



**INTRODUCTION TO ACTIVE AND PASSIVE ANALOG
FILTER DESIGN INCLUDING SOME INTERESTING AND
UNIQUE CONFIGURATIONS**

Speaker:

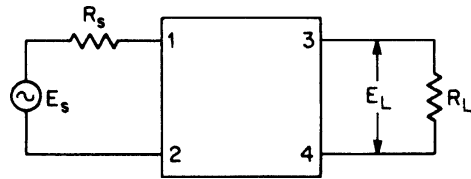
Arthur Williams – Chief Scientist
Telebyte Inc.

Thursday November 20th 2008

TOPICS

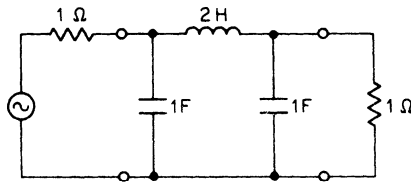
- **Introduction**
- **Basic Filter Polynomial types**
- **Frequency and Impedance Scaling**
- **Active Low-Pass Filters**
- **Design of D-Element Active Low-Pass Filters**
- **High-Pass Filters**
- **Band-Pass Filters**
- **Band-Reject Filters**
- **High-Q Notch Filters**
- **Q-Multiplier Active Band-Pass Filters**
- **Some Useful Passive Filter Transformations**
- **Attenuators**
- **Power Splitters**
- **Miscellaneous Circuits**
- **Questions and Answers**

Introduction



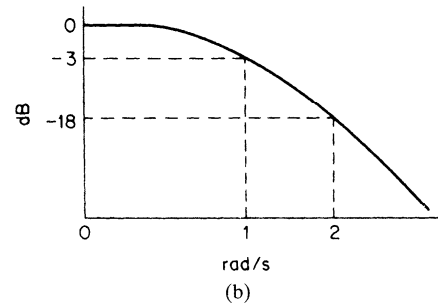
$$T(s) = \frac{E_L}{E_s} = \frac{N(s)}{D(s)}$$

Generalized Passive Filter



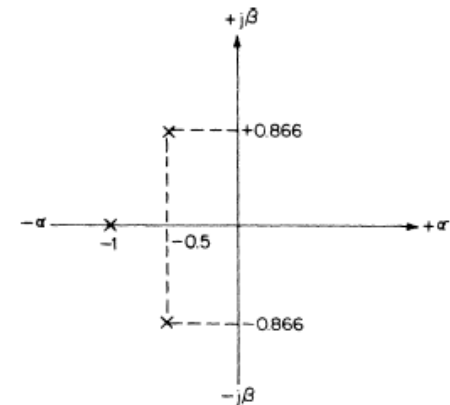
(a)

N=3 Butterworth
Normalized 3dB at 1 Rad/s



(b)

$$T(s) = \frac{1}{s^3 + 2s^2 + 2s + 1}$$



Pole Zero Plot on j-Omega Axis



Most Popular Filter Polynomial Types

Butterworth

Chebyshev

Linear Phase

Elliptic Function

Butterworth

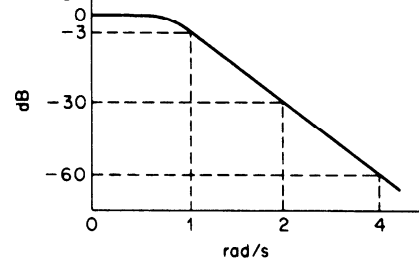
The Butterworth approximation based on the assumption that a flat response at zero frequency is more important than the response at other frequencies.

Normalized transfer function is an all-pole type

Roots all fall on a unit circle

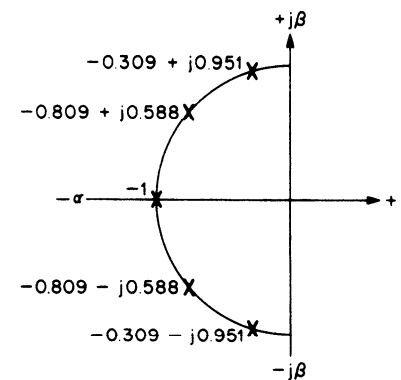
The attenuation is 3 dB at 1 rad/s.

Normalized Frequency Response

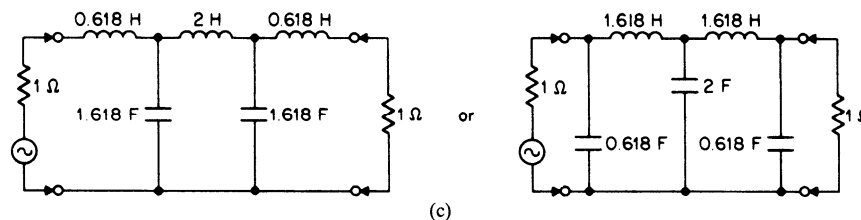


(a)

Roots on j-Omega Axis



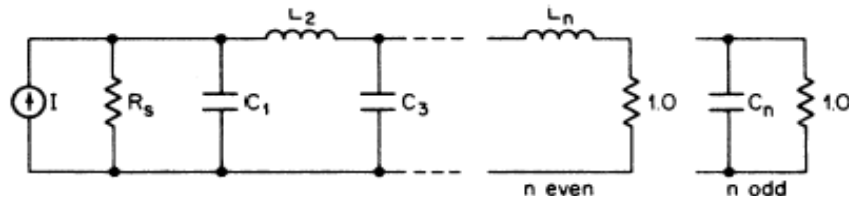
(b)



(c)

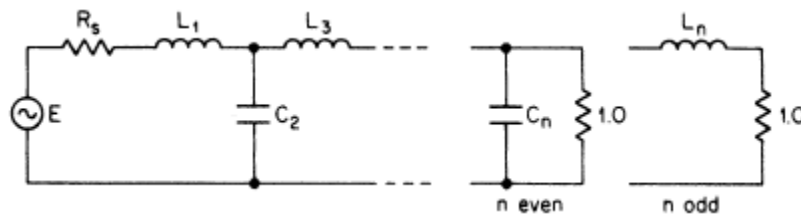
N=5 Butterworth LPF and its Dual

Butterworth LC Element Values (Representative Table, Extensive tables in reference)



n	R_s	C_1	L_2	C_3	L_4	C_5	L_6	C_7
2	1.0000	1.4142	1.4142					
3	1.0000	1.0000	2.0000	1.0000				
4	1.0000	0.7654	1.8478	1.8478	0.7654			
5	1.0000	0.6180	1.6180	2.0000	1.6180	0.6180		
6	1.0000	0.5176	1.4142	1.9319	1.9319	1.4142	0.5176	
7	1.0000	0.4450	1.2470	1.8019	2.0000	1.8019	1.2470	0.4450

n	$1/R_s$	L_1	C_2	L_3	C_4	L_5	C_6	L_7
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Butterworth Normalized Pole Locations

Order n	Real Part $-\alpha$	Imaginary Part $\pm j\beta$
2	0.7071	0.7071
3	0.5000 1.0000	0.8660
4	0.9239 0.3827	0.3827 0.9239
5	0.8090 0.3090 1.0000	0.5878 0.9511
6	0.9659 0.7071 0.2588	0.2588 0.7071 0.9659
7	0.9010 0.6235 0.2225 1.0000	0.4339 0.7818 0.9749

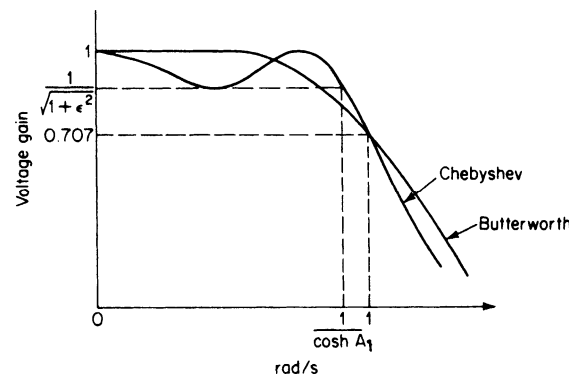
Chebyshev

If the poles of a normalized Butterworth low-pass transfer function were moved to the right by multiplying the real parts of the pole position by a constant k_r and the imaginary parts by a constant k_j where both k 's are <1 , the poles would lie on an ellipse instead of a unit circle.

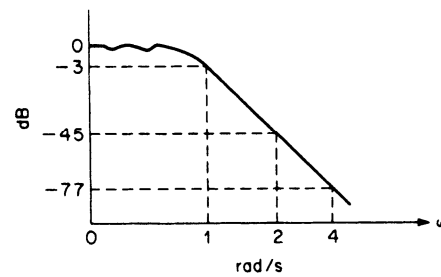
The frequency response would ripple evenly.

The resulting response is called the Chebyshev or Equiripple function.

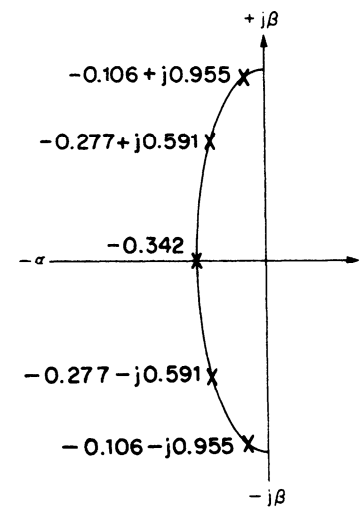
Chebyshev filters are categorized in terms of ripple (in dB) and order N .



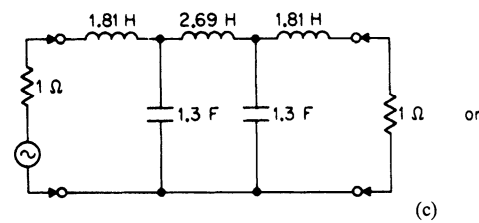
Chebyshev Low-Pass Filter



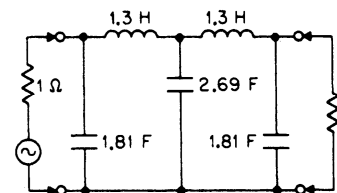
(a)



(b)



or



$$T(s) = \frac{1}{\sinh s + \cosh s}$$

Linear Phase Low Pass Filters

Butterworth filters - good amplitude and transient characteristics

Chebyshev family of filters- increased selectivity but poor transient behavior

Bessel transfer function - optimized to obtain a linear phase, i.e., a maximally flat delay

Frequency response- Much less selective than other filter types

The low-pass approximation to a constant delay can be expressed as the following general Bessel transfer function:

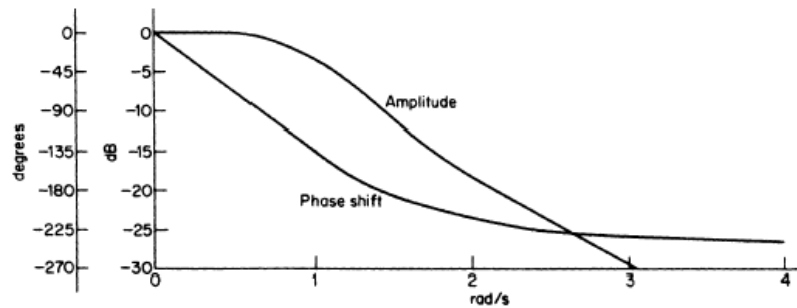
$$T(s) = \frac{1}{\sinh s + \cosh s}$$

Linear Phase Low-Pass Filters

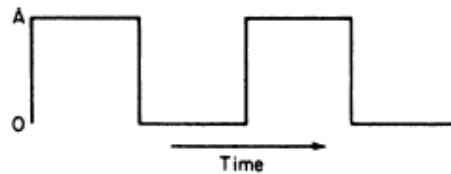
- **Other Linear Phase Filter Families**
 - Gaussian
 - Gaussian to 6dB
 - Gaussian to 12dB
 - Linear Phase with Equiripple Error (0.05° and 0.5°)
 - Maximally Flat Delay with Chebyshev Stop-Band

Extensive tables are available in the reference

Effects of Non-Linear Phase

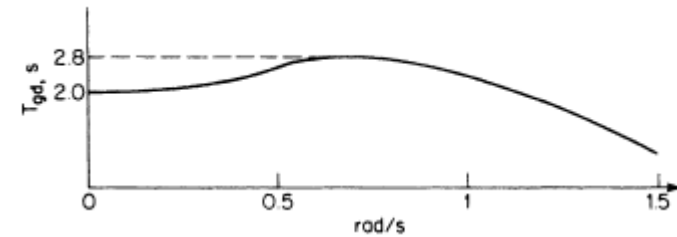


Amplitude and Phase Response of
N=3 Butterworth Low-Pass Filter

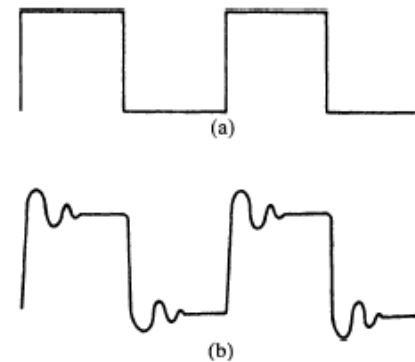


$$A(t) = A \left(\frac{1}{2} + \frac{2}{\pi} \cos \omega_1 \tau - \frac{2}{3\pi} \cos 3\omega_1 \tau + \frac{2}{5\pi} \cos 5\omega_1 \tau + \dots \right)$$

Square Wave containing Fourier Series



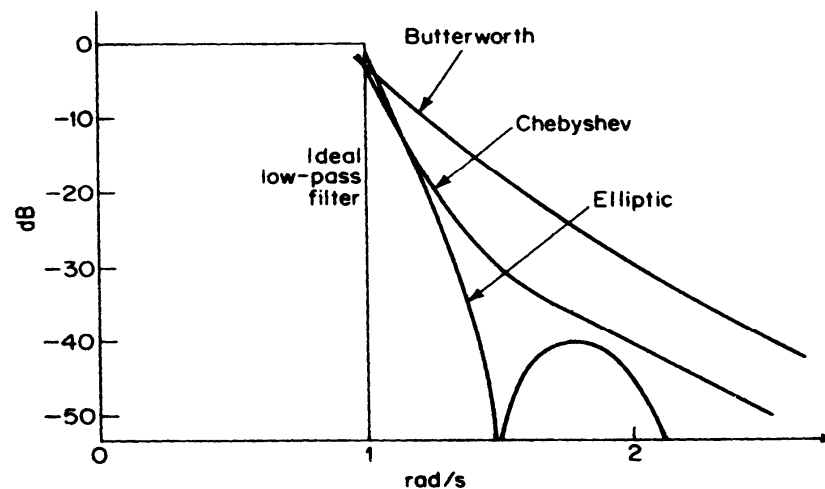
Group Delay of N=3 Butterworth Low-Pass Filter



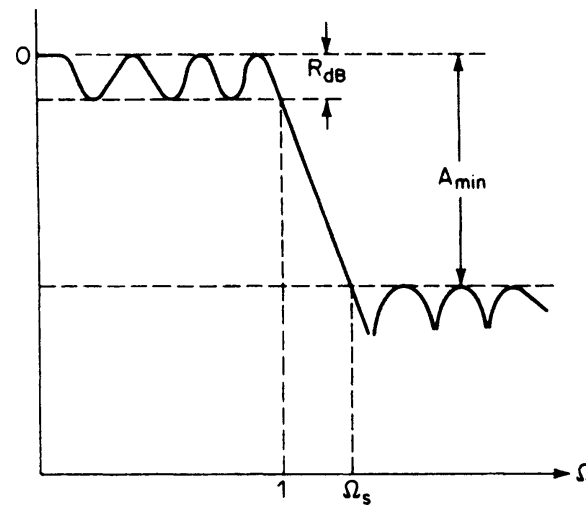
- a) Equally delayed components
- b) Unequally delayed components

Elliptic Function

All filter types previously discussed are all-pole networks. Infinite rejection occurs only at the extremes of the stop-band. Elliptic-function filters have zeros as well as poles at finite frequencies. Introduction of transmission zeros allows the steepest rate of descent theoretically possible for a given number of poles. However the highly non-linear phase response results in poor transient performance.



