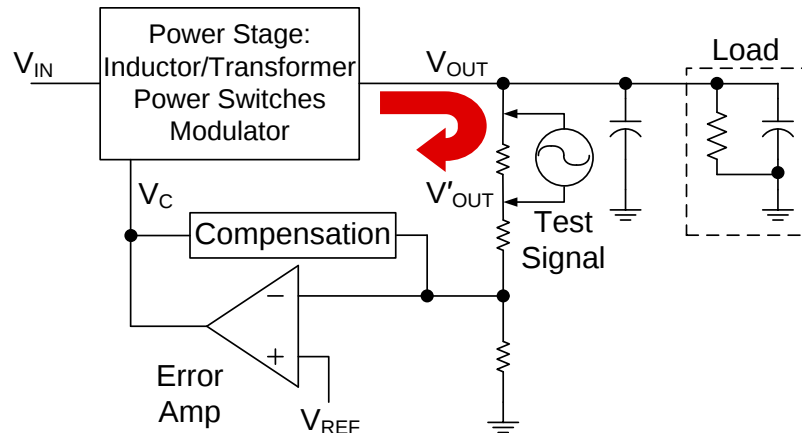
Worst Case Analysis Output regulation example

Problem statement

- What is my worst case output voltage regulation

Procedure

- Find tolerances for V_{ref} , error-amp, and resistor divider.
- Write equation for feedback regulation
- Calculate sensitivity of variables.
- Solve equation



Worst Case Analysis Output regulation example

Reference tolerance

$\text{tol_TL431_bol} := 0.5\%$ $\text{tol_TL431_eol} := .25\%$ $\text{tol_TL431_temp} := 60 \cdot 10^{-6} \cdot \text{delT}$

Reference Variation

$V_{\text{ref}} := 2.495$

$\text{TL431vrefmin} := V_{\text{ref}} \cdot (1 - \text{tol_TL431_bol}) \cdot (1 - \text{tol_TL431_eol}) \cdot (1 - \text{tol_TL431_temp})$

$\text{TL431vrefmin} = 2.465$

$\text{TL431vrefmax} := V_{\text{ref}} \cdot (1 + \text{tol_TL431_bol}) \cdot (1 + \text{tol_TL431_eol}) \cdot (1 + \text{tol_TL431_temp})$

$\text{TL431vrefmax} = 2.525$

- Reference Voltage Tolerance at 25°C
 - 0.5% (B Grade)
 - 1% (A Grade)
 - 2% (Standard Grade)

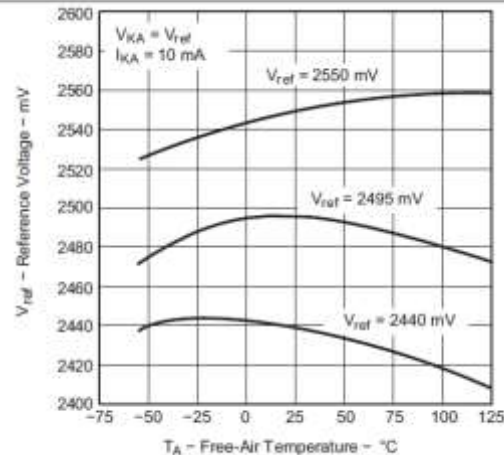


Figure 1. Reference Voltage vs Free-Air Temperature

Worst Case Analysis Output regulation example

Op-amp tolerance

Op-amp dc error sources include:

- Input offset voltage V_{OS}
- Input bias current I_B
- Input offset current I_{OS}
- Open loop gain

From LM158 Data sheet:

$V_{OS_bol} = 7\text{mV}$ from -55°C to 125°C

$V_{OS_temp} = 15\mu\text{V}/^\circ\text{C}$

$V_{OS_eol} =$ hard to find check with Manufacturer

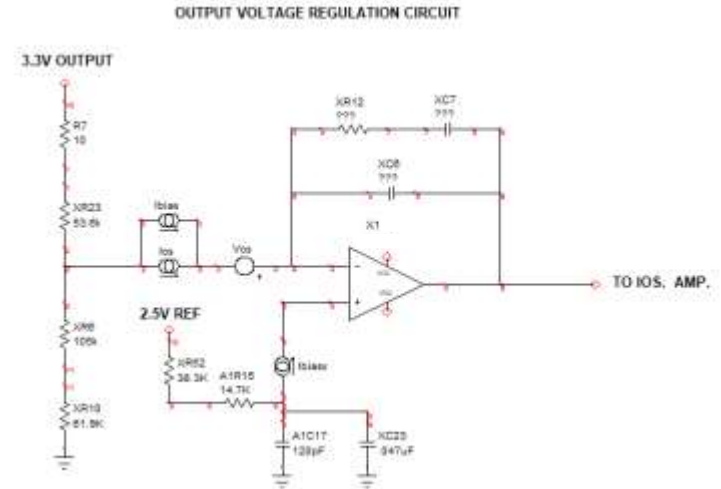
$I_{B_bol} = 300\text{nA}$ from -55°C to 125°C ,

$I_{OS_bol} = 100\text{nA}$ from -55°C to 125°C

$I_{OS_temp} = 200\text{pA}/^\circ\text{C}$, $I_{OS_eol} =$ hard to find check with Manufacturer

Open loop gain min = $35\text{V}/\text{mV} = 35000$

Open loop gain typ = $140\text{V}/\text{mV} = 140000$



Worst Case Analysis Output regulation example

Below is a sensitivity calculation to show which parts should be minimized or maximized

$$\text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) := \left(\begin{array}{l} \text{Vref} + \text{Vos} \dots \\ + \text{Vbiasnom} \dots \\ + \text{Vbias_gainnom} \end{array} \right) \cdot \frac{(\text{xr23} + \text{r7} + \text{xr10} + \text{xr6})}{\text{xr10} + \text{xr6}}$$

$$\frac{d}{d\text{Vref}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.321$$

$$\frac{d}{d\text{Vos}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.321$$

$$\frac{d}{d\text{Vbiasnom}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.321$$

$$\frac{d}{d\text{Vbias_gainnom}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.321$$

$$\frac{d}{d\text{xr23}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.504 \cdot 10^{-5}$$

$$\frac{d}{d\text{r7}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.504 \cdot 10^{-5}$$

$$\frac{d}{d\text{xr10}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = -4.83 \cdot 10^{-6}$$

$$\frac{d}{d\text{xr6}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = -4.83 \cdot 10^{-6}$$

Worst Case Analysis Output regulation example

Resistor divider tolerance

$$\text{Reqmax} := \frac{1}{\left(\frac{1}{\text{xr23max} + \text{r7max}} + \frac{1}{\text{xr10min} + \text{xr6min}} \right)}$$

$$\text{Reqmax} = 4.074 \cdot 10^4$$

$$\text{a1r15max} = 1.503 \cdot 10^4$$

$$\text{Reqmin} := \frac{1}{\left(\frac{1}{\text{xr23min} + \text{r7min}} + \frac{1}{\text{xr10max} + \text{xr6max}} \right)}$$

$$\text{Reqmin} = 4.041 \cdot 10^4$$

$$\text{a1r15min} = 1.437 \cdot 10^4$$

Worst Case Analysis Output regulation example

Voltage error due to the offset current, bias current, A1r15 and Req

$$V_{biasmin} := Req_{min} \cdot (I_{bias} - I_{os}) - I_{bias} \cdot (a1r15_{max} + xr52_{max}) \quad V_{biasmin} = -6.685 \cdot 10^{-4}$$

$$V_{biasmax} := Req_{max} \cdot (I_{bias} + I_{os}) - I_{bias} \cdot (a1r15_{min} + xr52_{min}) \quad V_{biasmax} = 1.748 \cdot 10^{-4}$$

$$V_{biasnom} := \frac{V_{biasmax} + V_{biasmin}}{2} \quad V_{biasnom} = -2.469 \cdot 10^{-4}$$

Voltage error due to the gain in the error amplifier

$$V_{out} = (V_{pos} - V_{neg}) \times A_v \quad V_{in} = V_{pos} - V_{neg} \quad V_{bias\ gain} = V_{in}$$