Normalized Elliptic Function Low-Pass Filter



R_{dB} = Ripple in dB up to cut-off (1 Rad/sec)

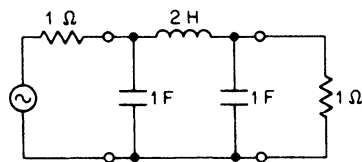
A_{min} = Minimum Stop-Band Attenuation in dB

Ω_s = Normalized Frequency (Rad/sec) to achieve A_{min} (Steepness Factor)

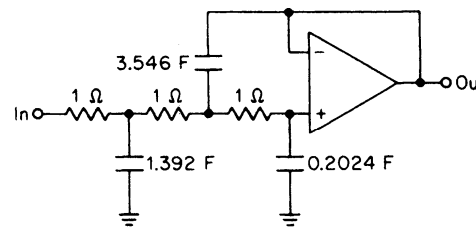
Frequency and Impedance Scaling from Normalized Circuit

Frequency Scaling

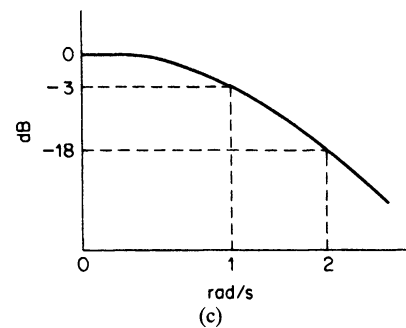
$$\text{FSF} = \frac{\text{desired reference frequency}}{\text{existing reference frequency}}$$



(a)



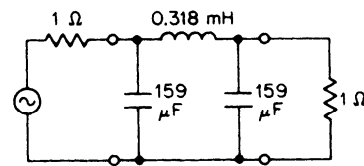
(b)



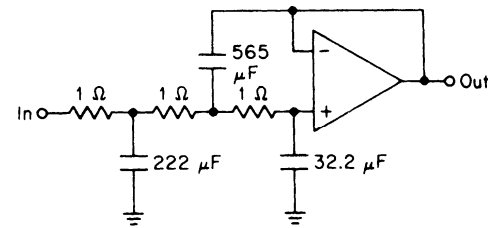
(c)

Normalized N = 3 Butterworth low-pass filter normalized to 1 rad/sec :

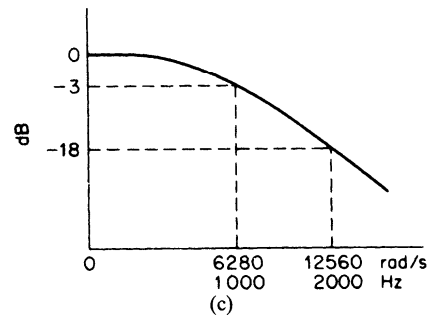
(a) LC filter; (b) active filter; (c) frequency response



(a)



(b)



(c)

Denormalized low-pass filter scaled to 1000Hz: (a) LC filter; (b) active filter; (c) frequency response.

All Ls and Cs of the normalized Low-Pass filter are divided by $2\pi F_C$ where $F_C=1,000$ Hz

Note Impractical Values

Impedance Scaling

Rule

A transfer function of a network remains unchanged if all impedances are multiplied (or divided) by the same factor.

This factor can be a fixed number or a variable, as long as every impedance element that appears in the transfer function is multiplied (or divided) by the same factor.

Impedance scaling can be mathematically expressed as

$$R' = Z \times R$$

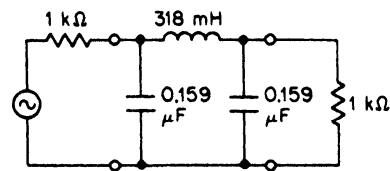
$$L' = Z \times L$$

$$C' = \frac{C}{Z}$$

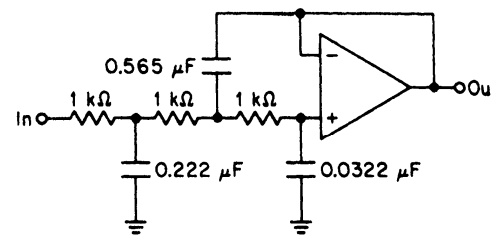
Frequency and impedance scaling are normally combined into one step rather than performed sequentially. The denormalized values are then given by

$$L' = \frac{Z \times L}{FSF}$$

$$C' = \frac{C}{Z \times FSF}$$



(a)

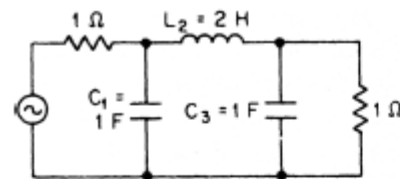


(b)

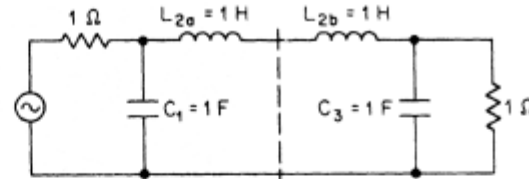
Impedance-scaled filters using $Z=1K$: (a) LC filter; (b) active filter.

Bartlett's Bisection Theorem

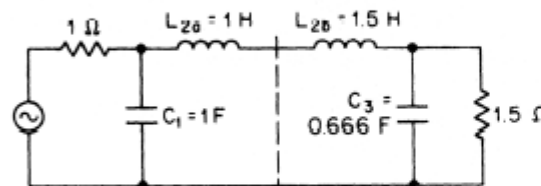
A passive network designed to operate between two equal terminations can be modified to work between two unequal terminations and still have the same Transfer Function (except for a constant multiplier) if the network is symmetrical. It can then be bisected and either half scaled in impedance.



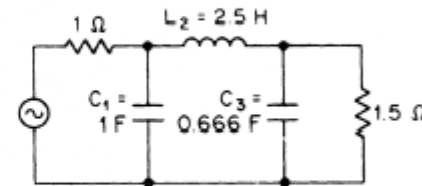
(a) Normalized N=3 LPF



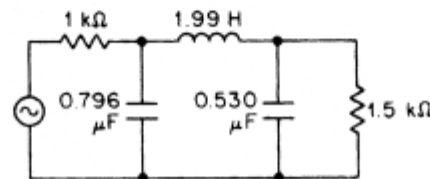
(b) Bisected LPF



Right half impedance scaled by 1.5



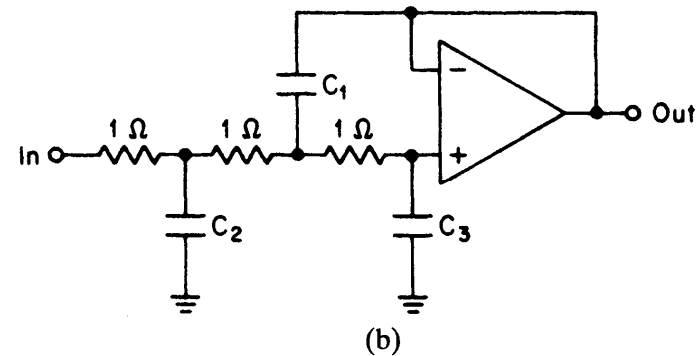
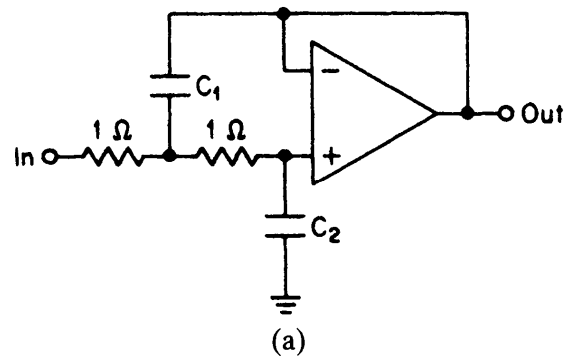
Re-combined LPF



(e)

Resulting filter frequency and impedance scaled to 200Hz, 1K Source, 1.5K Load

Active Low-Pass Filters



Unity gain Active Low-Pass N=2 and N=3

N=2 Section

$$T(s) = \frac{1}{C_1 C_2 s^2 + 2C_2 s + 1}$$

$$T(s) = \frac{1}{\frac{1}{\alpha^2 + \beta^2} s^2 + \frac{2\alpha}{\alpha^2 + \beta^2} s + 1}$$

$$C_1 = \frac{1}{\alpha} \quad C_2 = \frac{\alpha}{\alpha^2 + \beta^2}$$

N=3 Section

$$T(S) = \frac{1}{s^3 A + s^2 B + sC + 1}$$

$$A = C_1 C_2 C_3$$

$$B = 2C_3(C_1 + C_2)$$

$$C = C_2 + 3C_3$$

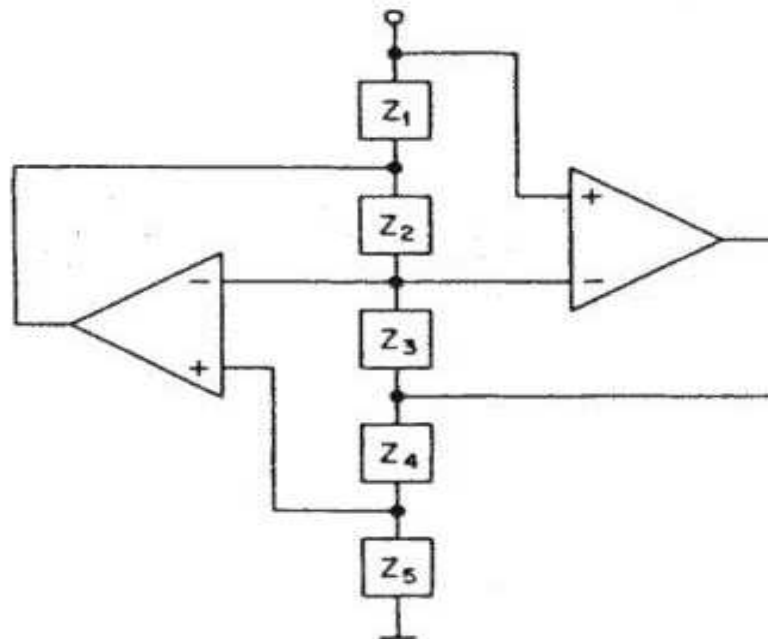
Values can be frequency and Impedance scaled

Design of D-Element Active Low-Pass Filters and a Bi-Directional Impedance Converter for Resistive Loads

Generalized Impedance Converters (GIC)

$$Z_{11} = \frac{Z_1 Z_3 Z_5}{Z_2 Z_4}$$

By substituting RC combinations for Z_1 through Z_5 a variety of impedances can be realized.



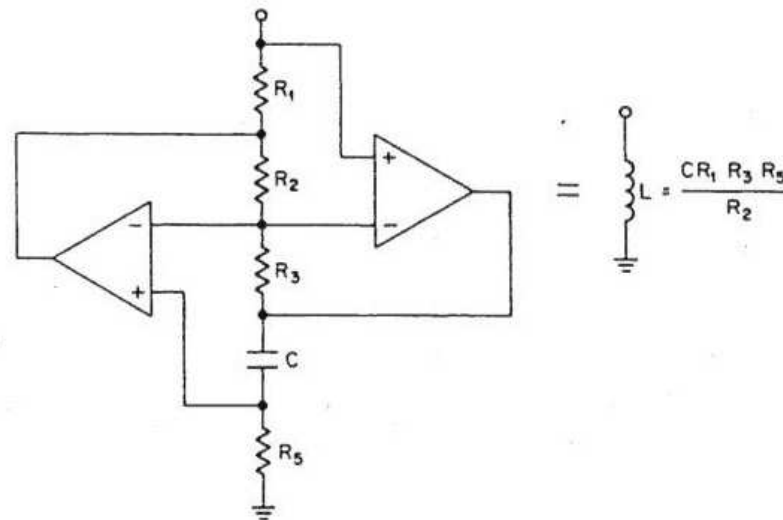
GIC Inductor Simulation

If Z_4 consists of a capacitor having an impedance $1/sC$ where $s=j\omega$ and all other elements are resistors, the driving point impedance becomes:

$$Z_{11} = \frac{sCR_1R_3R_5}{R_2}$$

The impedance is proportional to frequency and is therefore identical to an inductor having an inductance of:

$$L = \frac{CR_1R_3R_5}{R_2}$$



Note: If R_1 and R_2 and part of a digital potentiometer the value of L can be digitally programmable.

D Element

If both Z_1 and Z_3 are capacitors C and Z_2, Z_4 and Z_5 are resistors, the resulting driving point impedance becomes:

$$Z_{11} = \frac{R_5}{s^2 C^2 R_2 R_4}$$

An impedance proportional to $1/s^2$ is called a D Element.

$$Z_{11} = \frac{1}{s^2 D} \quad \text{where:} \quad D = \frac{C^2 R_2 R_4}{R_5}$$

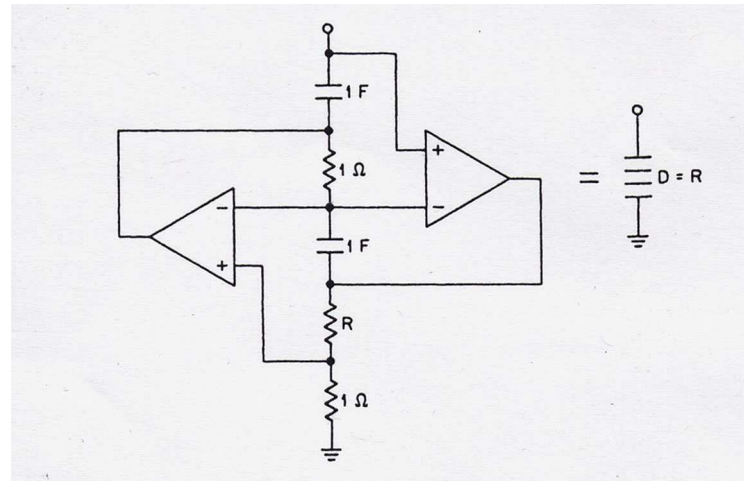
If we let $C=1F, R_2=R_5=1 \Omega$ and $R_4=R$ we get $D=R$ so:

$$Z_{11} = \frac{1}{s^2 R}$$

If we let $s=j\omega$ the result is a Frequency Dependant Negative Resistor FDNR

$$Z_{11} = \frac{1}{-\omega^2 R}$$

D Element Circuit

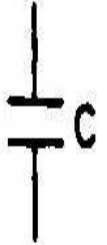
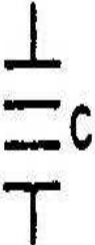
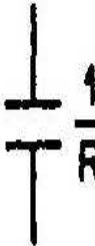


Rule

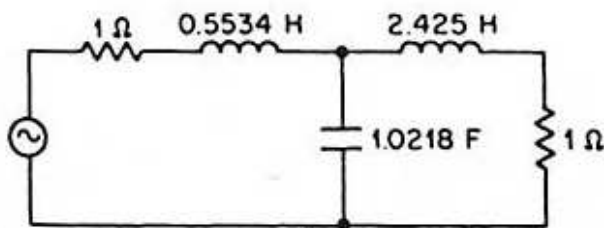
A transfer function of a network remains unchanged if all impedances are multiplied (or divided) by the same factor. This factor can be a fixed number or a variable, as long as every impedance element that appears in the transfer function is multiplied (or divided) by the same factor.

The $1/S$ transformation involves multiplying all impedances in a network by $1/S$.

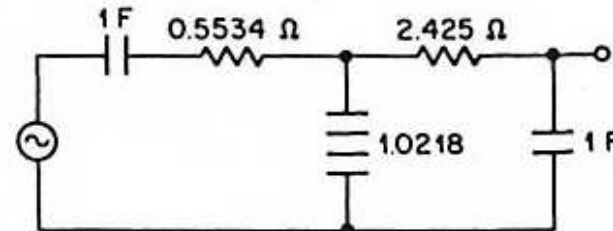
The 1/S Transformation

Element	Impedance	Transformed Element	Transformed Impedance
 L	sL	 L	L
 C	$\frac{1}{sC}$	 C	$\frac{1}{s^2C}$
 R	R	 $\frac{1}{R}$	$\frac{R}{s}$

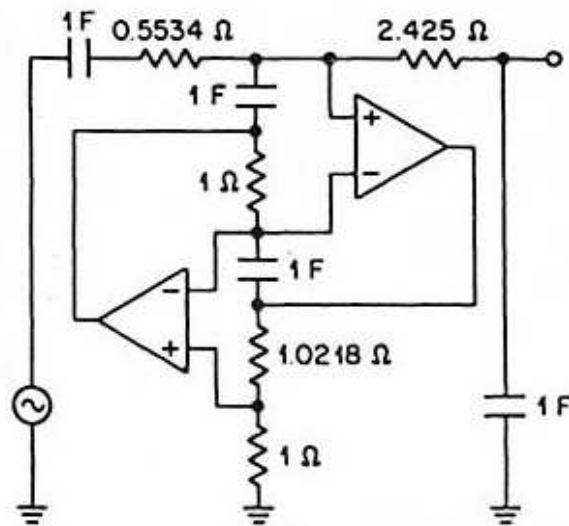
Design of Active Low-Pass filter with 3dB point at 400Hz using D Elements



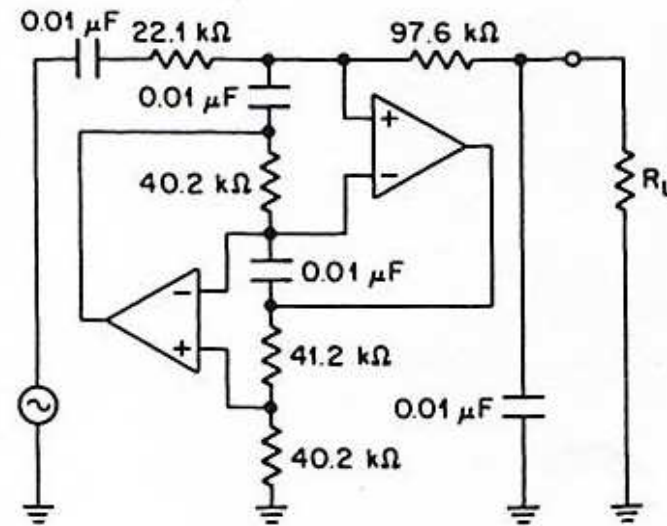
(a) Normalized Low-Pass filter



(b) 1/S Transformation



(c) Realization of D Element



(d)

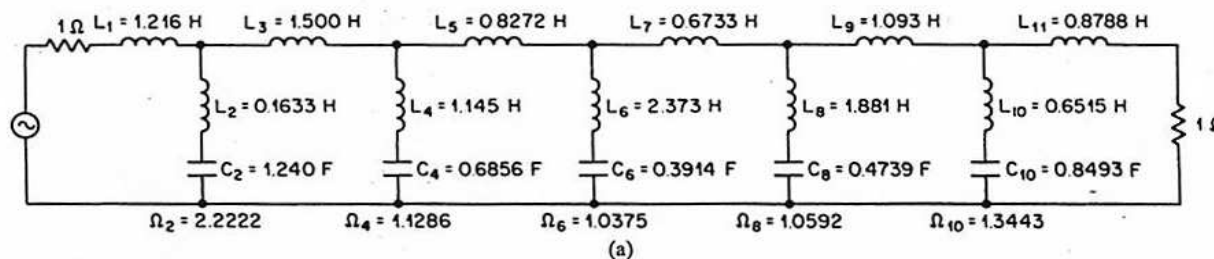
Frequency and Impedance Scaled Final Circuit

Filter is Linear Phase $\pm 0.5^\circ$ Type

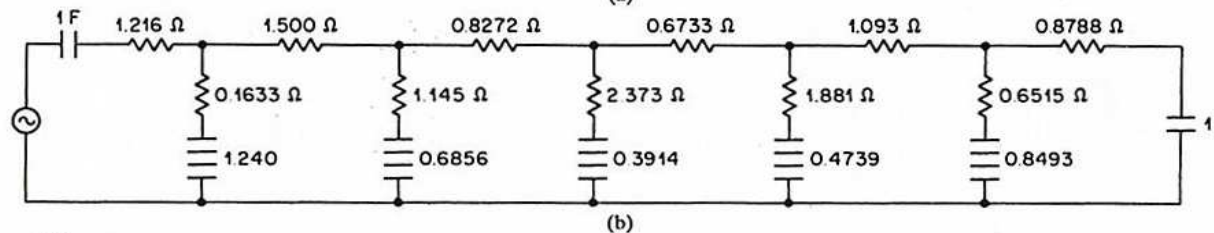
Elliptic Function Low-Pass filter using GICs

Requirements: 0.5dB Maximum at 260Hz
60dB Minimum at 270Hz
Steepness factor=1.0385

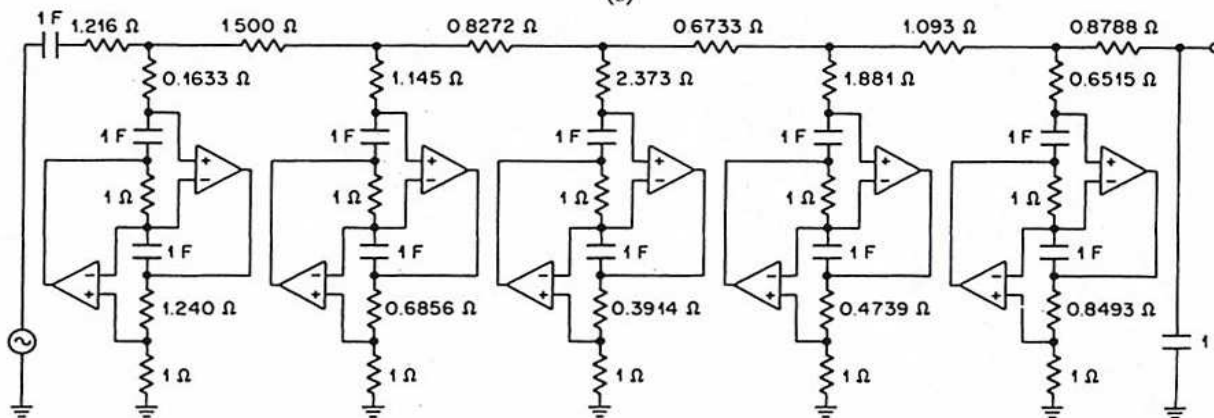
Normalized Elliptic Function Filter
C11 20 0=75°
N=11 $R_{db}=0.18\text{dB}$ $\Omega_s=1.0353$ 60.8dB



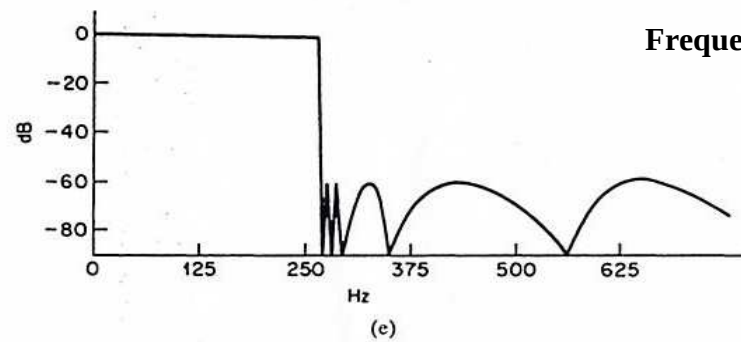
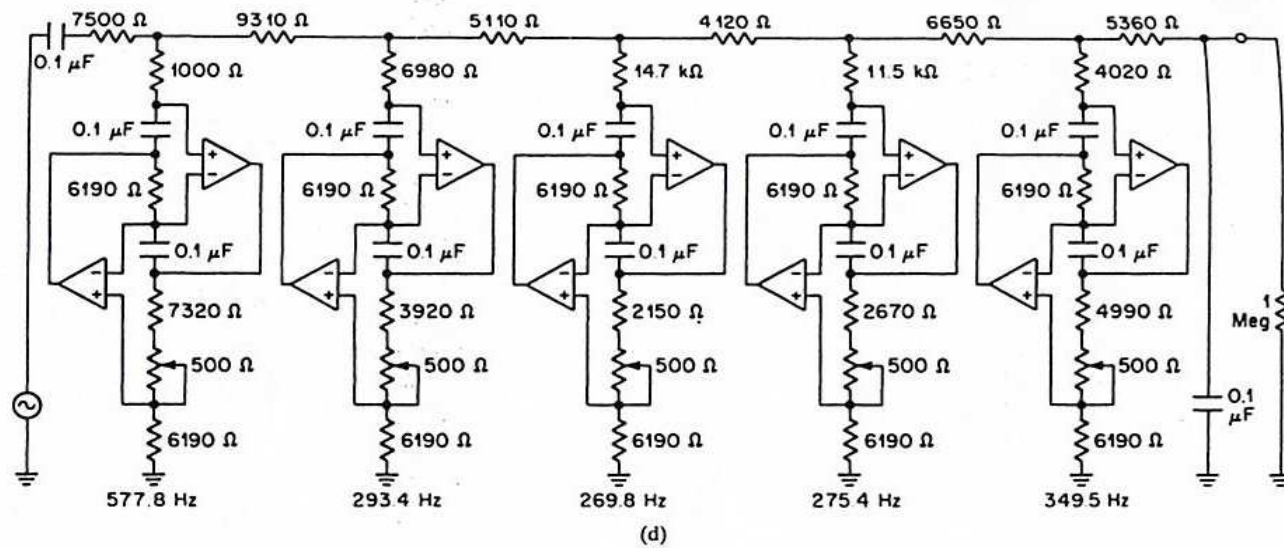
Normalized
Elliptic Function Filter



1/S Transformation



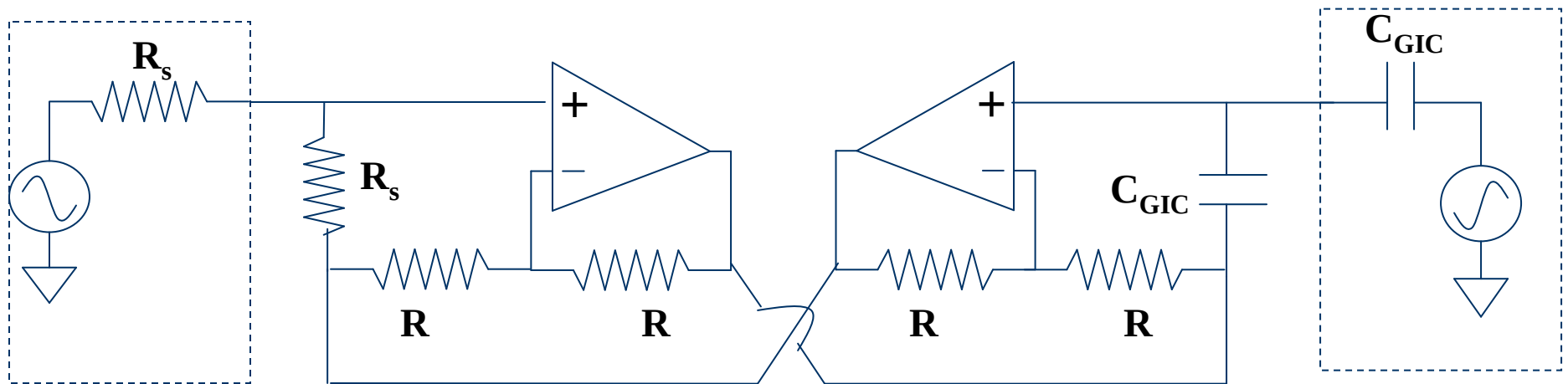
Realization of D Elements



Frequency and Impedance Scaled Final Circuit

Note: 1 meg termination resistor is needed to provide DC return path.

Bi-Directional Impedance Converter for Matching D Element Filters Requiring Capacitive Loads to Resistive Terminations

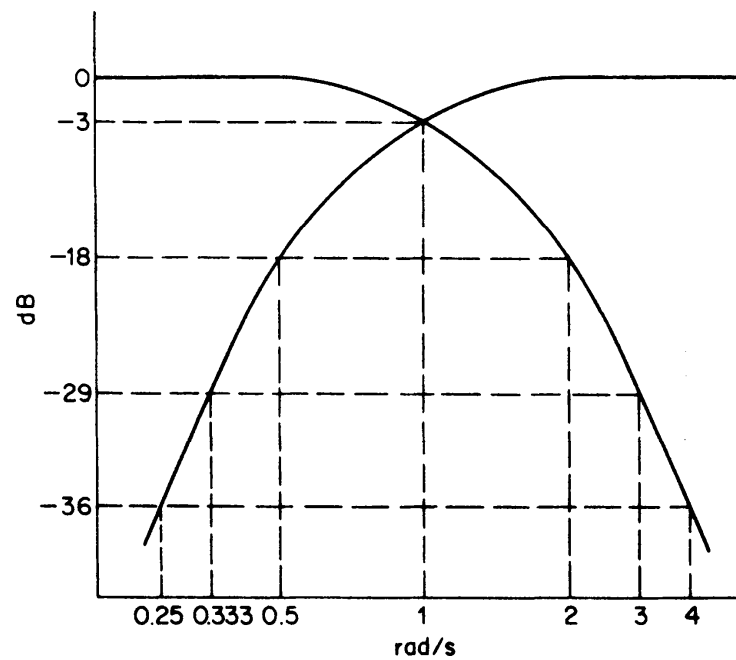


Value of R Arbitrary

R_s is source and load resistive terminations

C_{GIC} is D Element Circuit Capacitive Terminations

High-Pass Filters

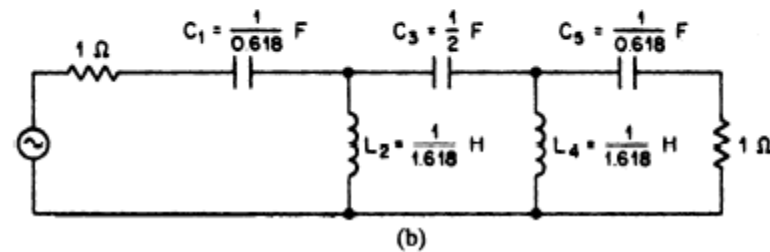
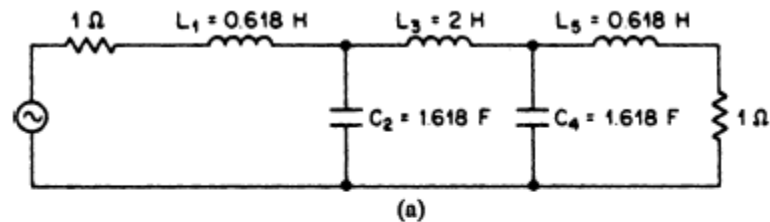