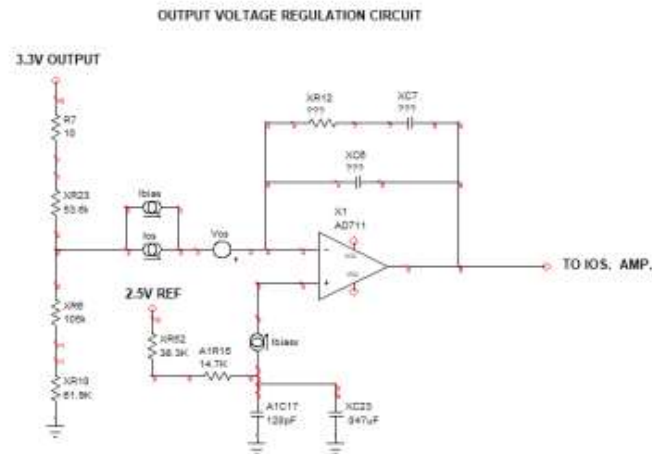
$v_{oh} := 5$ **Voh is the Vdd voltage on the error amp. therefore the maximum output voltage on the error amp.**

$$V_{bias_gainmax} := \frac{v_{oh}}{OLG_{min}} \quad V_{bias_gainmax} = 1.429 \cdot 10^{-4}$$

$$V_{bias_gainmin} := \frac{v_{oh}}{OLG_{max}} \quad V_{bias_gainmin} = 3.571 \cdot 10^{-5}$$

This is the min. and max. voltage required for op-amp operation

$$V_{bias_gainnom} := \frac{V_{bias_gainmax} + V_{bias_gainmin}}{2} \quad V_{bias_gainnom} = 8.929 \cdot 10^{-5}$$



Worst Case Analysis Output regulation example

The total output voltage error due to Vref, Vos, Vbias, Req, and A1r15

$$V_{\max} := (v_{\text{refmax}} + V_{\text{os}} + V_{\text{biasmax}} + V_{\text{bias_gainmax}}) \cdot \frac{(x_{\text{r23max}} + r_{\text{7max}} + x_{\text{r10min}} + x_{\text{r6min}})}{x_{\text{r10min}} + x_{\text{r6min}}} \quad V_{\max} = 3.37$$

$$V_{\min} := (v_{\text{refmin}} - V_{\text{os}} + V_{\text{biasmin}} + V_{\text{bias_gainmin}}) \cdot \frac{(x_{\text{r23min}} + r_{\text{7min}} + x_{\text{r10max}} + x_{\text{r6max}})}{x_{\text{r10max}} + x_{\text{r6max}}} \quad V_{\min} = 3.236$$

The percent delta for Vout is as follows

$$V_{\text{nom}} := 3.3$$

$$V_{\text{delta\%pos}} := \frac{V_{\max} - V_{\text{nom}}}{V_{\text{nom}}} \cdot 100$$

$$V_{\text{delta\%pos}} = 2.126$$

$$V_{\text{delta\%neg}} := \frac{V_{\text{nom}} - V_{\min}}{V_{\text{nom}}} \cdot 100$$

$$V_{\text{delta\%neg}} = 1.926$$

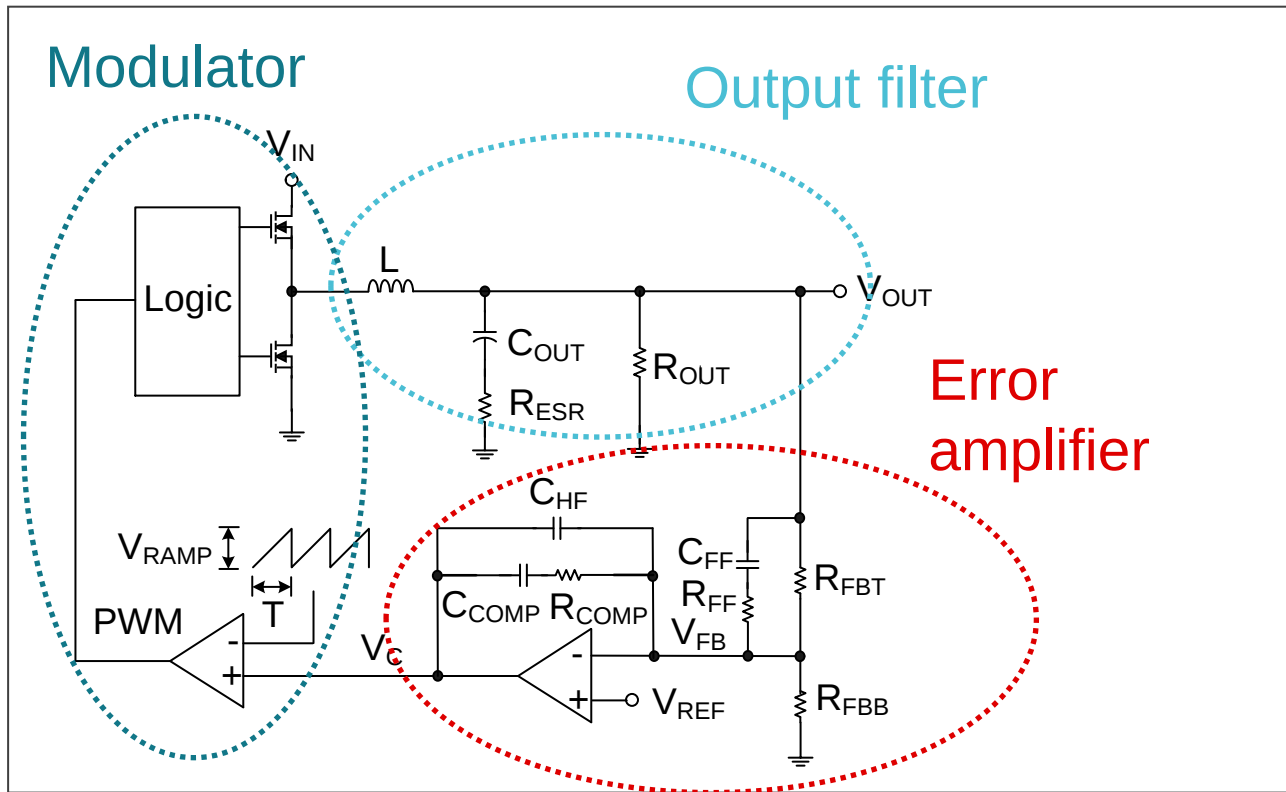
Voltage-mode buck loop stability worst case

Problem statement

- What is my worst case loop stability

Procedure

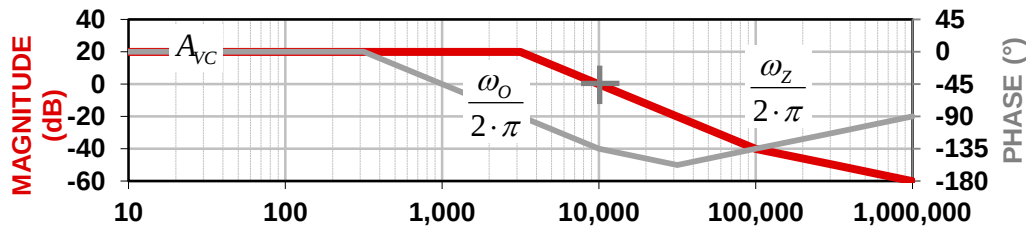
- Find tolerances for L , C_{OUT} , and compensation components.
- Write equation for the power stage, and the type 3 error amp
- Plot the bode plot for each section
- Plot the loop bode plot



Voltage-mode buck loop stability worst case

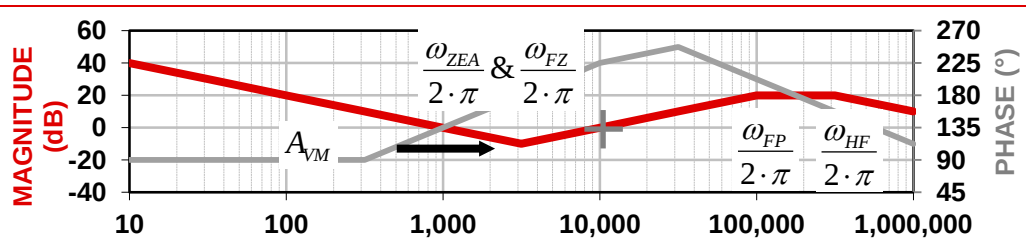
Power stage

$$\frac{\hat{v}_{OUT}}{\hat{v}_C} \approx A_{VC} \cdot \frac{1 + \frac{s}{\omega_z}}{1 + \frac{s}{Q_o \cdot \omega_o} + \frac{s^2}{\omega_o^2}}$$