Normalized Reciprocal Low-Pass High-Pass Relationship

Passive High-Pass Filters

Low-Pass to High-Pass Transformation for Normalized Values

$$C_{hp} = \frac{1}{L_{LP}} \qquad L_{hp} = \frac{1}{C_{LP}}$$

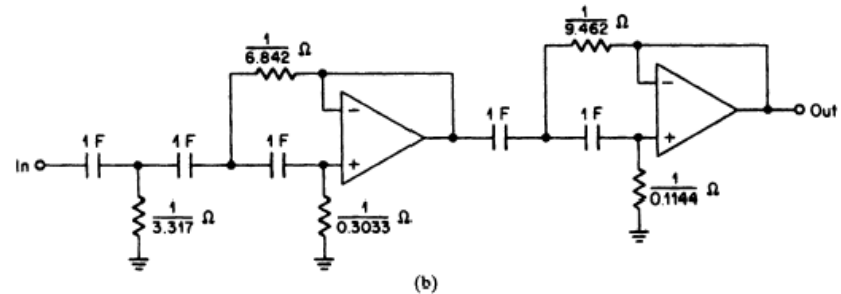
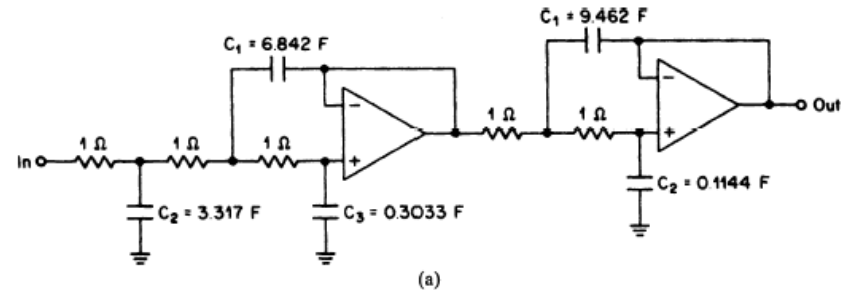


Replace Low-Pass Values by Reciprocal Components
Then frequency and impedance scale to desired cut-off

Active High-Pass Filters

$$C_{hp} = \frac{1}{R_{lp}}$$

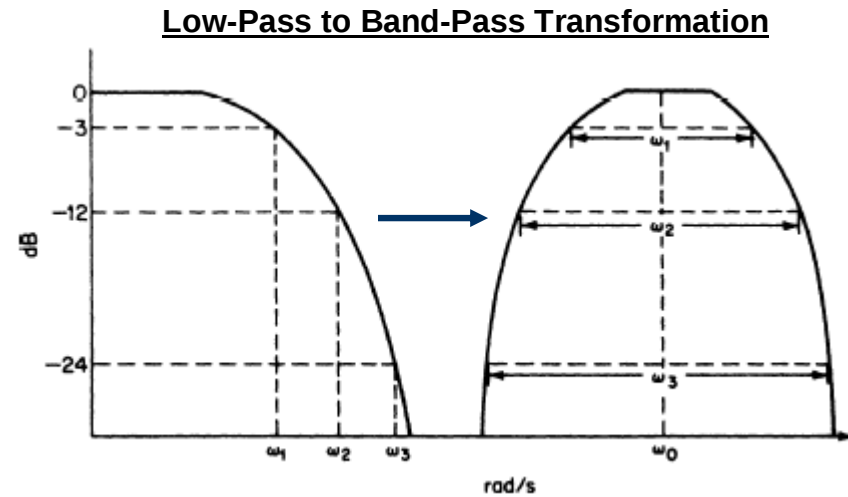
$$R_{hp} = \frac{1}{C_{lp}}$$



To convert a normalized active low-pass filter into an active high-pass filter replace each resistor by a capacitor having the reciprocal value and vice versa. The filter can then be scaled to the desired cut-off and impedance level.

This conversion does not apply to feedback resistors that determine an amplifiers gain which applies to some active configurations.

Band-Pass Filters

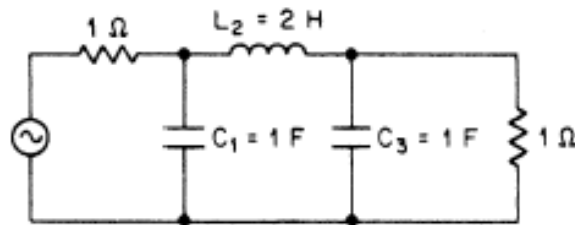


This figure shows the relationship of a low-pass filter when transformed into a band-pass filter. The response at frequencies of the low-pass filter results in the same attenuation at corresponding bandwidths of the band-pass filter.

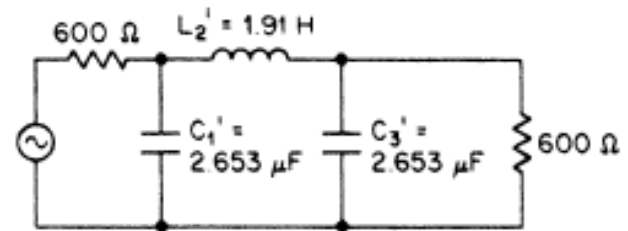
Band-Pass Filters

Band-Pass Transformation Procedure for LC Filters

- 1) Design a low-pass filter having the desired Bandwidth of the band-pass filter and impedance level.
- 2) Resonate each inductor with a series capacitor and resonate each capacitor with a parallel inductor. The resonant frequency should be the desired center frequency of the band-pass filter.

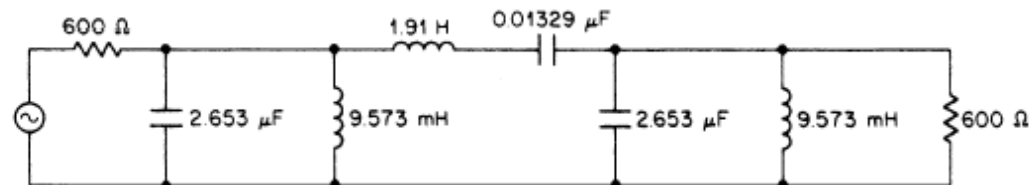


Normalized N=3 Butterworth Low-Pass Filter



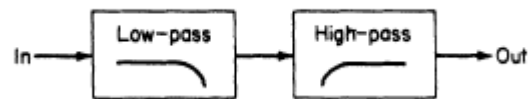
Scaled to 3dB at 100Hz and 600-ohms

$$F_o = \frac{1}{2 \pi \sqrt{LC}}$$

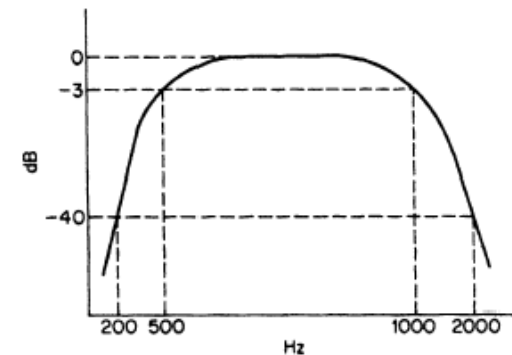


Resulting Band-Pass Transformation

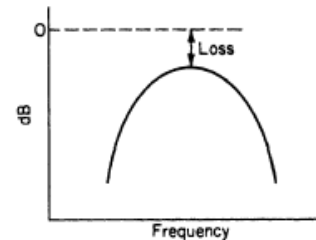
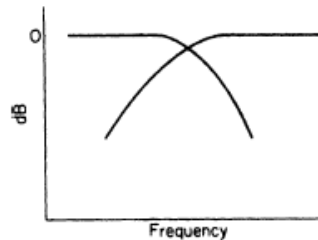
Wide Band Band-Pass Filters



Cascade of Low-Pass and High-Pass



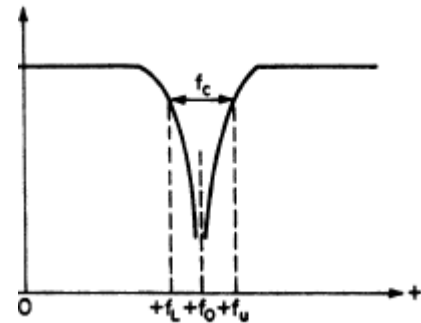
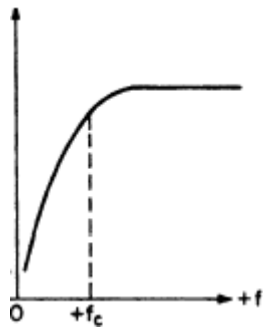
Example of Wide Band Band-Pass Filter



Effect of Interaction for Less Than an Octave of Separation of Cut-Offs

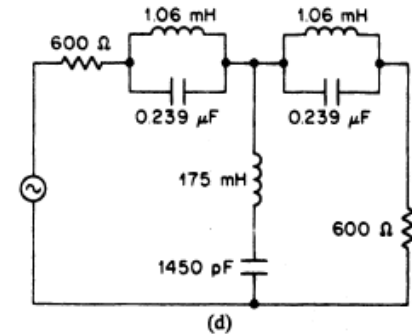
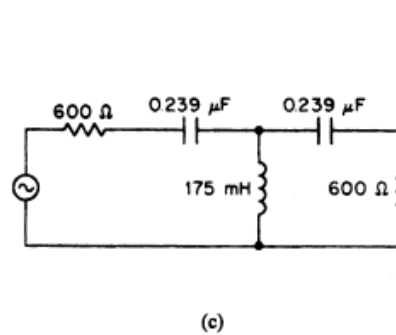
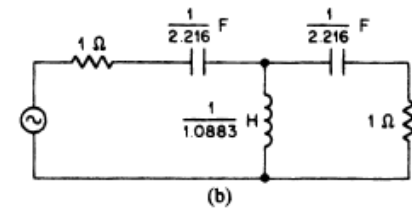
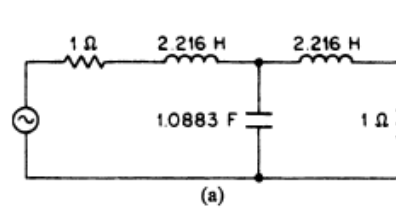
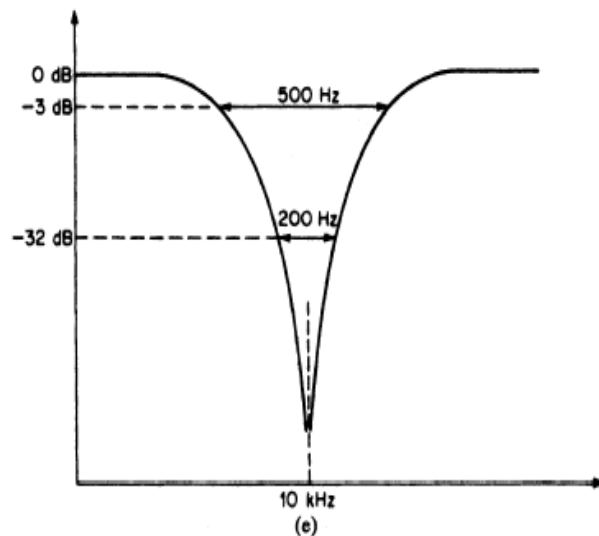
To prevent impedance interaction between a passive low-pass filter and high-pass filter, a 3dB Attenuator between filters is helpful.

Band Reject Filters



This figure shows the relationship of a high-pass filter when transformed into a band-reject filter. The response at frequencies of the high-pass filter results in the same attenuation at corresponding bandwidths of the band-reject filter.

Band-Reject Filters

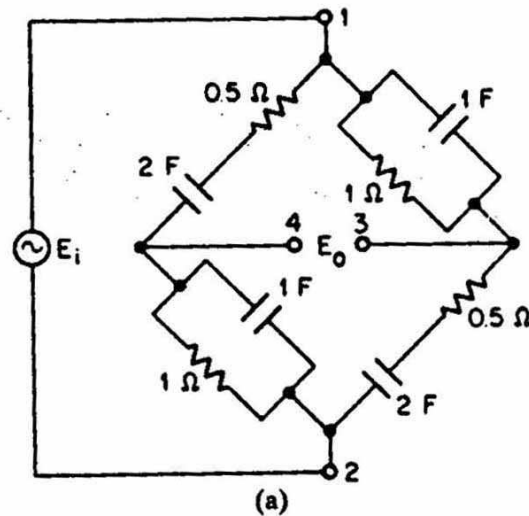


- a) N=3 Normalized 1dB Chebyshev LPF
- b) Transformed HPF
- c) Frequency and Impedance Scaled HPF (500Hz BW)
- d) Resonate inductors and capacitors
- e) Resulting Response

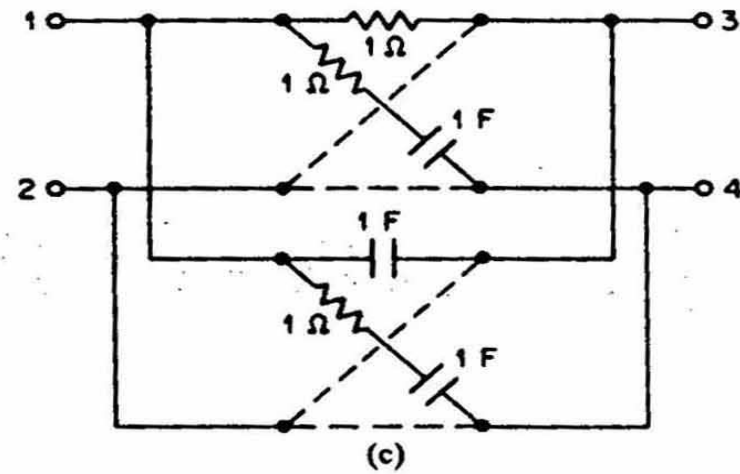
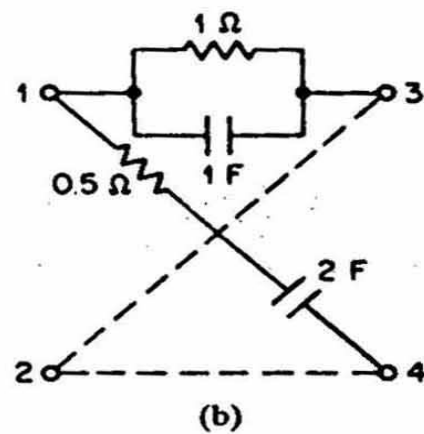
Band-Reject Transformation Procedure for LC Filters

- 1) Design a high-pass filter having the desired Bandwidth of the band-reject filter and impedance level.
- 2) Resonate each inductor with a parallel capacitor and resonate each capacitor with a series inductor. The resonant frequency should be the desired center frequency of the band-reject filter.