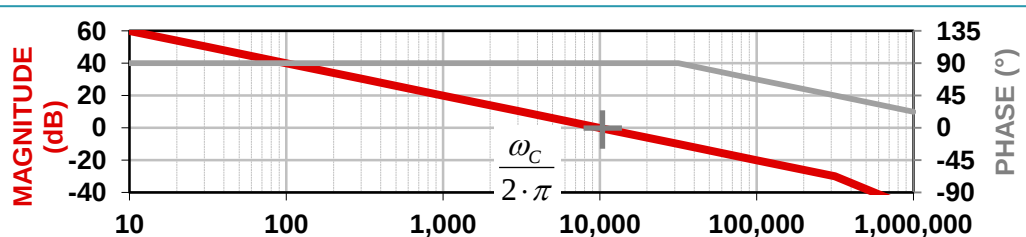
Error amplifier

$$\frac{\hat{v}_C}{\hat{v}'_{OUT}} \approx -A_{VM} \cdot \frac{\left(1 + \frac{\omega_{ZEA}}{s}\right) \cdot \left(1 + \frac{s}{\omega_{FZ}}\right)}{\left(1 + \frac{s}{\omega_{FP}}\right) \cdot \left(1 + \frac{s}{\omega_{HF}}\right)}$$

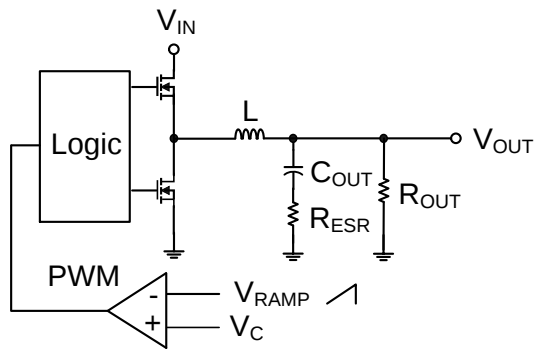


Control loop

$$\frac{\hat{v}_{OUT}}{\hat{v}'_{OUT}} = \frac{\hat{v}_{OUT}}{\hat{v}_C} \cdot \frac{\hat{v}_C}{\hat{v}'_{OUT}}$$



Voltage-mode buck power stage

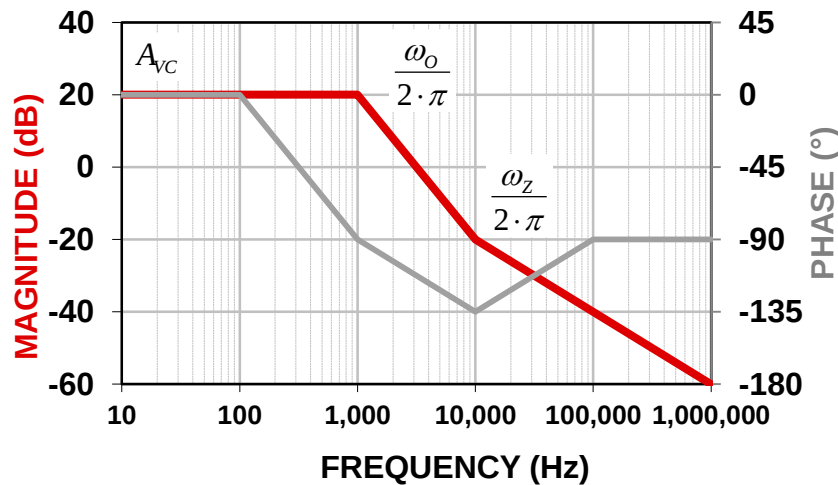


$$A_{VC} = \frac{V_{IN}}{V_{RAMP}}$$

$$\omega_O = \frac{1}{\sqrt{L \cdot C_{OUT}}}$$

$$Q_O = \frac{R_{OUT}}{\sqrt{L/C_{OUT}}}$$

$$\omega_Z = \frac{1}{R_{ESR} \cdot C_{OUT}}$$



$$\frac{\hat{v}_{OUT}}{\hat{v}_C} = A_{VC} \cdot \frac{1 + \frac{s}{\omega_Z}}{1 + \frac{s}{Q_O \cdot \omega_O} + \frac{s^2}{\omega_O^2}}$$

Loop stability worst case

$$\underline{\text{Vinmin}} := 26\text{V}$$

$$\underline{\text{Vinmax}} := 30\text{V}$$

$$K5 := .46$$

$$\text{fzeromax} := \frac{1}{\text{ESRCoutmin} \cdot \text{Coutmin}}$$

$$\text{fzeromin} := \frac{1}{\text{ESRCoutmax} \cdot \text{Coutmax}}$$

$$\text{Vrampmin} := 1.8\text{V}$$

$$\text{Vrampmax} := 2.2\text{V}$$

$$\omega := (100, 200.. 6400000)$$

$$\text{gainmin} := \frac{\text{Vinmin}}{\text{Vrampmax}}$$

$$\text{gainmin} = 11.818$$

$$\text{Cout1} := 470 \cdot 10^{-6}$$

$$\text{fpolemax} := \frac{1}{\sqrt{\frac{\text{Loutmin}}{H}} \cdot \text{Coutmin} \cdot \frac{R_{Lmax}}{\Omega}}$$

$$\text{fpolemin} := \frac{1}{\sqrt{\frac{\text{Loutmax}}{H}} \cdot \text{Coutmax} \cdot \frac{R_{Lmin}}{\Omega}}$$

$$\text{gainmax} := \frac{\text{Vinmax}}{\text{Vrampmin}}$$

$$\text{gainmax} = 16.667$$

$$\text{RCout1} := 0.05$$

$$\text{Qomax} := \frac{\Omega}{\sqrt{\frac{\text{Loutmin}}{H}} \cdot \text{Coutmin}}$$

$$\text{Qomin} := \frac{\Omega}{\sqrt{\frac{\text{Loutmax}}{H}} \cdot \text{Coutmax}}$$

$$\text{Loutmin} := \text{Lout_act} - \text{Lout_act} \cdot 20\%$$

$$\text{Loutmin} = 1.76 \times 10^{-5} \text{ H}$$

$$\text{Loutmax} := \text{Lout_act} + \text{Lout_act} \cdot 20\%$$

$$\text{Loutmax} = 2.64 \times 10^{-5} \text{ H}$$

$$\text{Coutmin} := \text{Cout1} \cdot (1 - K5)$$

$$\text{Coutmin} = 2.538 \times 10^{-4}$$

$$\text{Coutmax} := \text{Cout1} \cdot (1 + K5)$$

$$\text{Coutmax} = 6.862 \times 10^{-4}$$

$$\text{ESRCoutmax} := \text{RCout1} \cdot (1 + 20\%)$$

$$\text{ESRCoutmax} = 0.06$$

$$\text{ESRCoutmin} := \text{RCout1} \cdot (1 - 20\%)$$

$$\text{ESRCoutmin} = 0.04$$

$$\text{PSmin}(\omega) := \text{gainmin} \cdot \frac{1 + \frac{i \cdot \omega}{\text{fzeromin}}}{1 + \frac{i \cdot \omega}{\text{Qomin} \cdot \text{fpolemin}} + \frac{\omega^2}{\text{fpolemin}^2}}$$

$$\text{PSmax}(\omega) := \text{gainmax} \cdot \frac{1 + \frac{i \cdot \omega}{\text{fzeromax}}}{1 + \frac{i \cdot \omega}{\text{Qomax} \cdot \text{fpolemax}} + \frac{\omega^2}{\text{fpolemax}^2}}$$

$$\text{PSmagmin}(\omega) := 20 \cdot \log(|\text{PSmin}(\omega)|)$$

$$\text{PSmagmax}(\omega) := 20 \cdot \log(|\text{PSmax}(\omega)|)$$

$$\text{PSphasemin}(\omega) := -\frac{180}{\pi} \cdot \arg(\text{PSmin}(\omega))$$