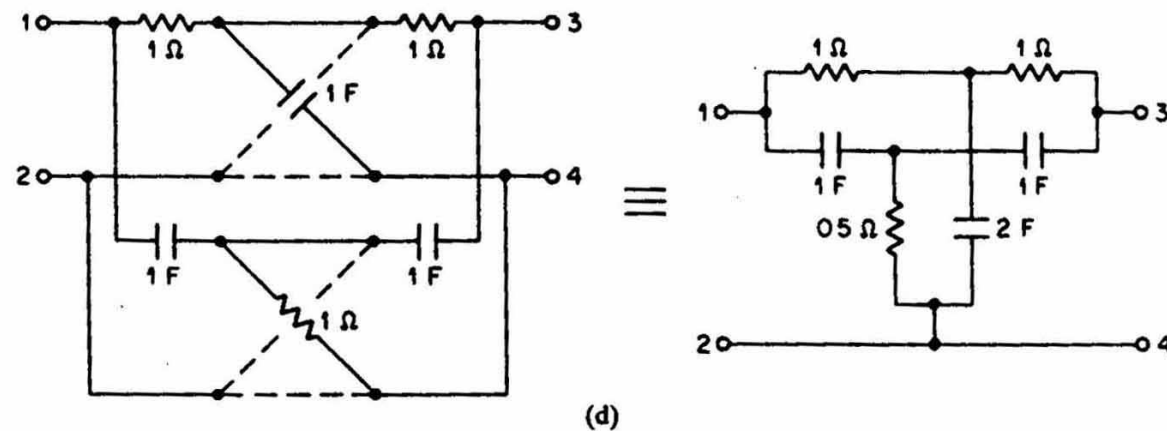
High-Q Notch Filters



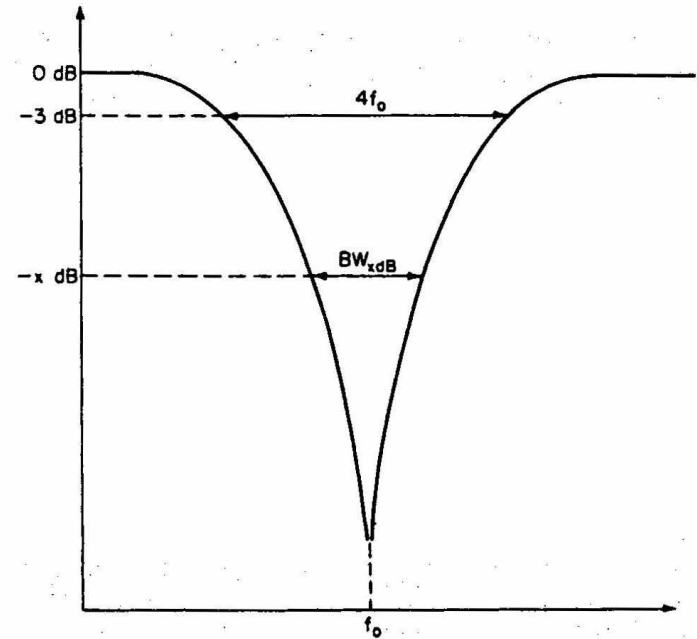
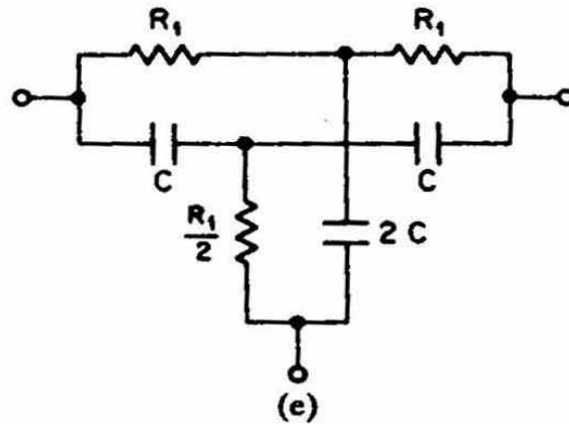
This circuit is in the form of a bridge where a signal is applied across terminals' 1 and 2 the output is measured across terminals' 3 and 4. At $\omega=1$ all branches have equal impedances of $0.707 \angle -45^\circ$ so a null occurs across the output.



The circuit is redrawn in figure B in the form of a lattice. Circuit C is the Identical circuit shown as two lattices in parallel.



There is a theorem which states that any branch in series with both the Z_A and Z_B branches of a lattice can be extracted and placed outside the lattice. The branch is replaced by a short. This is shown in figure D above. The resulting circuit is known as a Twin-T. This circuit has a null at 1 radian for the normalized values shown.

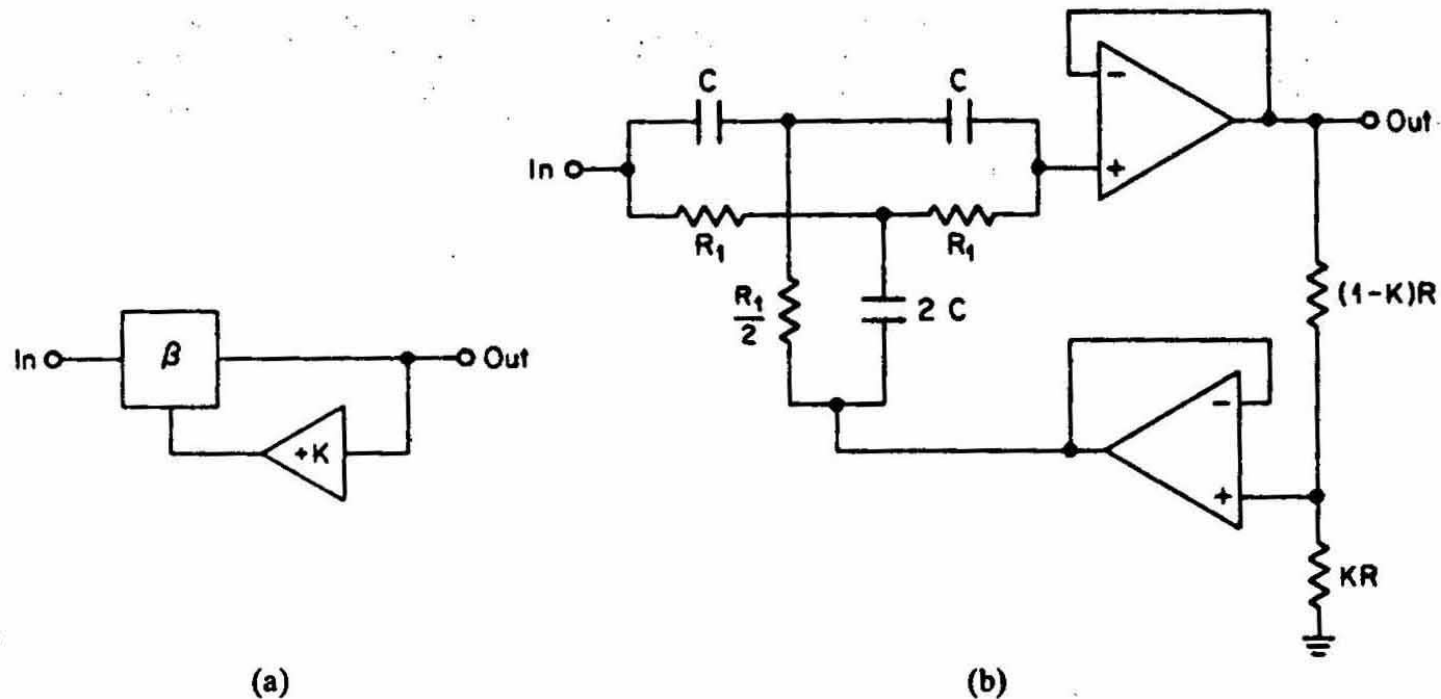


To calculate values for this circuit pick a convenient value for C. Then

$$R_1 = \frac{1}{2\pi f_0 C}$$

The Twin-T has a Q (f_0/BW_{3dB}) of only $1/4$ which is far from selective.

Note: R-source $\ll R_1$ R-load $\gg R_1$

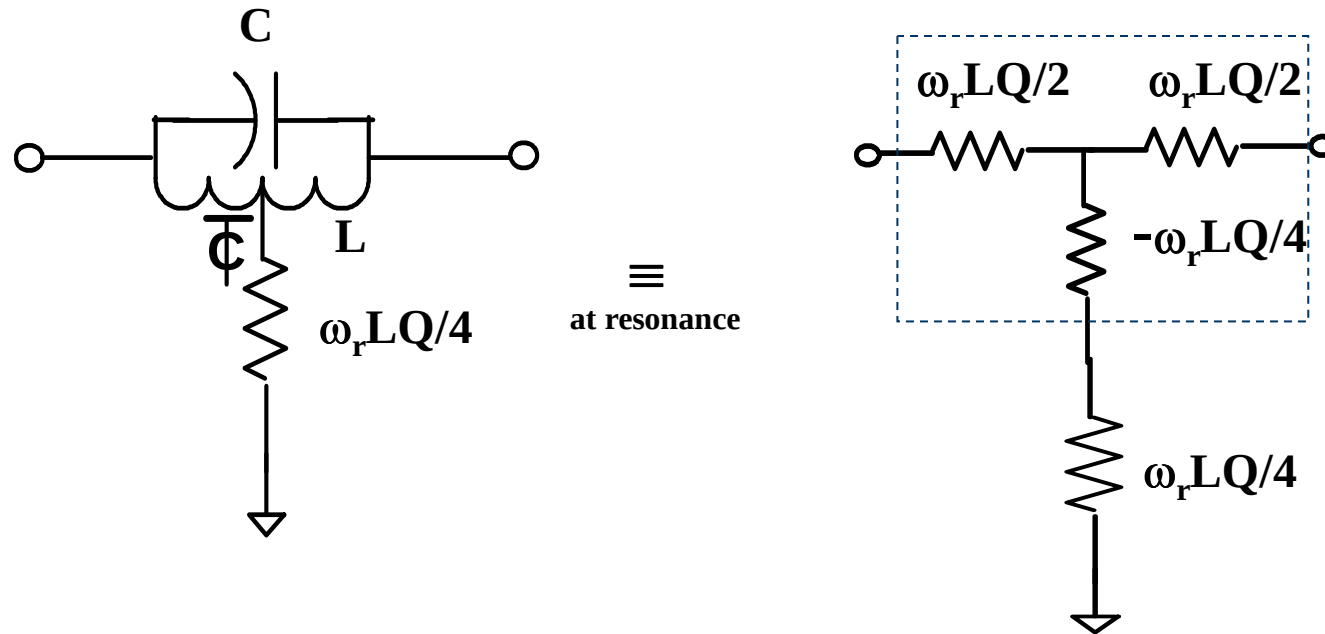


Circuit A above illustrates bootstrapping a network β with a factor K . If β is a twin-T the resulting Q becomes:

$$Q = \frac{1}{4(1-K)}$$

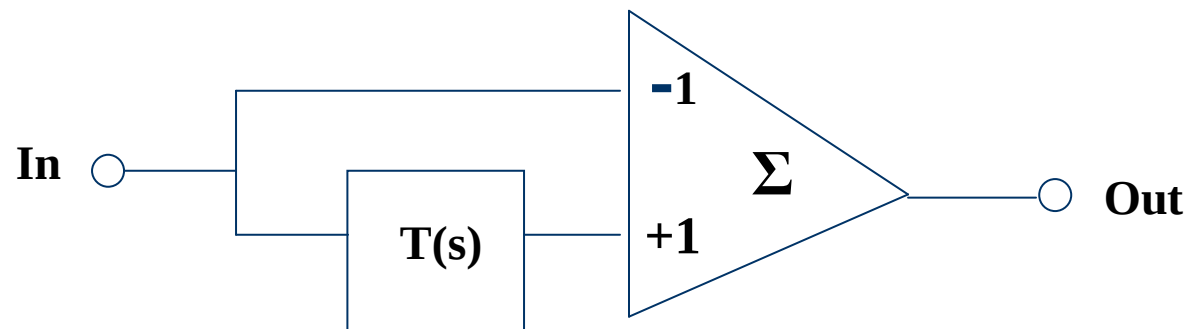
If we select a positive $K < 1$, and sufficiently close to 1, the circuit Q can be dramatically increased. The resulting circuit is shown in figure B.

Bridged-T Null Network



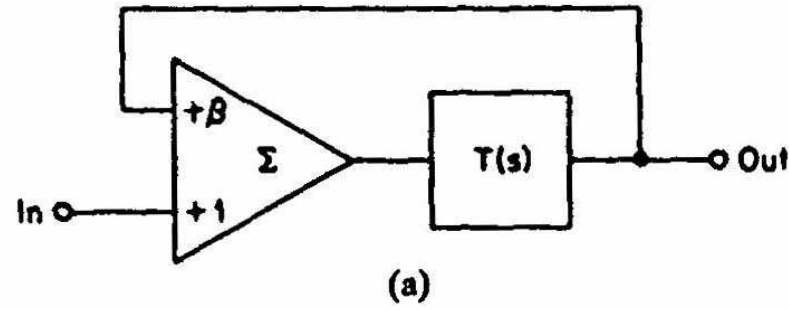
Impedance of a center-tapped parallel resonant circuit at resonance is $\omega_r LQ$ total and $\omega_r LQ/4$ from end to center tap (due to N^2 relationship). Hence a phantom negative resistor of $-\omega_r LQ/4$ appears in the equivalent circuit which can be cancelled by a positive resistor of $\omega_r LQ/4$ resulting in a very deep null at resonance (60dB or more).

Adjustable Q and Frequency Null Network



$T(s)$ can be any band-pass circuit having properties of unity gain at f_r , adjustable Q and adjustable f_r .

Q Multiplier Active Bandpass Filters



If $T(s)$ in circuit A corresponds to a band-pass transfer function of:

$$T(s) = \frac{\frac{\omega_r}{Q} s}{s^2 + \frac{\omega_r}{Q} s + \omega_r^2}$$

The overall circuit transfer function becomes:

$$\frac{\text{Out}}{\text{In}} = \frac{\frac{\omega_r}{Q} s}{s^2 + \frac{\omega_r}{Q} s + \omega_r^2} \cdot \frac{Q}{1 - \beta}$$

The middle term of the denominator has been modified so the circuit Q is given by $Q/(1-\beta)$ where $0 < \beta < 1$. The Q can then be increased by the factor $1/(1-\beta)$. Note that the circuit gain is increased by the same factor.

A simple implementation of this circuit is shown in figure B.

The design equations are:

First calculate β from $\beta = 1 - \frac{Q_r}{Q_{eff}}$

where Q_{eff} is the overall circuit Q and Q_r is the design Q of the bandpass section.

The component values can be computed from:

$$R_3 = \frac{R}{\beta}$$

$$R_2 = \frac{Q_r}{\pi f_r C}$$

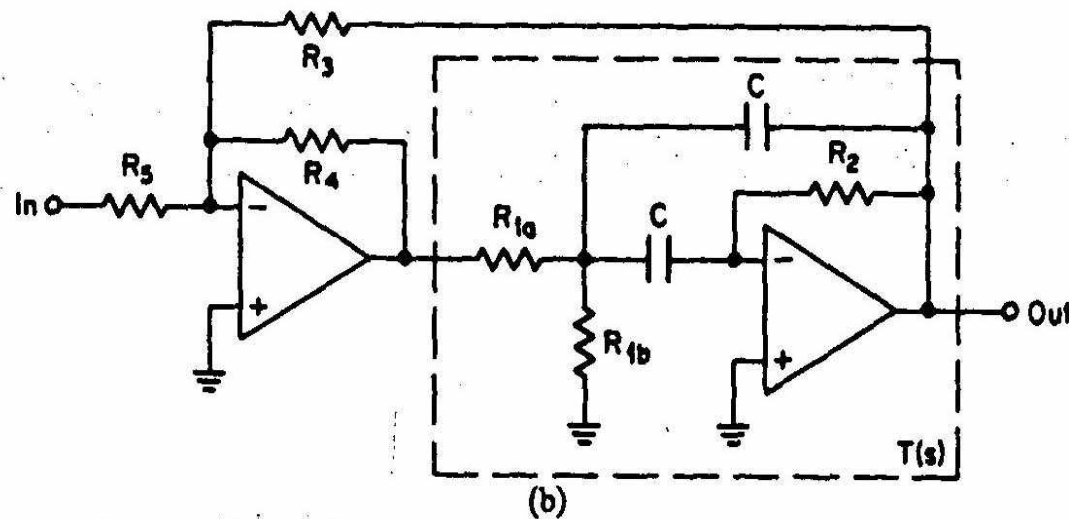
$$R_{1b} = \frac{R_{1a}}{2Q_r^2 - 1}$$

$$R_4 = R$$

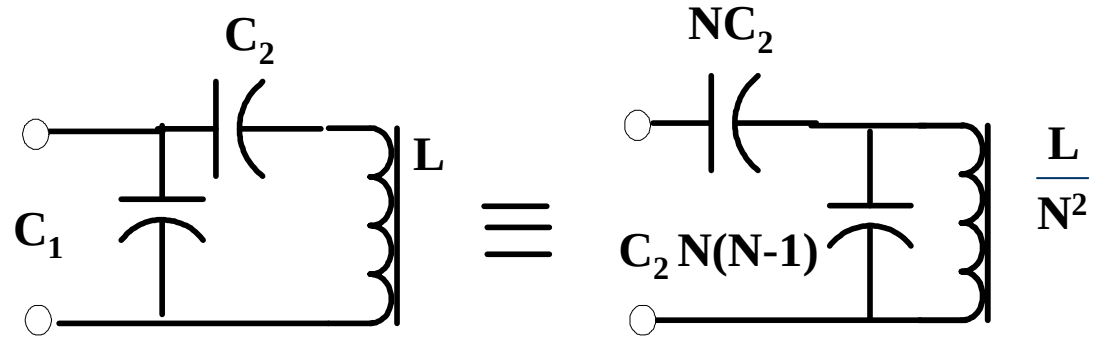
$$R_{1a} = \frac{R_2}{2}$$

$$R_5 = \frac{R}{(1 - \beta)A_r}$$

Where R and C can be conveniently chosen.



Some Useful Passive Filter Transformations to Improve Realizability

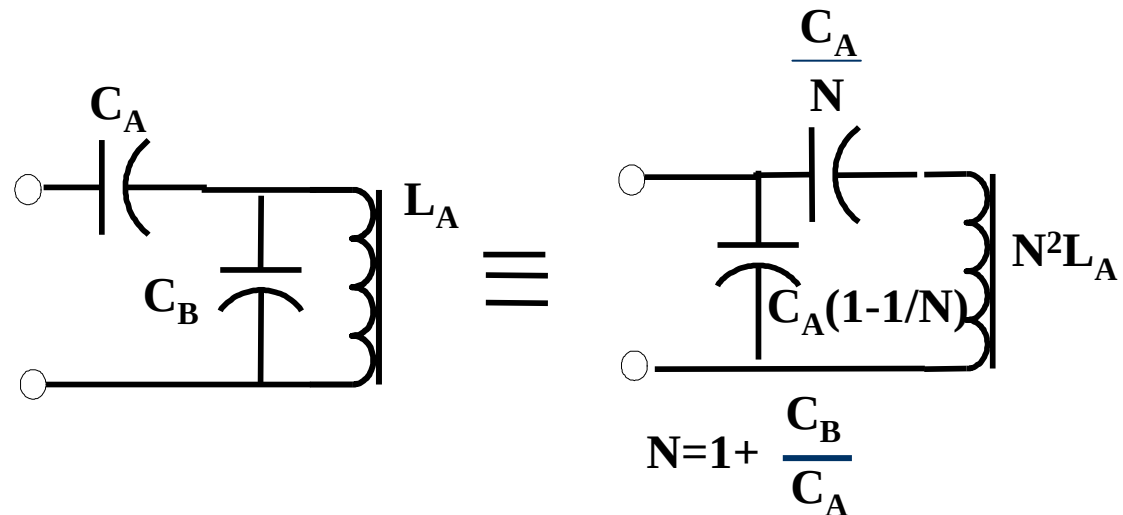


Advantages :

Reduces value of L

Allows for parasitic capacity across inductor

$$N = 1 + \frac{C_1}{C_2}$$

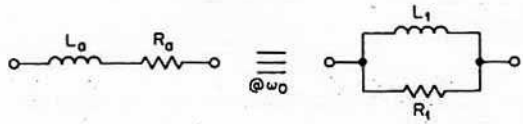
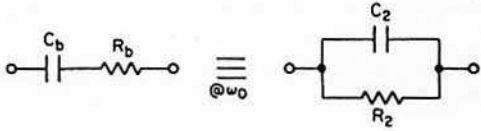


Advantages:

Increases value of L

$$N = 1 + \frac{C_B}{C_A}$$

Narrow Band Approximations

Circuit	Design Equations
	$L_1 = L_a + \frac{R_a^2}{\omega_0^2 L_a}$ $R_1 = R_a + \frac{\omega_0^2 L_a^2}{R_a}$ $L_a = \frac{L_1 R_1^2}{R_1^2 + \omega_0^2 L_1^2}$ $R_a = \frac{\omega_0^2 L_1^2 R_1}{R_1^2 + \omega_0^2 L_1^2}$
	$C_2 = \frac{C_b}{1 + \omega_0^2 C_b^2 R_b^2}$ $R_2 = R_b + \frac{1}{\omega_0^2 C_b^2 R_b}$ $C_b = C_2 + \frac{1}{\omega_0^2 R_2^2 C_2}$ $R_b = \frac{R_2}{1 + \omega_0^2 C_2^2 R_2^2}$

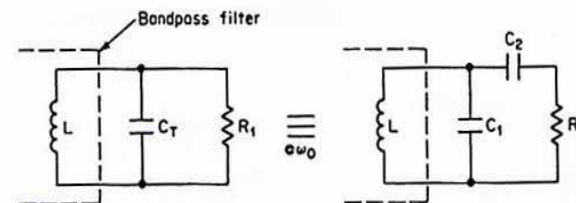
This transformation can be used to reduce the value of a terminating resistor and yet maintain the narrow-band response.

$$C_2 = \frac{1}{\omega_0 \sqrt{R_1 R_2 - R_2^2}}$$

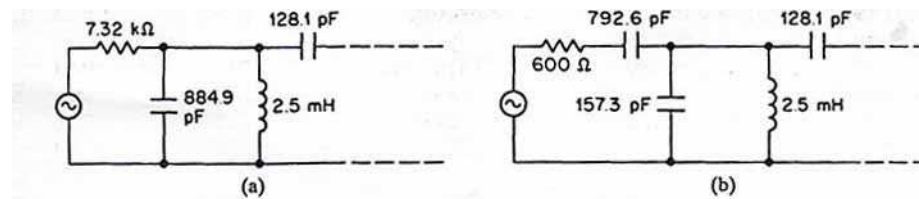
and

$$C_1 = C_T - \frac{1}{\omega_0} \sqrt{\frac{R_1 - R_2}{R_1^2 R_2}}$$

where the restrictions $R_2 < R_1$ and $(R_1 - R_2)/(R_1^2 R_2) < \omega_0^2 C_T^2$ apply.



The following example illustrates how this approximation can reduce the source impedance of a filter.



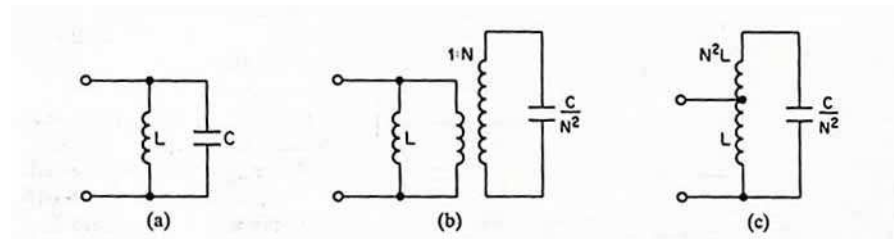
$$C_2 = \frac{1}{\omega_0 \sqrt{R_1 R_2 - R_2^2}} = \frac{1}{2\pi \times 10^5 \sqrt{7.32 \times 6 \times 10^3 - 600^2}}$$

$$= 792.6 \text{ pF}$$

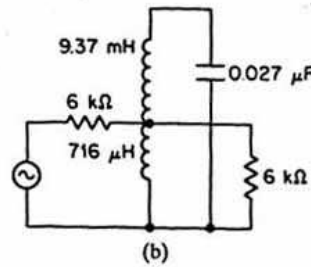
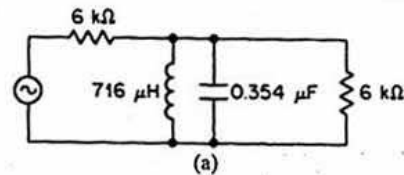
$$C_1 = C_T - \frac{1}{\omega_0} \sqrt{\frac{R_1 - R_2}{R_1^2 R_2}} = 884.9 \times 10^{-12}$$

$$- \frac{1}{2\pi \times 10^5} \sqrt{\frac{7.32 \times 10^3 - 600}{7320^2 \times 600}} = 157.3 \text{ pF}$$

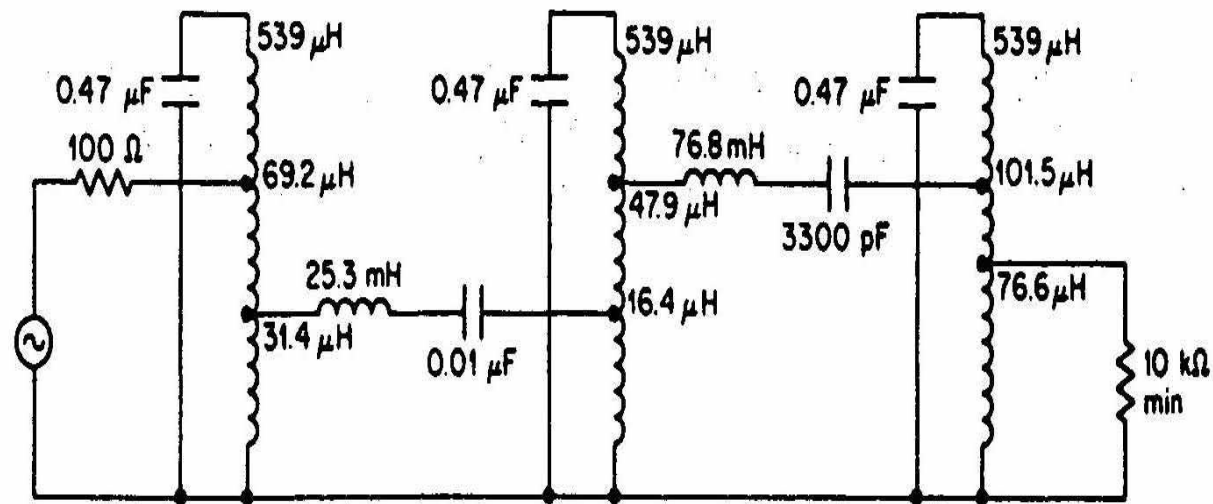
Using the Tapped Inductor



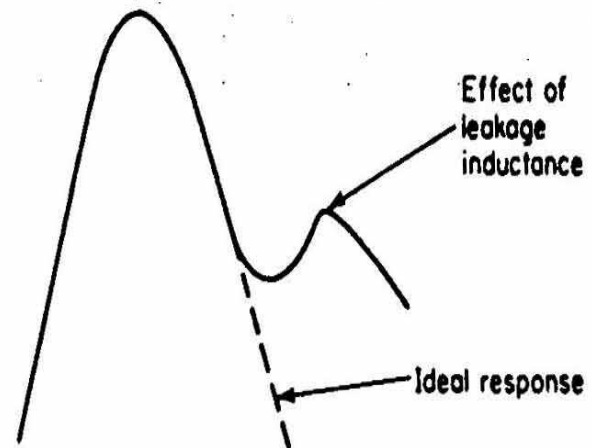
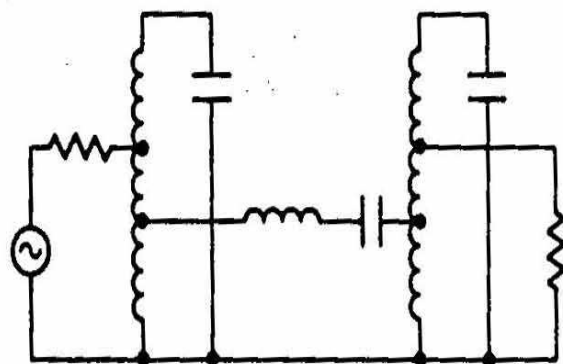
An inductor can be used as an auto-transformer by adding a tap



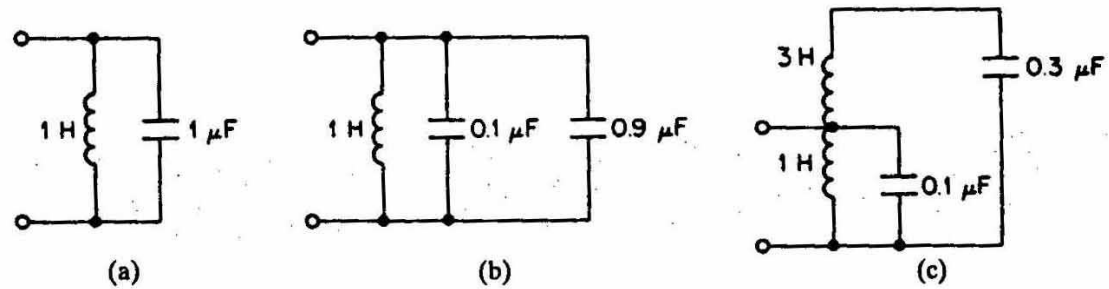
Resonant circuit capacitor values can be reduced



Intermediate branches can be scaled in impedance

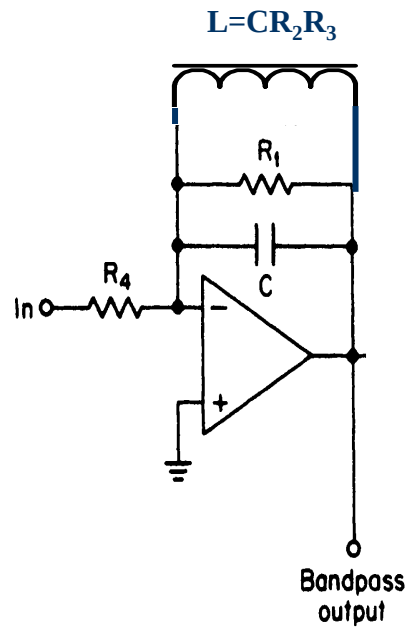
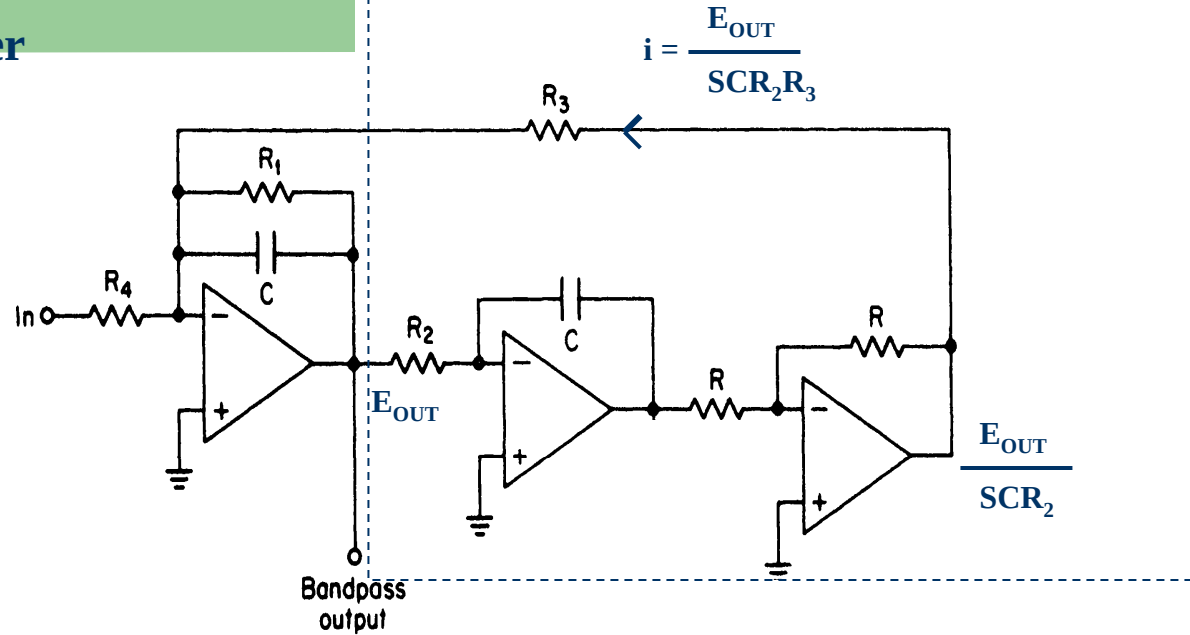