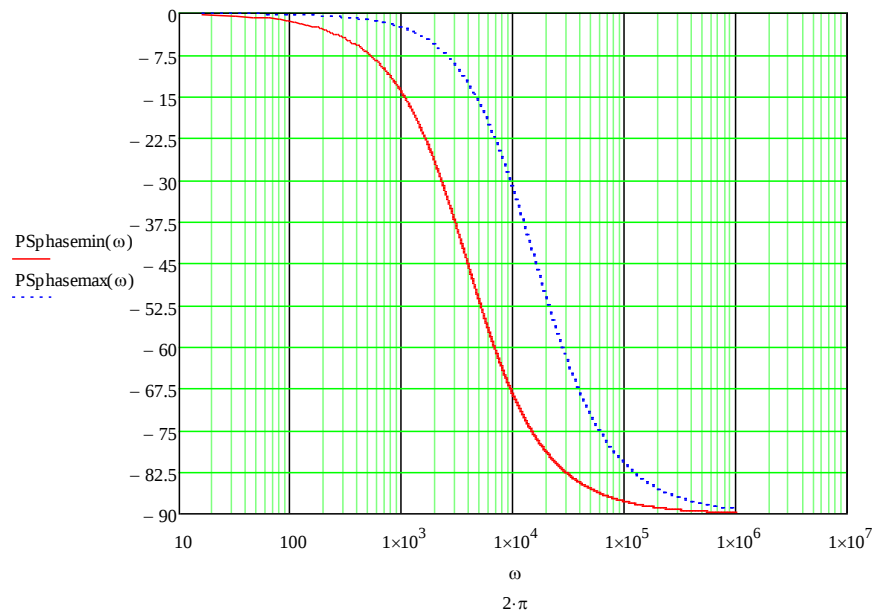
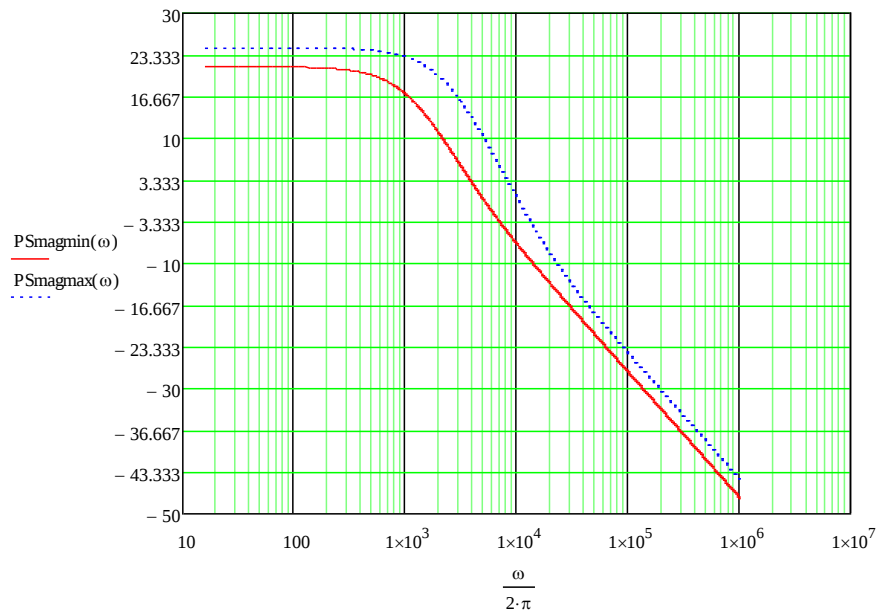
$$\text{PSphasemax}(\omega) := -\frac{180}{\pi} \cdot \arg(\text{PSmax}(\omega))$$

$$R_{Lmin} := 75 \cdot \Omega$$

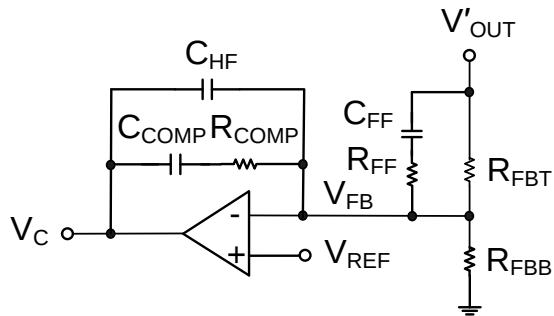
$$R_{Lmax} := 5 \cdot \Omega$$

TI Information – Selective Disclosure

Loop stability worst case



Type III error amplifier



$$A_{VM} \approx \frac{R_{COMP}}{R_{FBT}}$$

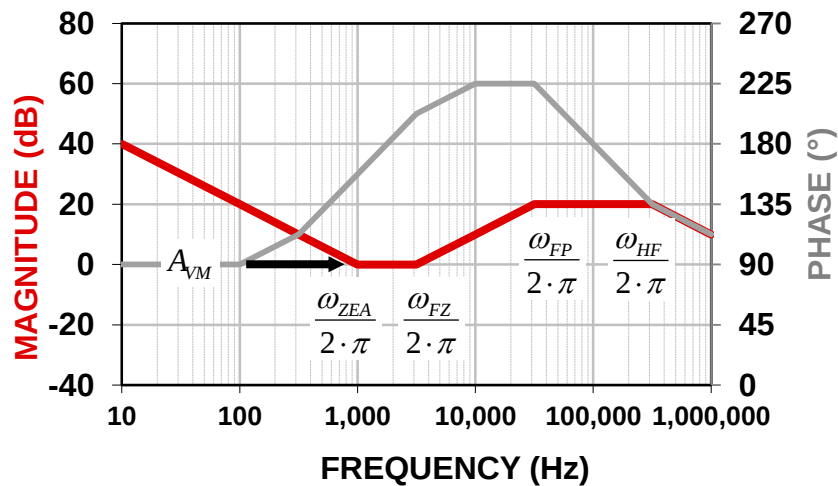
$$\omega_{ZEA} = \frac{1}{R_{COMP} \cdot C_{COMP}}$$

$$\omega_{FZ} \approx \frac{1}{R_{FBT} \cdot C_{FF}}$$

$$\omega_{FP} = \frac{1}{R_{FF} \cdot C_{FF}}$$

$$\omega_{HF} \approx \frac{1}{R_{COMP} \cdot C_{HF}}$$

Assumptions: $C_{COMP} \gg C_{HF}$ & $R_{FBT} \gg R_{FF}$



$$\frac{\hat{v}_C}{\hat{v}'_{OUT}} = -A_{VM} \cdot \frac{\left(1 + \frac{\omega_{ZEA}}{s}\right) \cdot \left(1 + \frac{s}{\omega_{FZ}}\right)}{\left(1 + \frac{s}{\omega_{FP}}\right) \cdot \left(1 + \frac{s}{\omega_{HF}}\right)} = -\frac{A_{VM} \cdot \omega_{ZEA}}{s} \cdot \frac{\left(1 + \frac{s}{\omega_{ZEA}}\right) \cdot \left(1 + \frac{s}{\omega_{FZ}}\right)}{\left(1 + \frac{s}{\omega_{FP}}\right) \cdot \left(1 + \frac{s}{\omega_{HF}}\right)}$$