Leakage inductance can wreck havoc



Effect of leakage inductance can be minimized by splitting capacitors which adds additional poles

State Variable Bandpass Filter



$$Q = F_0 / 3\text{dbBW}$$

$$R_1 = 2\pi F_0 L Q$$

$$\text{Gain}@F_0 = -R_1/R_4$$

Attenuators

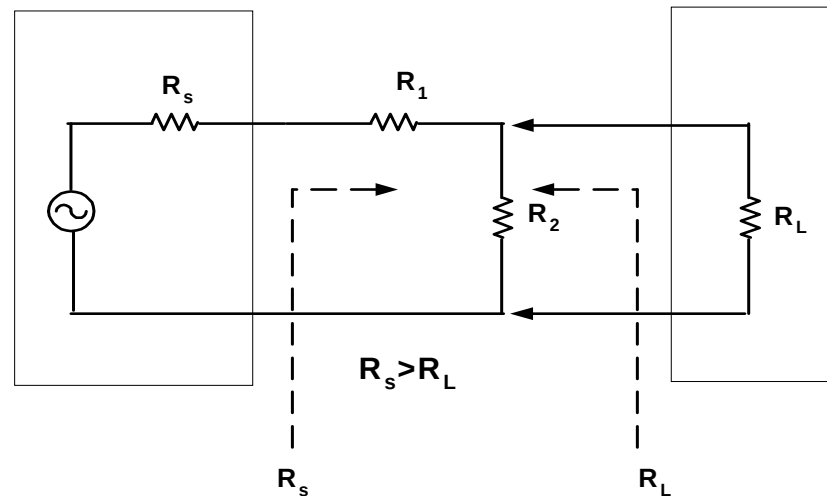
Minimum Loss Resistive Pad For Impedance Matching

$$R_1 = R_s \sqrt{1 - \frac{R_L}{R_s}}$$

$$R_2 = \frac{R_L}{\sqrt{1 - \frac{R_L}{R_s}}}$$

$$\text{Voltage Loss dB} = 20 \log_{10} \left(\frac{R_1(R_2 + R_L)}{R_2 R_L} + 1 \right)$$

$$\text{Power Loss dB} = \text{Voltage Loss dB} - 10 \log_{10} \frac{R_s}{R_L}$$

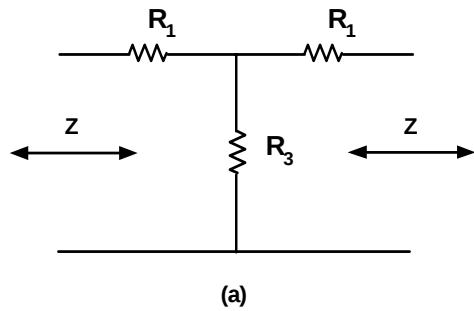


Symmetrical T and π Attenuators

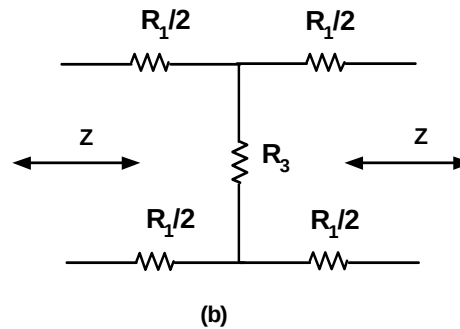
$$K = 10^{\text{dB}/20}$$

For a Symmetrical T Attenuator

$$R_1 = Z \frac{K-1}{K+1} \quad R_3 = \frac{2 Z K}{K^2 - 1}$$



Unbalanced

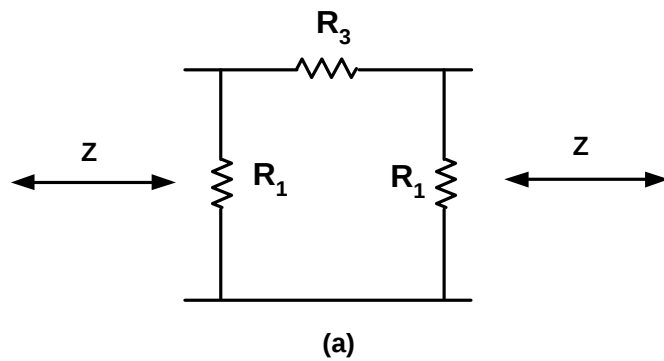


Balanced

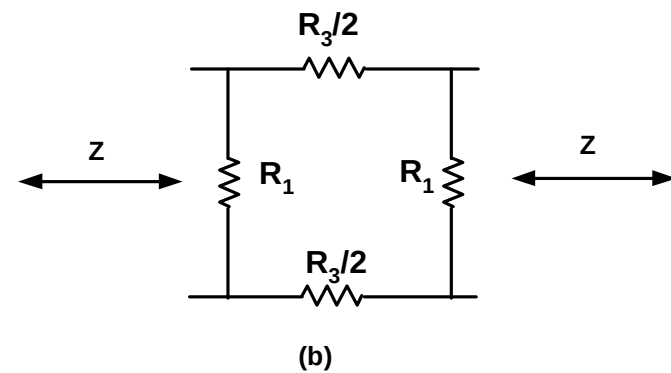
For a Symmetrical π Attenuator

$$R_1 = Z \frac{K+1}{K-1}$$

$$R_3 = Z \frac{K^2-1}{2K}$$



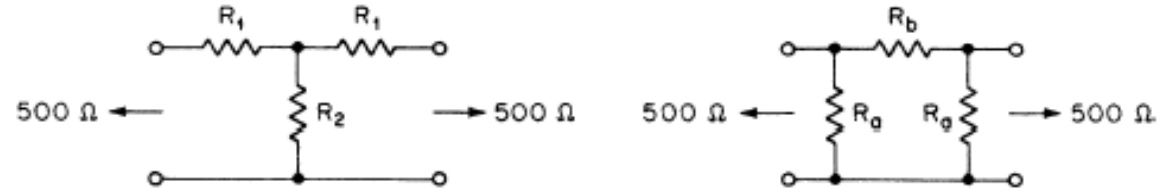
Unbalanced



Balanced

T and PI Attenuators at 500-ohms Impedance Level

Values can be scaled to other impedances



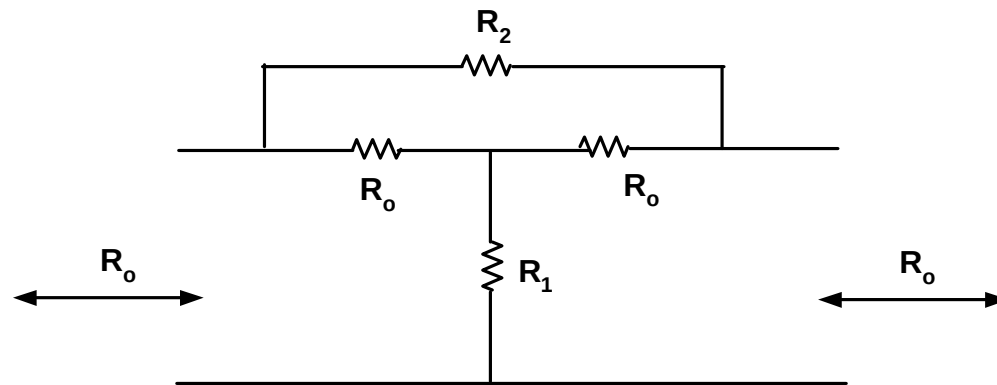
dB	R_1	R_2	R_a	R_b
1	28.8	4330	8700	57.7
2	57.3	2152	4362	116
3	85.5	1419	2924	176
4	113	1048	2210	239
5	140	822	1785	304
6	166	669	1505	374
7	191	558	1307	448
8	215	473	1161	528
9	238	406	1050	616
10	260	351	963	712

Bridged T Attenuator

$$R_1 = \frac{R_0}{K-1}$$

$$R_2 = R_0(K-1)$$

where $K = 10^{\text{dB}/20}$



Only R_1 and R_2 change to vary attenuation and they change inversely

Return Loss

$$A_{\rho} = 20 \log \left| \frac{Z_s + Z_x}{Z_s - Z_x} \right|$$

Z_s = standard or Ref Impedance
 Z_x = Impedance being Measured

If $Z_s = R_s$, then a symmetrical attenuator of X dB designed for an impedance of R_s preceding any network insures a minimum return loss of 2 X dB no matter what the impedance of the network, including zero or infinity (short or open).

For example a 3dB symmetrical attenuator insures a minimum Return Loss of 6dB even if terminated with a short or open.

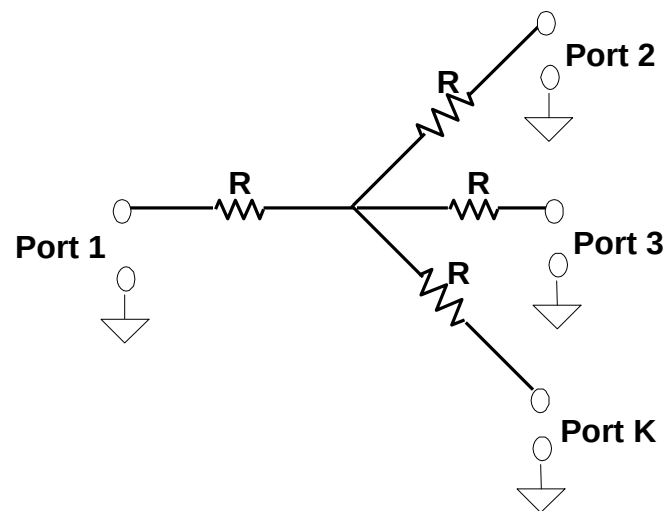
Resistive Power Splitter

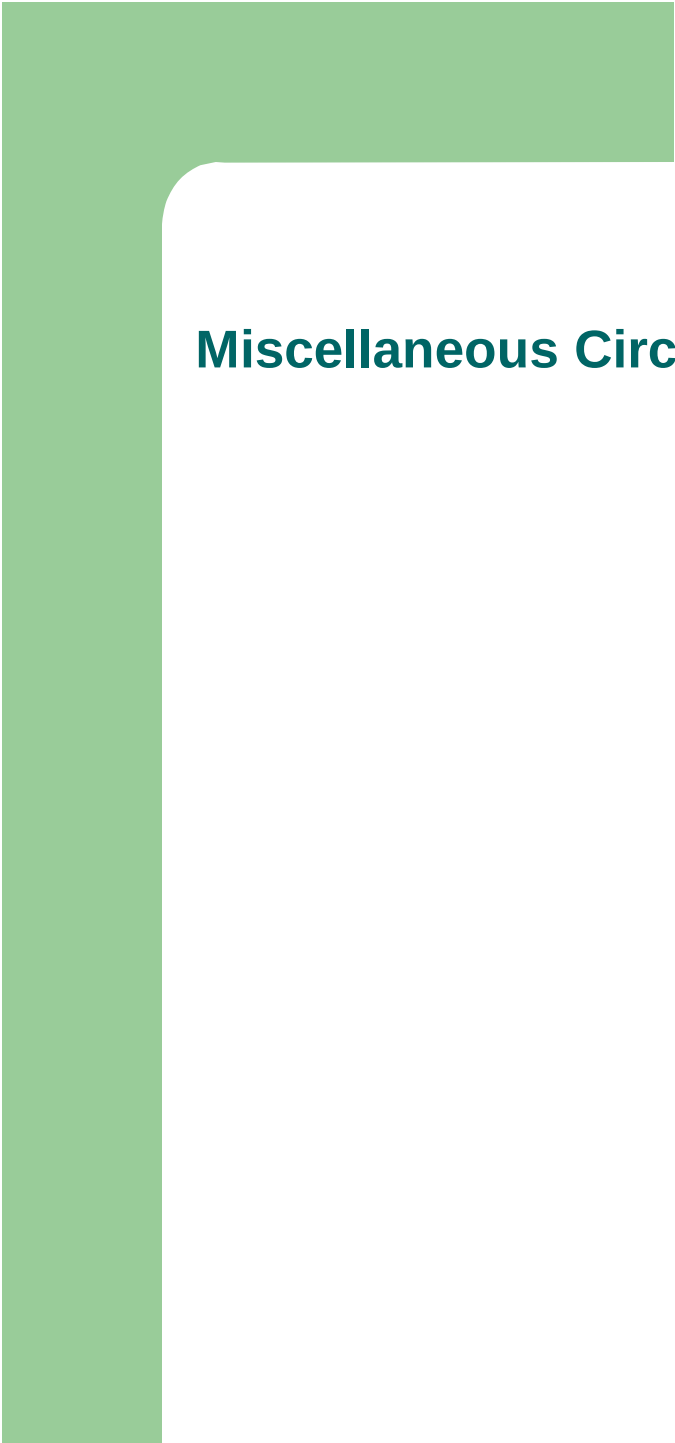
$N = \text{total number of ports} - 1 \quad (N=K-1)$

$$R = R_0 \frac{N-1}{N+1}$$

where R_0 is the impedance at all ports.