Loop stability worst case

$$k1 := .007875$$

$$R_{fbt} := 51.1K$$

$$R_{fbtmin} := R_{fbt} \cdot ((1 - k1))$$

$$R_{fbtmax} := R_{fbt} \cdot ((1 + k1))$$

$$R_{comp} := 100K$$

$$R_{compmin} := R_{comp} \cdot ((1 - k1))$$

$$R_{compmax} := R_{comp} \cdot ((1 + k1))$$

$$Chf := 2200 \cdot 10^{-12}$$

$$Chfmin := Chf \cdot (1 - K3)$$

$$Chfmax := Chf \cdot (1 + K3)$$

$$C_{comp} := 1800 \cdot 10^{-12}$$

$$C_{compmin} := C_{comp} \cdot (1 - K3)$$

$$C_{compmax} := C_{comp} \cdot (1 + K3)$$

$$C_{ff} := 1800 \cdot 10^{-12}$$

$$C_{ffmin} := C_{ff} \cdot (1 - K3)$$

$$C_{ffmax} := C_{ff} \cdot (1 + K3)$$

$$K3 := .057$$

$$R_{fbb} := 10K$$

$$R_{fbbmin} := R_{fbb} \cdot ((1 - k1))$$

$$R_{fbbmax} := R_{fbb} \cdot ((1 + k1))$$

$$R_{ff} := 26.12K$$

$$R_{ffmin} := R_{ff} \cdot ((1 - k1))$$

$$R_{ffmax} := R_{ff} \cdot ((1 + k1))$$

$$Chfmin = 2.075 \times 10^{-9}$$

$$Chfmax = 2.325 \times 10^{-9}$$

$$C_{compmin} = 1.697 \times 10^{-9}$$

$$C_{compmax} = 1.903 \times 10^{-9}$$

$$C_{ffmin} = 1.697 \times 10^{-9}$$

$$C_{ffmax} = 1.903 \times 10^{-9}$$

$$A_{vmmin} := \frac{R_{compmin}}{R_{fbtmax}}$$

$$A_{vmmax} := \frac{R_{compmax}}{R_{fbtmin}}$$

$$W_{zeamin} := \frac{1}{R_{compmax} \cdot C_{compmax}}$$

$$W_{zeamax} := \frac{1}{R_{compmin} \cdot C_{compmin}}$$

$$W_{fzmin} := \frac{1}{R_{fbtmax} \cdot C_{ffmax}}$$

$$W_{fzmax} := \frac{1}{R_{fbtmin} \cdot C_{ffmin}}$$

$$W_{fpmin} := \frac{1}{R_{ffmax} \cdot C_{ffmax}}$$

$$W_{fpmax} := \frac{1}{R_{ffmin} \cdot C_{ffmin}}$$

$$W_{hfmin} := \frac{1}{R_{compmax} \cdot Chfmax}$$

$$W_{hfmax} := \frac{1}{R_{compmin} \cdot Chfmin}$$

$$A_{vmmin} = 1.926$$

$$A_{vmmax} = 1.988$$

$$W_{zeamin} = 5.215 \times 10^3$$

$$W_{zeamax} = 5.938 \times 10^3$$

$$W_{fzmin} = 1.021 \times 10^4$$

$$W_{fzmax} = 1.162 \times 10^4$$

$$W_{fpmin} = 1.997 \times 10^4$$

$$W_{fpmax} = 2.273 \times 10^4$$

$$W_{hfmin} = 4.267 \times 10^3$$

$$W_{hfmax} = 4.858 \times 10^3$$

$$G_{cmin}(\omega) := -\frac{A_{vmmin} \cdot W_{zeamin}}{i \cdot \omega} \cdot \frac{\left[1 + \frac{(i \cdot \omega)}{W_{zeamin}}\right] \cdot \left(1 + \frac{i \cdot \omega}{W_{fzmin}}\right)}{\left(1 + \frac{i \cdot \omega}{W_{fpmax}}\right) \cdot \left(1 + \frac{i \cdot \omega}{W_{hfmax}}\right)}$$

$$G_{cmax}(\omega) := -\frac{A_{vmmax} \cdot W_{zeamax}}{i \cdot \omega} \cdot \frac{\left[1 + \frac{(i \cdot \omega)}{W_{zeamax}}\right] \cdot \left(1 + \frac{i \cdot \omega}{W_{fzmax}}\right)}{\left(1 + \frac{i \cdot \omega}{W_{fpmin}}\right) \cdot \left(1 + \frac{i \cdot \omega}{W_{hfmin}}\right)}$$

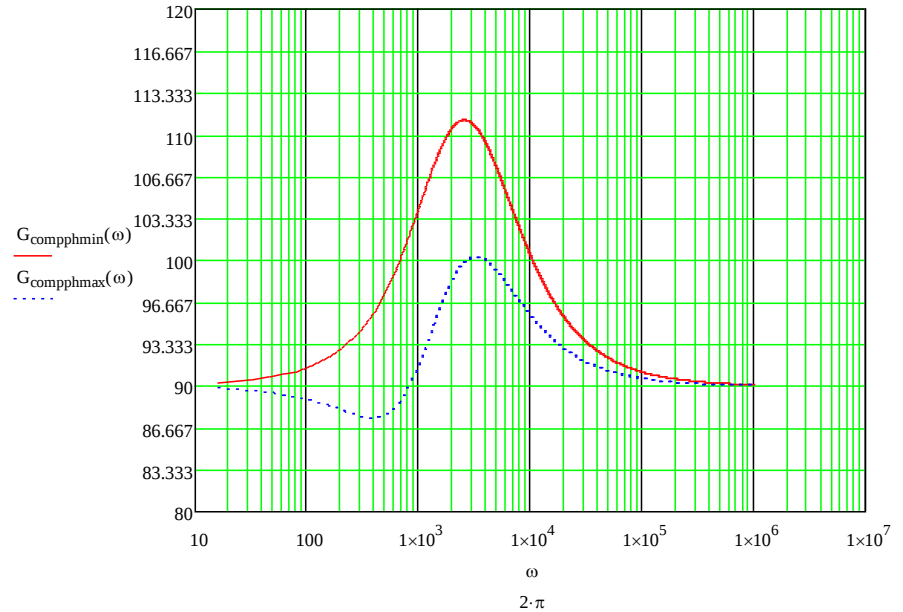
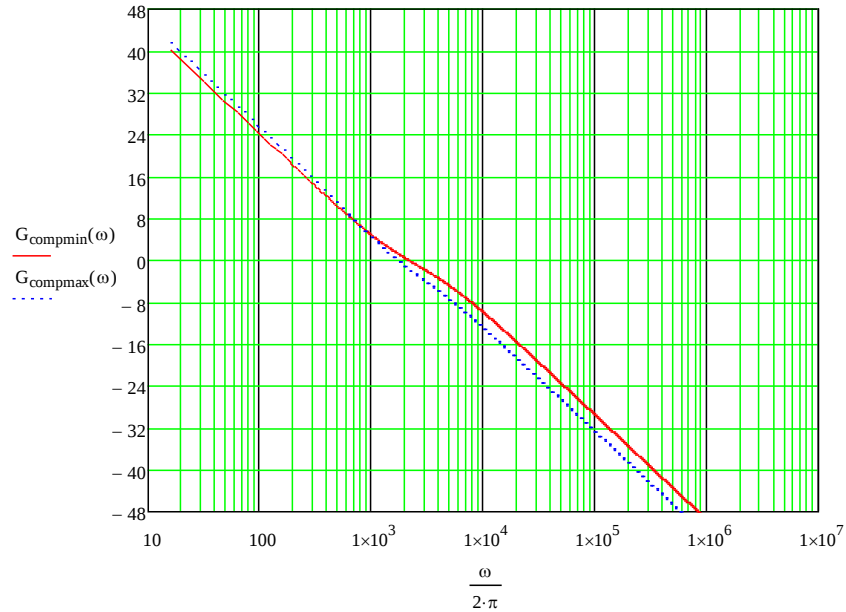
$$G_{compmin}(\omega) := 20 \cdot \log(|G_{cmin}(\omega)|)$$

$$G_{compmax}(\omega) := 20 \cdot \log(|G_{cmax}(\omega)|)$$

$$G_{compmin}(\omega) := \frac{180}{\pi} \cdot \arg(G_{cmin}(\omega))$$

$$G_{compmax}(\omega) := \frac{180}{\pi} \cdot \arg(G_{cmax}(\omega))$$

Loop stability worst case



Loop stability worst case

Open Loop Response:

$$G_{loopmin}(\omega) := -PS_{min}(\omega) \cdot G_{cmin}(\omega)$$

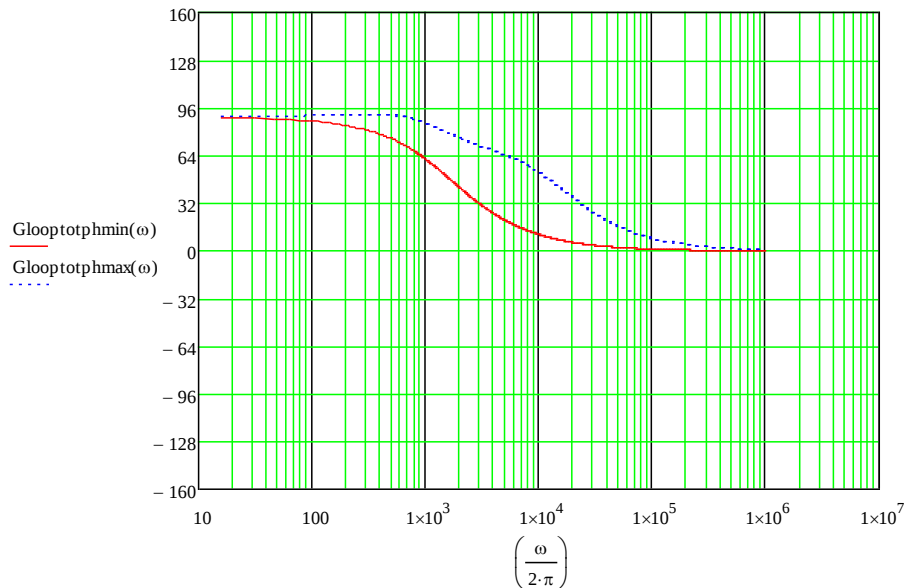
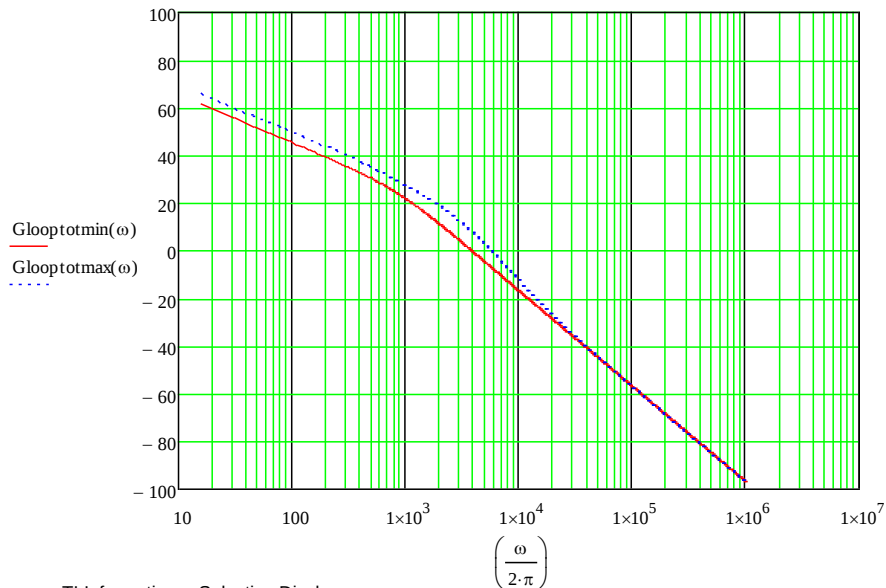
$$G_{loopmax}(\omega) := -PS_{max}(\omega) \cdot G_{cmax}(\omega)$$

$$G_{looptotmin}(\omega) := 20 \cdot \log(|G_{loopmin}(\omega)|)$$

$$G_{looptotphmin}(\omega) := -\frac{180}{\pi} \cdot \arg(G_{loopmin}(\omega))$$

$$G_{looptotmax}(\omega) := 20 \cdot \log(|G_{loopmax}(\omega)|)$$

$$G_{looptotphmax}(\omega) := -\frac{180}{\pi} \cdot \arg(G_{loopmax}(\omega))$$



TI Information – Selective Disclosure

Worst Case Analysis MOSFET Power Dissipation Example

Problem statement

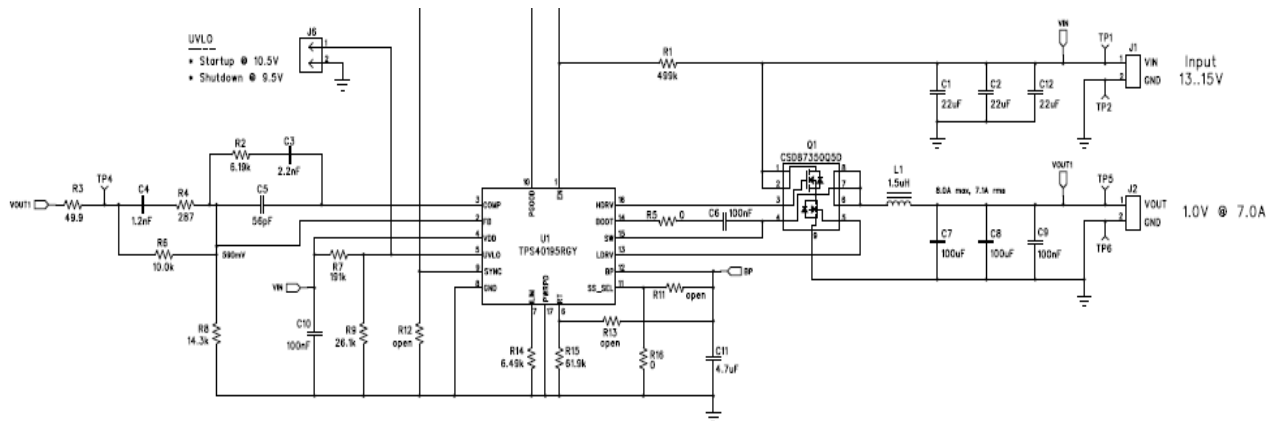
- The FET's in my PS are getting hot

Possible causes

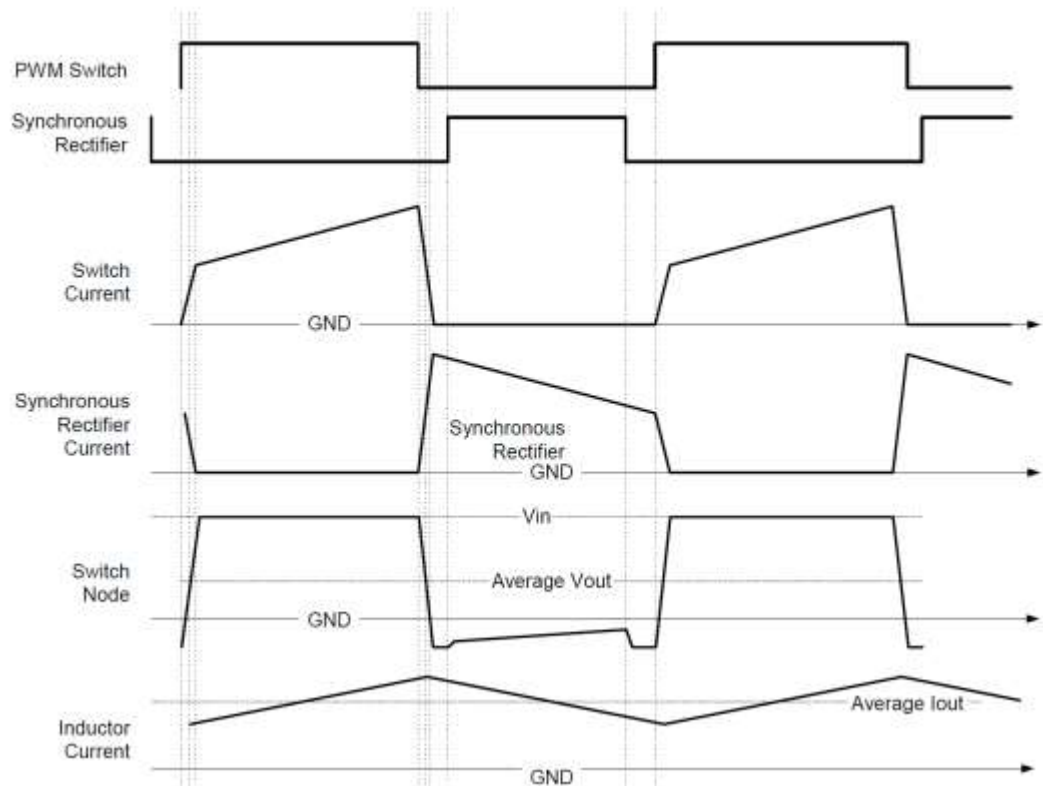
- Not enough heat sink
- Shoot through

Solution

- WCA on FET power dissipation



Worst Case Analysis MOSFET Power Dissipation Example



Procedure

- Find tolerances for R_{ds} , Q_g total gate charge, Q_{gs} charge gate to source, Q_{gd} charge gate to drain, Q_{oss} output charge, body drain diode forward voltage, and controller dead time.
- Write equation and Analyze R_{ds} conducted losses, switching loss, and gate drive loss for top FET.
- Write equation and Analyze R_{ds} conducted losses, body drain diode loss, and gate drive loss for bottom FET
- Add up all losses

Worst Case Analysis component Tolerances

MOSFET tolerance

CSD87350Q5D Synchronous Buck NexFET™ Power Block

Rds goes up as temp goes up

$$R_{ds_bol} = 20\%$$

$$R_{ds_tempmax} = 63\%$$

$$R_{ds_tempmin} = -40\%$$

$$R_{ds(on)_top} := 5 \cdot 10^{-3} \cdot \Omega$$

$$R_{ds(on)_bot} := 1.2 \cdot 10^{-3} \cdot \Omega$$

$$R_{dsmin_top} = 2.4 \times 10^{-3} \Omega$$

$$R_{dsmin_bot} = 5.76 \times 10^{-4} \Omega$$

$$R_{dsmax_top} = 9.78 \times 10^{-3} \Omega$$

$$R_{dsmax_bot} = 2.347 \times 10^{-3} \Omega$$

Total gate charge

$$q_{total_top} := 8.4nC$$

$$q_{total_bol} := 30\%$$

$$q_{total_bot} := 20nC$$

$$q_{total_min_top} = 5.88 \times 10^{-9} C$$

$$q_{total_min_bot} = 1.4 \times 10^{-8} C$$

$$q_{total_max_top} = 1.092 \times 10^{-8} C$$

$$q_{total_max_bot} = 2.6 \times 10^{-8} C$$

Gate charge gate to drain and gate to source

$$Q_{gd_top} := 1.6nC$$

$$Q_{gd_bol} := 30\%$$

$$Q_{gs_top} := 2.6nC$$

$$Q_{gs_bol} := 30\%$$

$$Q_{gd_min_top} = 1.12 \times 10^{-9} C$$

$$Q_{gs_min_top} = 1.82 \times 10^{-9} C$$

$$Q_{gd_max_top} = 2.08 \times 10^{-9} C$$

$$Q_{gs_max_top} = 3.38 \times 10^{-9} C$$

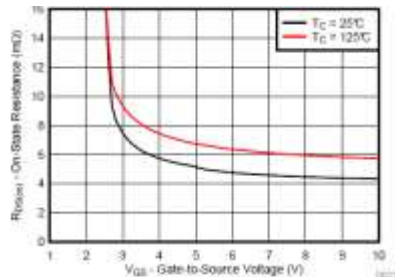


Figure 20. Control MOSFET $R_{DS(on)}$ vs V_{GS}

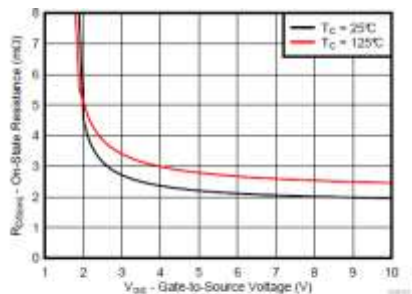


Figure 21. Sync MOSFET $R_{DS(on)}$ vs V_{GS}

Worst Case Analysis component Tolerances

MOSFET tolerance

Qoss output charge

$$\begin{aligned} Q_{oss_bol} &:= 30\% & Q_{oss_top} &:= 9.7\text{nC} & Q_{oss_min_top} &= 6.79 \times 10^{-9}\text{C} & Q_{oss_bot} &:= 28\text{nC} & Q_{oss_min_bot} &= 1.96 \times 10^{-8}\text{C} \\ & & & & Q_{oss_max_top} &= 1.261 \times 10^{-8}\text{C} & & & Q_{oss_max_bot} &= 3.64 \times 10^{-8}\text{C} \end{aligned}$$

Body drain diode forward voltage

$$V_{body} := .8\text{V}$$

$$V_{body_bol} := 25\% \quad V_{body_temphot} := 30\% \text{ At } 125\text{C} \quad V_{body_tempcold} := 22.5\% \text{ At } -50\text{C}$$

$$V_{body_max} = 1.3\text{V}$$

$$V_{body_min} = 0.42\text{V}$$

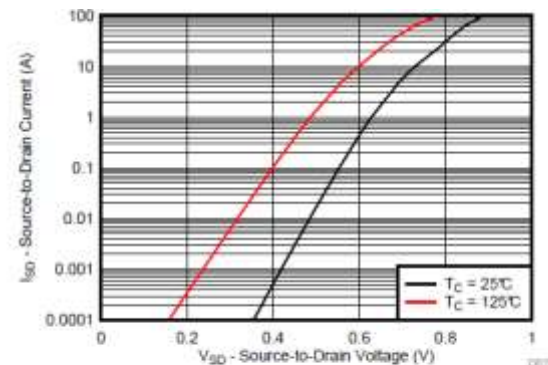


Figure 25. Sync MOSFET Body Diode

Worst Case Analysis component Tolerances

TPS40190 Controller dead time tolerance for body diode PWR calculation

Deadtime_HSoff_LSon := 50ns Deadtime_LSoff_HSon := 25ns DT_bol := 20%

Deadtime_HSoff_LSon_min = 4×10^{-8} s Deadtime_LSoff_HSon_min = 2×10^{-8} s

Deadtime_HSoff_LSon_max = 6×10^{-8} s Deadtime_LSoff_HSon_max = 3×10^{-8} s

Power block delay time tolerance for body diode PWR calculation

Td_FET_bol := 30% Turnon_dly_HS := 7ns Turnon_dly_LS := 8ns Turnoff_dly_HS := 13ns Turnoff_dly_LS := 33ns

Trise_HS := 17ns Trise_LS := 10ns Tfall_HS := 2.3ns Tfall_LS := 4.7ns

Turnon_dly_HSmin = 4.9×10^{-9} s Trise_HSmin = 1.19×10^{-8} s Turnoff_dly_HSmin = 9.1×10^{-9} s Tfall_HSmin = 1.61×10^{-9} s

Turnon_dly_HSmax = 9.1×10^{-9} s Trise_HSmax = 2.21×10^{-8} s Turnoff_dly_HSmax = 1.69×10^{-8} s Tfall_HSmax = 2.99×10^{-9} s

Turnon_dly_LSmin = 5.6×10^{-9} s Trise_LSmin = 7×10^{-9} s Turnoff_dly_LSmin = 2.31×10^{-8} s Tfall_LSmin = 3.29×10^{-9} s

Turnon_dly_LSmax = 1.04×10^{-8} s Trise_LSmax = 1.3×10^{-8} s Turnoff_dly_LSmax = 4.29×10^{-8} s Tfall_LSmax = 6.11×10^{-9} s

Worst Case Analysis MOSFET Power Dissipation Example

1) First calculate conducted loss

$$I_{rms_top_fet} = 10.462 \text{ A}$$

$$P_{fet_cond_topmax} := I_{rms_top_fet}^2 \cdot R_{dsmax_top} \quad P_{fet_cond_topmax} = 1.07 \cdot \text{W} \quad (\text{Cond losses})$$

$$P_{fet_cond_topmin} := I_{rms_top_fet}^2 \cdot R_{dsmin_top} \quad P_{fet_cond_topmin} = 0.263 \cdot \text{W} \quad (\text{Cond losses})$$

$$I_{rms_bot_fet} = 38.677 \text{ A}$$

$$P_{fet_cond_botmax} := I_{rms_bot_fet}^2 \cdot R_{dsmax_bot} \quad P_{fet_cond_botmax} = 3.511 \text{ W} \quad (\text{Cond losses})$$

$$P_{fet_cond_botmin} := I_{rms_bot_fet}^2 \cdot R_{dsmin_bot} \quad P_{fet_cond_botmin} = 0.862 \text{ W} \quad (\text{Cond losses})$$

2) Calculate top FET switching loss

$$I_g := 1 \text{ A}$$

$$P_{sw_fet_top} := V_{inmax} \cdot f_{max} \cdot \left[\frac{I_{pfet_top} \cdot (Q_{gd_max_top} + Q_{gs_max_top})}{I_g} + \frac{Q_{oss_max_top} + Q_{oss_max_bot}}{2} \right] \quad P_{sw_fet_top} = 1.502 \text{ W} \quad (\text{Switching losses})$$

$$T_{sw} := 18 \cdot \text{ns}$$

$$P_{d_SW_FET} := 2 \cdot \left[\frac{1}{T_{min}} \cdot \int_0^{T_{sw}} \left(V_{inmax} \cdot \frac{t}{T_{sw}} \right) \cdot \left[I_{pfet_top} \cdot \left(1 - \frac{t}{T_{sw}} \right) \right] dt \right] \quad P_{d_SW_FET} = 1.517 \cdot \text{W} \quad (\text{Switching losses})$$

Bottom FET has body diode voltage across it at turn on/off therefore loss is in the body diode

Worst Case Analysis MOSFET Power Dissipation Example

3) Calculate gate drive losses

PARAMETER	TEST CONDITIONS	Q1 CONTROL FET			Q2 SYNC FET			UNIT
		MIN	TYP	MAX	MIN	TYP	MAX	
R _G	Series gate resistance		1.3	3		0.8	2	Ω