$$\text{Power Loss dB} = 10 \log_{10} \frac{1}{N^2}$$

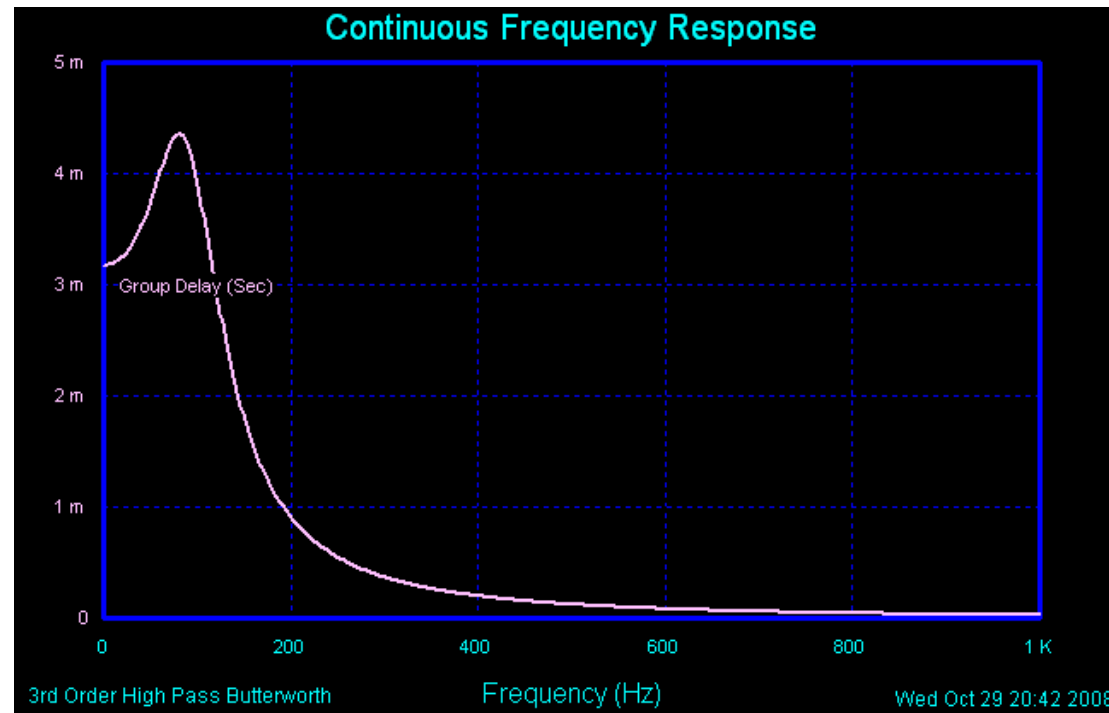




Miscellaneous Circuits and Topics

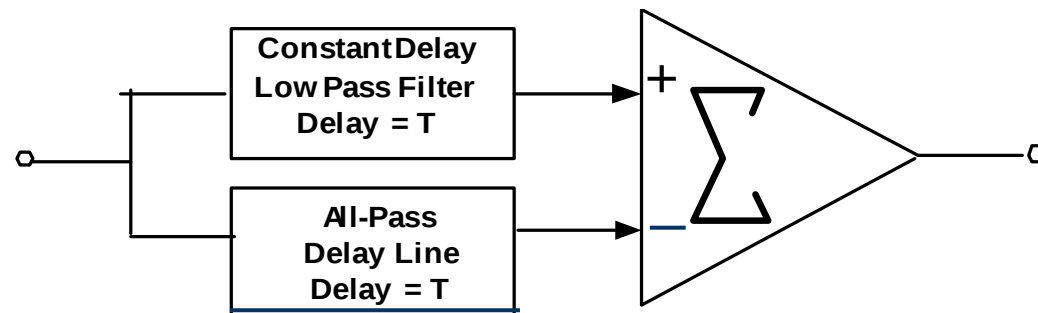
Constant Delay High Pass Filter

Delay of N=3 Butterworth High-Pass Filter
3dB at 100Hz



Delay peaks near 3dB Cutoff and approaches zero at higher frequencies
Not acceptable if constant delay is desired in the Pass-Band

Solution



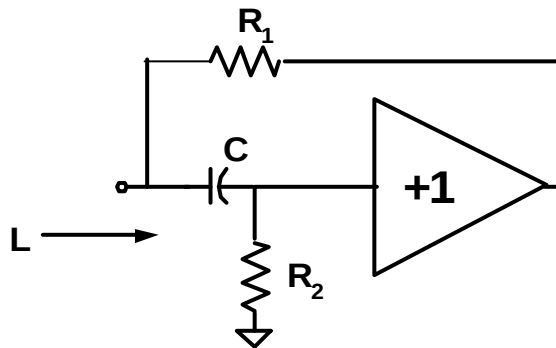
Low-Pass Filter has unity gain in stop-band

All-Pass Delay Line has unity gain

In pass-band of Low-Pass Filter signals are cancelled in summer by subtraction

In stop-band of Low-Pass Filter the signal path is through the delay line

Simple Active Shunt Inductor



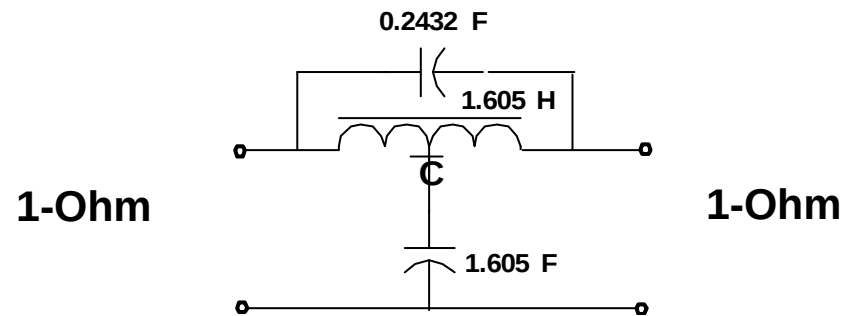
Let $R_2 \gg R_1$

$$L = R_1 R_2 C$$

$$F_{Q_{\max}} = \frac{1}{2 \pi C \sqrt{R_1 R_2}}$$

$$Q_{\max} = \frac{1}{2} \sqrt{\frac{R_2}{R_1}}$$

All-Pass Delay Line Section



Flat delay of 1.60 Sec within 1% to 1 Rad/S

$$N = \frac{2 \pi F T_{\text{total}}}{1.6}$$

Round off to nearest higher N

Use N sections each scaled to delay of T_{total}/N

Impedance scale to practical values

Use high-Q Inductors to avoid dips at parallel resonant frequency

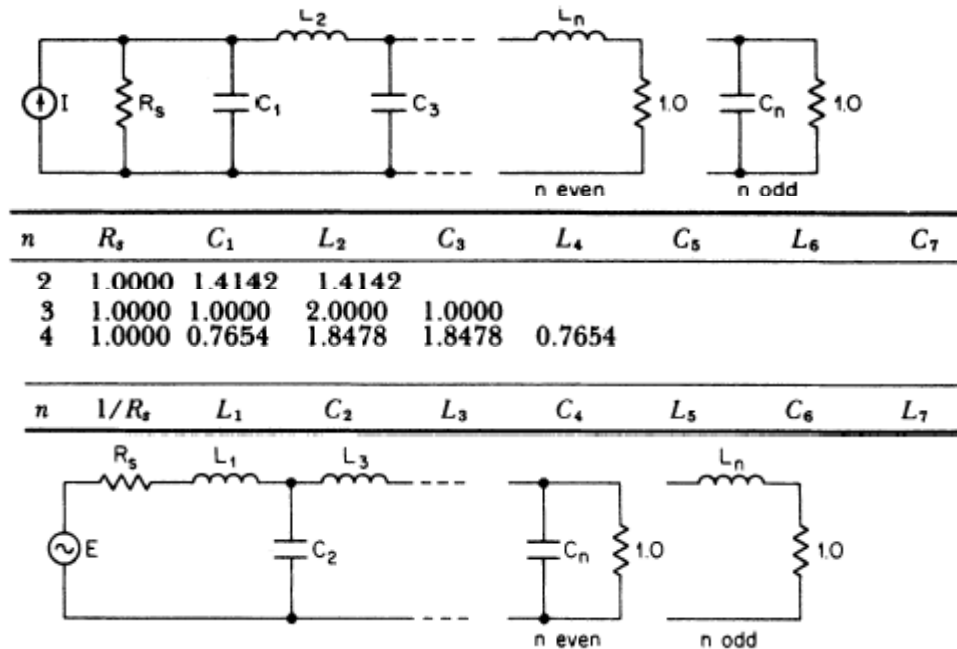
Duality

Any ladder network has a dual which has the same transfer function.

In order to transform a network into its dual:

- Inductors are transformed into capacitors and vice versa having the same element values (henrys into farads and vice versa)
- Resistors are transformed into conductances (ohms into mhos)
- Open circuit becomes a short circuit and vice versa
- Voltage sources become current sources and vice versa
- Series branches become shunt branches and vice versa
- Elements in parallel become elements in series and vice versa

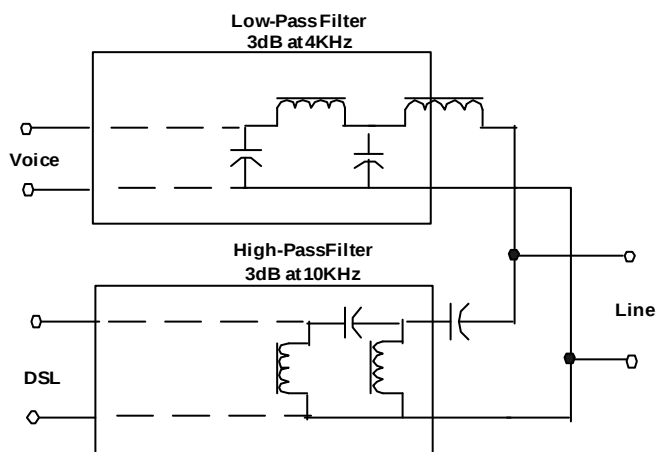
Note that the following table has schematics on both top and bottom which are duals of each other



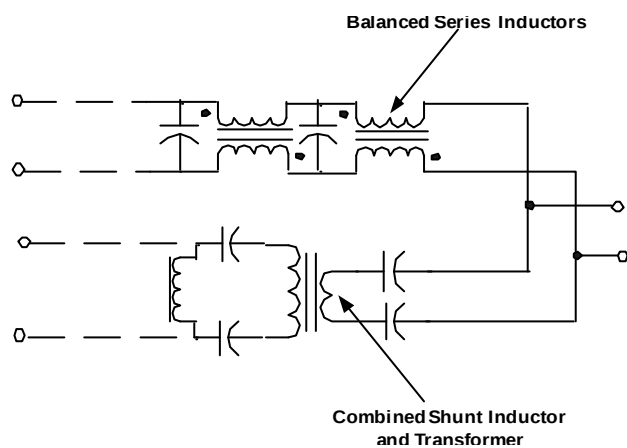
Out of Band Impedance of Low-Pass and High-Pass Filters to Allow Combining

- The input and/or output impedance of a low-pass and high-pass filter is determined to a great extent by the last element.
- For example a low-pass filter having a series inductor at the load end has a rising impedance at that end in the stop band (for rising frequencies).
- A high-pass filter having a series capacitor at the load end has a rising impedance in the stop band (for lower frequencies).
- This property allows the paralleling of low-pass and high-pass filters with minimal interaction as long as the pass-bands don't overlap. By selecting odd or even order filters and/or by using a circuits' dual, the appropriate series terminating element can be forced.

Simplified Low-Pass High-Pass Combining at Output

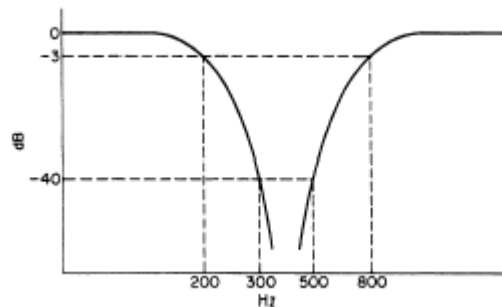
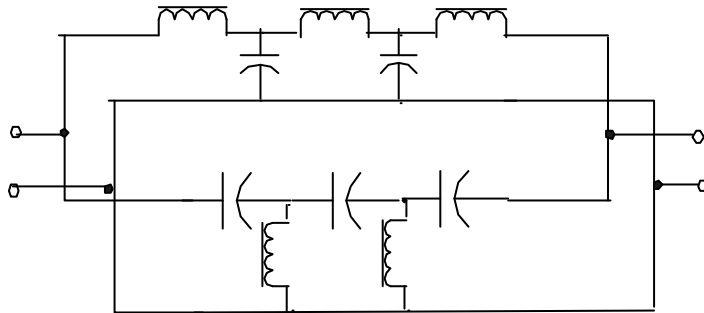


Practical Implementation in POTS Splitter

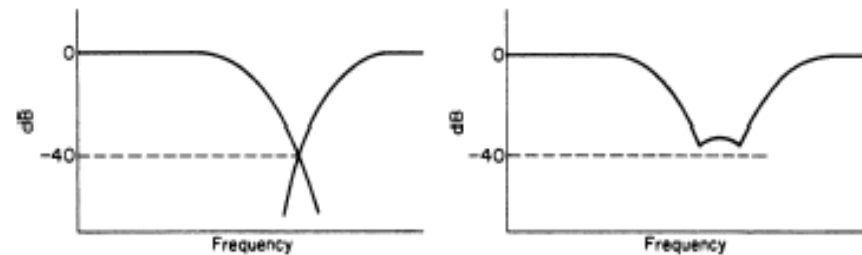


Wide Band Band-Reject Filter by Low-Pass High-Pass Filters in Parallel

The technique of connecting LC filters in parallel that have rising out-of-band impedance can be used to generate a wide-band band-reject filter. Wide-band is generally defined as at least one octave between cut-offs.



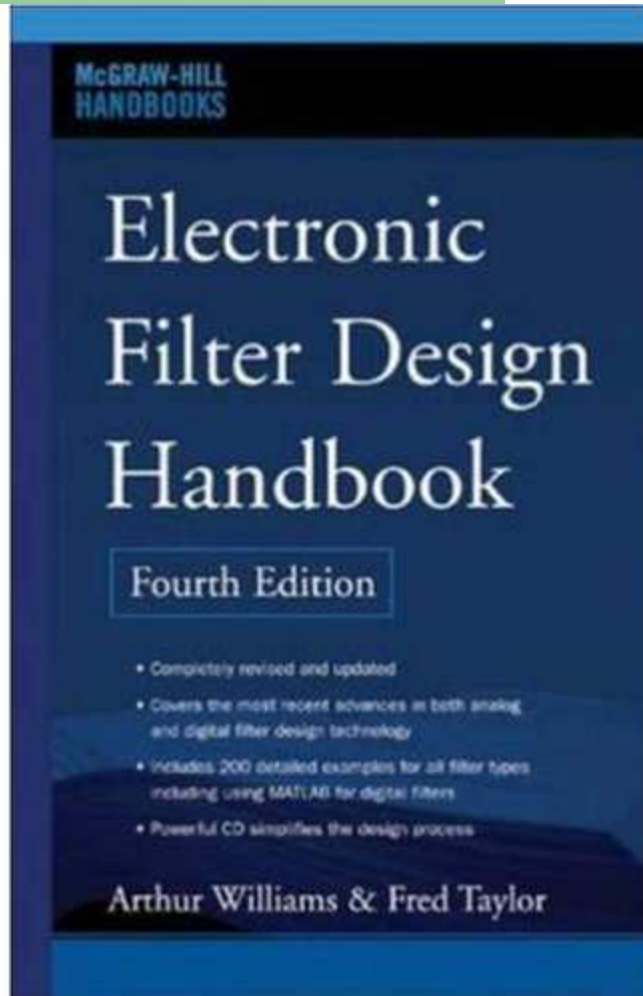
Example having sufficient separation of cut-offs



Individual Responses

Combined

Effect of Insufficient Separation



REFERENCE:

Electronic Filter Design Handbook
Fourth Edition (McGraw-Hill Handbooks)
[Arthur Williams](#) (Author)
[Fred J. Taylor](#) (Author)

From Amazon
<http://www.amazon.com/>

Or from McGraw Hill
<http://www.mhprofessional.com/>
Then enter Electronic Filter Design Handbook
for search

This is the *fourth* edition of the *Electronic Filter Design Handbook*. This book was first published in 1981. It was expanded in 1988 to include five additional chapters on digital filters and updated in 1995. This revised edition contains new material on both analog and digital filters. A CD-ROM has been included containing a number of programs which allow rapid design of analog filters from input requirements without the tedious mathematical computations normally encountered. The digital filter chapters are all integrated with a profusion of MATLAB examples.

Additional reference: "Filter Solutions" Software <http://www.filter-solutions.com/>