PARAMETER	TEST CONDITIONS	MIN	TYP	MAX	UNIT
OUTPUT DRIVERS					
R _{HDHI}	High-side driver pull-up resistance	V _{BOOT} - V _{SW} = 4.5 V, I _{HDRV} = -100 mA		3	6 Ω
R _{HDLO}	High-side driver pull-down resistance	V _{BOOT} - V _{SW} = 4.5 V, I _{HDRV} = 100 mA		1.5	3 Ω
R _{LDHI}	Low-side driver pull-up resistance	I _{LDRV} = -100 mA		2.5	5 Ω
R _{LDLO}	Low-side driver pull-down resistance	I _{LDRV} = 100 mA		0.8	1.5 Ω

V_{gate} := 8V

P_{g_dr_top} := f · q_{total_max_top} · V_{gate} P_{g_dr_top} = 0.028 W (Gate losses)

Act_{gate_drive_pwr_top} := $\frac{1.3}{3}$ · P_{g_dr_top} Act_{gate_drive_pwr_top} = 0.012 W

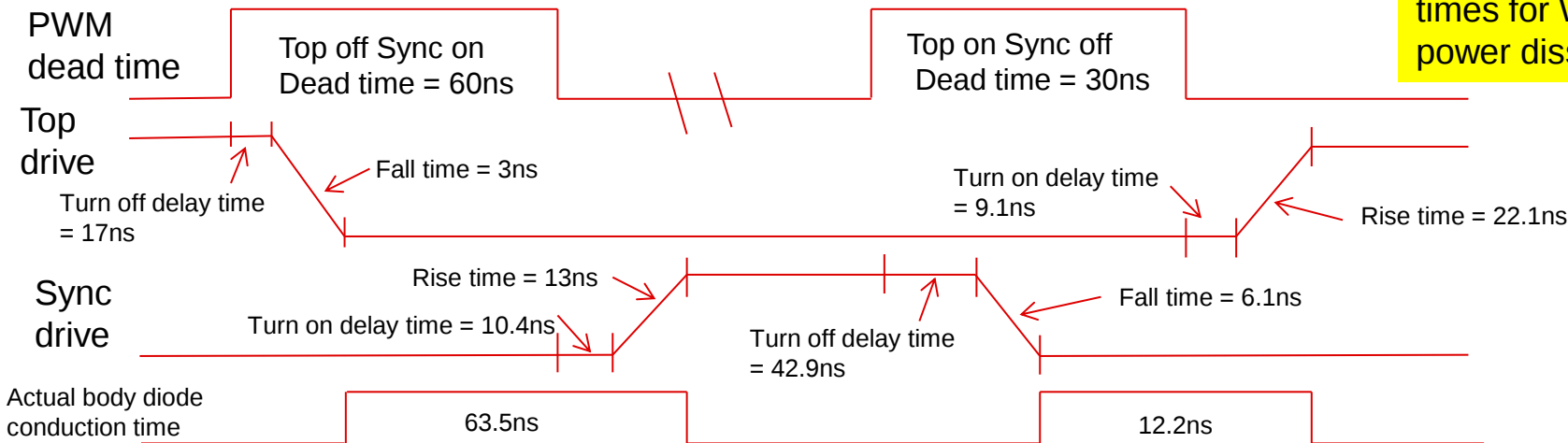
P_{g_dr_bot} := f · q_{total_max_bot} · V_{gate} P_{g_dr_bot} = 0.068 W (Gate losses)

Act_{gate_drive_pwr_LS} := $\frac{.8}{2.5}$ · P_{g_dr_bot} Act_{gate_drive_pwr_LS} = 0.022 W

Worst Case Analysis MOSFET Power Dissipation Example

3) Calculate body diode losses

Used maximum times for WC power dissipation



$$T_{delay1} := \text{Deadtime_HSoff_LSon_max} - \text{Turnoff_dly_HSmax} - T_{fall_HSmax} + \text{Turnon_dly_LSmax} + T_{rise_LSmax}$$

$$T_{delay1} = 6.351 \times 10^{-8} \text{ s}$$

$$T_{delay2} := \text{Deadtime_LSoff_HSON_max} - \text{Turnoff_dly_LSmax} - T_{fall_LSmax} + \text{Turnon_dly_HSmax} + T_{rise_HSmax}$$

$$T_{delay2} = 1.219 \times 10^{-8} \text{ s}$$

$$P_{body_diode_max} := V_{body_min} \cdot I_{omax} \cdot \frac{T_{delay1} + T_{delay2}}{T_{min}}$$

$$P_{body_diode_max} = 0.475 \text{ W}$$

Worst Case Analysis MOSFET Power Dissipation Example

4) Add up all the top and bottom FET losses

$$P_{fet_tot_top_min} := P_{fet_cond_topmin} + P_{sw_fet_top} + A_{ct_gate_drive_pwr_top}$$

$$P_{fet_tot_top_min} = 1.777\text{ W} \quad (\text{Total top FET losses Cond min})$$

$$P_{fet_tot_top_max} := P_{fet_cond_topmax} + P_{sw_fet_top} + A_{ct_gate_drive_pwr_top}$$

$$P_{fet_tot_top_max} = 2.584\text{ W} \quad (\text{Total top FET losses max})$$

$$P_{fet_tot_bot_min} := P_{fet_cond_botmin} + A_{ct_gate_drive_pwr_LS} + P_{body_diode_max}$$

$$P_{fet_tot_bot_min} = 1.359\text{ W} \quad (\text{Total bottom FET losses cond min})$$

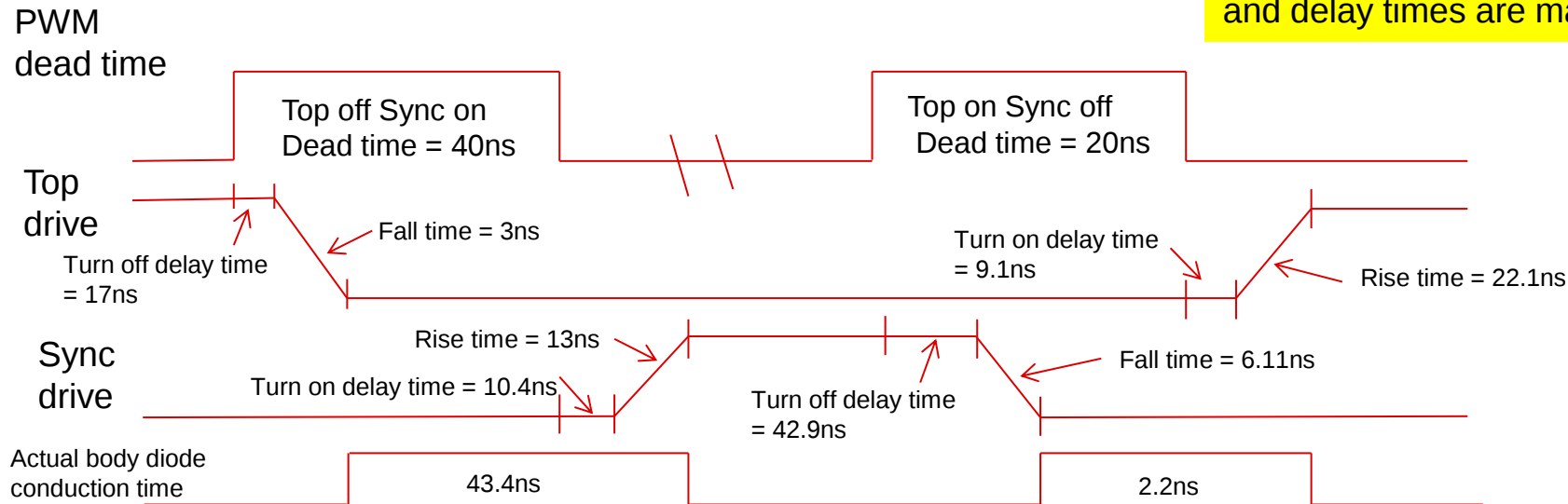
$$P_{fet_tot_bot_max} := P_{fet_cond_botmax} + A_{ct_gate_drive_pwr_LS} + P_{body_diode_max}$$

$$P_{fet_tot_bot_max} = 4.008\text{ W} \quad (\text{Total bottom FET losses max})$$

Worst Case Analysis MOSFET

Cross conduction and Timing issues

Look at what happens when dead time is minimum and delay times are maximum



Summary

- Analyze the circuit to determine potential issues in the design
- Decide what type of analysis needs to be performed - EV, RSS, Monte Carlo
- Write an equation for the potential issues you found
- Determine the variables in each equation
- Determine the BOL, EOL, and temp tolerances for each variable from the manufactures DS or company APL
- Calculate the tolerances for each
- Calculate the behavioral equations using the variable tolerances to determine the worst case parameters for your design

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